

# ECE 3040 Microelectronic Circuits

*Exam 1*

*September 30, 2015*

*Dr. W. Alan Doolittle*

Print your name clearly and largely:

*Solutions*

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## **Instructions:**

Read all the problems carefully and thoroughly before you begin working. You are allowed to use 1 sheet of notes (1 page front and back) as well as a calculator. There are 100 total points. Observe the point value of each problem and allocate your time accordingly. **SHOW ALL WORK AND CIRCLE YOUR FINAL ANSWER WITH THE PROPER UNITS INDICATED.** Write legibly. If I cannot read it, it will be considered a wrong answer. Do all work on the paper provided. Turn in all scratch paper, even if it did not lead to an answer. Report any and all ethics violations to the instructor. A periodic table is supplied on the last page. Good luck!

Sign your name on ONE of the two following cases:

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I DID NOT observe any ethical violations during this exam:

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I observed an ethical violation during this exam:

**First 33% Multiple Choice and True/False**  
**(Circle the letter of the most correct answer or answers )**

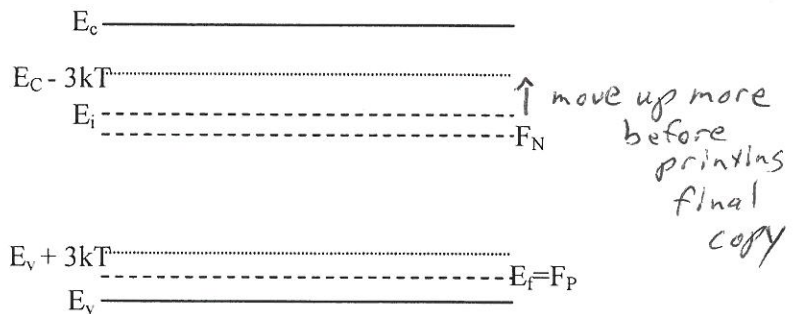
- 1.) (3-points) True or False: Valence electrons hold the crystal together and do not directly participate in conduction of electricity.
- 2.) (3-points) True or False: A high mobility (due to less frequent collisions with atoms) results from a low atomic density.
- 3.) (3-points) True or False: States that lie far below the fermi-energy are most likely filled.
- 4.) (3-points) True or False:  $(Al_{0.1}In_{0.50}Ga_{0.40}N_{0.3}P_{0.4}As_{0.3})$  is not a valid semiconductor formula in standard semiconductor notation because it has too many atoms.
- 5.) (3-points) True or False: The probability of a hole existing in a state is mathematically described by one minus the fermi-distribution function evaluated at the energy of that state.
- 6.) (3-points) True or False: The density of states describes the likelihood of a state being occupied.
- 7.) (3-points) True or False: The fermi-energy can never be found inside the conduction band.

Select the **best** answer or answers for 8-10:

- 8.) (4-points) Which of the following are true about diffusion currents ...
  - a.) ... they equal the drift current in equilibrium
  - b.) ... they are driven by electric field
  - c.) ... they only happen when there is an imbalance (gradient) in carrier concentration
  - d.) ... they are the smaller of the three types of current flow
  - e.) ... they always balance (negate) the drift velocity
  
- 9.) (4-points) Which of the following are true about partial ionization.
  - a.) You rarely need to be concerned with this since impurities are always totally ionized
  - b.) The degeneracy factor for donors results from two electrons having the same momentum
  - c.) The degeneracy factor for donors results from two electrons having the same spin (quantum numbers)
  - d.) The further the ionization energy is toward the center of the bandgap, the higher the ionization probability
  - e.) The degeneracy factor for acceptors is larger than that for donors because there are more valence bands than conduction bands

10.) (4-points) The following energy band diagram indicates the material is:

- a.) In equilibrium
- b.) Degenerate and n-type
- c.) Degenerate and p-type
- d.) Non-degenerate n-type
- e.) Non-degenerate p-type
- f.) In low level injection
- g.) In high level injection
- h.)  $m_n^* > m_p^*$
- i.)  $m_n^* < m_p^*$
- j.) In steady state



$$E_i = \frac{E_g}{2} + \frac{3}{4} kT \ln \left( \frac{m_p^*}{m_n^*} \right)$$

$$\Rightarrow m_p^* > m_n^*$$

*add before printing final copy*  
~~h.) In steady state~~

**Second 17% Short Answer ("Plug and Chug"):**

For the following problems (11-12) use the following material parameters and assuming total ionization:

For InP:

$n_i = 1.3 \times 10^7 \text{ cm}^{-3}$   $N_D = 1 \times 10^{15} \text{ cm}^{-3}$  donors  $N_A = 2 \times 10^{15} \text{ cm}^{-3}$  acceptors  $m_p^* = 0.6 m_0$   $m_n^* = 0.08 m_0$   
 $E_G = 1.344 \text{ eV}$  Electron mobility,  $\mu_n = 5000 \text{ cm}^2/\text{V-sec}$  Hole mobility,  $\mu_p = 150 \text{ cm}^2/\text{V-sec}$   
 Temperature = 27 degrees C

11.) (7-points) Where is the fermi energy (relative to the valence band which is referenced to zero energy)?

$$p = \frac{N_A - N_D}{2} + \sqrt{\frac{(N_A - N_D)^2}{4} + n_i^2} = 1 \times 10^{15} \text{ cm}^{-3} \quad n = \frac{n_i^2}{p} = \frac{(1.3 \times 10^7)^2}{1 \times 10^{15}} = 0.169 \text{ cm}^{-3}$$

$$E_i = \frac{E_g}{2} + \frac{3}{4} kT \ln\left(\frac{m_p^*}{m_n^*}\right) = 0.711 \text{ eV}$$

Several possible approaches

1)  $p = 1 \times 10^{15} = 1.3 \times 10^7 e^{(E_i - E_f)/kT}$   
 $E_f = 0.241 \text{ eV}$

2)  $n = 0.169 = 1.3 \times 10^7 e^{(E_f - E_i)/kT}$   
 $E_f = 0.241 \text{ eV}$

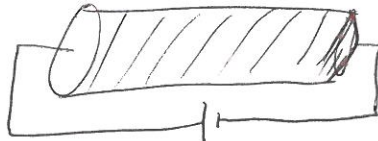
3)  $N_c = 2.51 \times 10^{19} \left(\frac{m_n^*}{m_0}\right)^{3/2} = 5.679 \times 10^{17} \text{ cm}^{-3}$   
 $0.169 = n = N_c e^{(E_f - E_c)/kT}$   
 $E_f = 0.239 \text{ eV}$

4)  $N_v = 2.59 \times 10^{19} \left(\frac{m_p^*}{m_0}\right)^{3/2}$   
 $1 \times 10^{15} = p = N_v e^{(E_v - E_f)/kT}$   
 $E_f = 0.243 \text{ eV}$

12.) (10-points) A 10  $\mu\text{m}$  diameter x 500  $\mu\text{m}$  long cylindrical semiconductor resistor is made from the semiconductor from problem 11. It is biased on two opposing sides (longest dimension) with 1.5 volt battery. Determine both the electron and hole current flowing in the device.

$$A = \pi (5 \times 10^{-4} \text{ cm})^2 = 7.854 \times 10^{-7} \text{ cm}^2$$

$$L = 500 \times 10^{-4} \text{ cm}$$



$$R_n = \frac{\rho_n L}{A} = 4.71 \times 10^{20} \Omega$$

massive

$$I_n = \frac{V}{R_n} = 3.2 \times 10^{-21} \text{ A}$$

practically zero!

$$\rho = \frac{1}{q(\mu_n n + \mu_p p)} \quad R = \frac{\rho L}{A}$$

$$\rho_n = \frac{1}{q \mu_n n} \quad \rho_p = \frac{1}{q \mu_p p} = 41.66 \Omega \cdot \text{cm}$$

$$\rho_n = 7.4 \times 10^{15} \Omega \cdot \text{cm}$$

$$R_p = \frac{\rho_p L}{A} = \frac{(41.66)(5 \times 10^{-2})}{7.854 \times 10^{-7}} = 2.65 \times 10^6 \Omega$$

$$I_p = \frac{V}{R_p} = 0.565 \mu\text{A}$$

**Section 3 (more short answer)**

13.) (10-points total) The material in problems 11 and 12 is exposed to the sun's light (like in a solar cell) that generates  $2 \times 10^{16} \text{ cm}^{-3}$  extra minority carriers.

a) (2 points) Is this low level or high level injection?

$$\Delta p = 2 \times 10^{16} > 1 \times 10^{15} \text{ so High Level}$$

$\uparrow$   
 $p_0$

b) (8 points) Draw the 1 dimensional energy band diagram showing the placement of both the quasi-fermi levels (numeric answer) relative to  $E_i$ ,  $E_c$ , and  $E_v$ .

$$n = 0.169 + 2 \times 10^{16}$$

$$n = 2 \times 10^{16}$$

$$n = 1.3 \times 10^{17} e$$

$$(F_n - E_i) / kT$$

$F_n = 1.26 \text{ eV}$

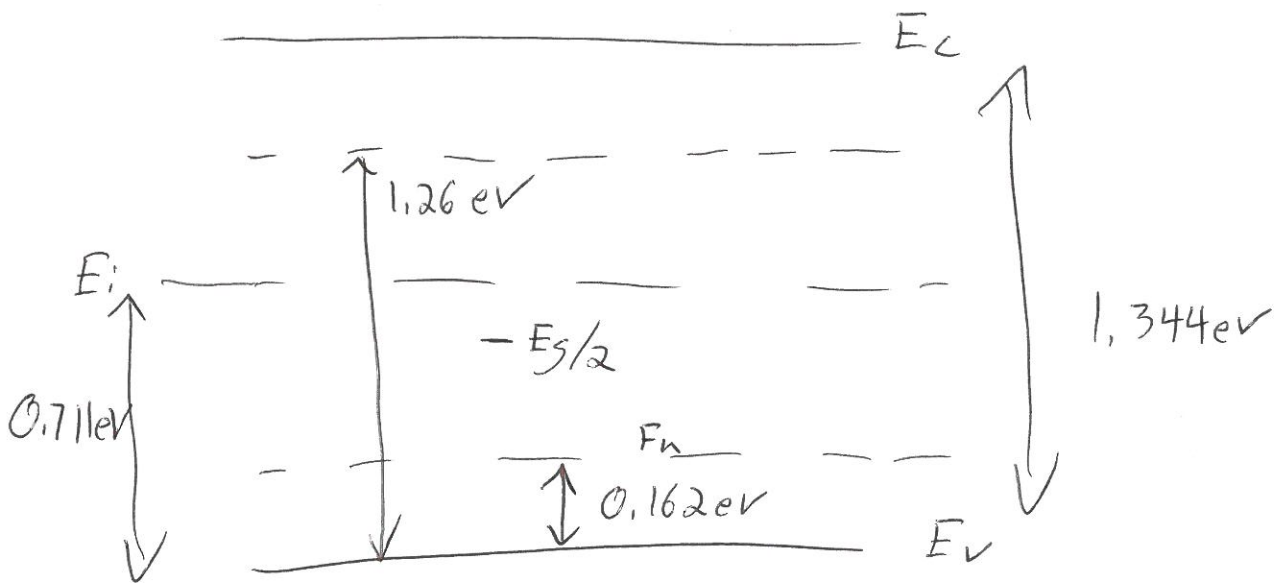
$$p = 1 \times 10^{15} + 2 \times 10^{16}$$

$$p = 2.1 \times 10^{16}$$

$$p = 1.3 \times 10^{17} e$$

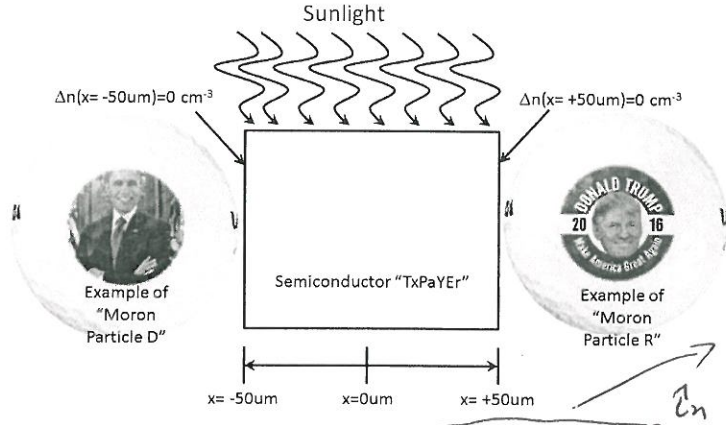
$$(E_i - F_p) / kT$$

$F_p = 0.162 \text{ eV}$



Pulling all the concepts together for a useful purpose:  
14.) (40-points)

(Humor intended to Diffuse Test Tension. Apologies if the choice of "morons" offends.)  
The world is made up of 4 types of particles; tiny electrons, protons, neutrons and gigantic morons. Morons are particles only found in government and have the ability to completely consume every other particle (electrons in this case). A 100 um length of a semiconductor named "TxPaYEr" has been constantly stuck between democrat morons and republican morons since February 3, 1913 when the 16<sup>th</sup> amendment was passed. The semiconductor is to be used in the presence of sunlight. The semiconductor is doped p-type with an acceptor concentration of  $1e17 \text{ cm}^{-3}$  and has a minority carrier lifetime of  $10^0 \text{ microseconds}$ . The sunlight is absorbed uniformly in the semiconductor generating an excess minority carrier concentration rate of  $10^{20} \text{ cm}^{-3}/\text{sec}$ . At both ends of the semiconductor (at +50 and -50 um), the democrat and republican morons act to steal minority carriers from the semiconductor "TxPaYEr" resulting in the excess electron concentration being zero at the semiconductor boundaries,  $\Delta n(x=+50)=\Delta n(x=-50)=0 \text{ cm}^{-3}$ . If the semiconductor is held at room temperature (27 degrees C), determine the minority carrier diffusion current density at all positions in the semiconductor ( $-50 \text{ um} \geq x \geq 50 \text{ um}$ ). Assume a minority carrier mobility of  $200 \text{ cm}^2/\text{Vsec}$  and the intrinsic concentration is  $1e14 \text{ cm}^{-3}$ .



62  
 concentration rate of  $10^{20} \text{ cm}^{-3}/\text{sec}$ .  
 BC Given, easy  
 $\Delta n(x=+50)=\Delta n(x=-50)=0 \text{ cm}^{-3}$ .  
 $200 \text{ cm}^2/\text{Vsec}$  and the intrinsic concentration is  $1e14 \text{ cm}^{-3}$ .

Given:  $0 = D_n \frac{d^2 \Delta n_p}{dx^2} - \frac{\Delta n_p}{\tau_n}$

General Solution is:  $\Delta n_p(x) = Ae^{-x/L_n} + Be^{+x/L_n}$

Given:  $0 = D_n \frac{d^2 \Delta n_p}{dx^2} - \frac{\Delta n_p}{\tau_n} + G_L$

General Solution is:  $\Delta n_p(x) = Ae^{-x/L_n} + Be^{+x/L_n} + G_L \tau_n$

Given:  $0 = D_n \frac{d^2 \Delta n_p}{dx^2}$

General Solution is:  $\Delta n_p(x) = A + Bx$

Given:  $0 = D_n \frac{d^2 \Delta n_p}{dx^2} + G_L$

General Solution is:  $\Delta n_p(x) = Ax^2 + Bx + C$

Given:  $0 = D_n \frac{d^2 \Delta n_p}{dx^2} + G_{LO} f(x)$  General Solution is:  $\Delta n_p(x) = \left[ -\frac{G_{LO}}{D_n} \iint f(x) dx \right] + Bx + C$

Given:  $\frac{d\Delta n_p}{dt} = -\frac{\Delta n_p}{\tau_n}$

General Solution is:  $\Delta n_p(t) = \Delta n_p(t=0)e^{-t/\tau_n}$

Given:  $0 = -\frac{\Delta n_p}{\tau_n} + G_L$

General Solution is:  $\Delta n_p = G_L \tau_n$

Extra work can be done here, but clearly indicate which problem you are solving.

$$D_n = \mu_n \left( \frac{kT}{q} \right) = 5.18 \text{ cm}^2/\text{sec}$$

$$L_n = \sqrt{D_n \tau_n} = \sqrt{5.18 (100 \times 10^{-6})} = 227.6 \text{ } \mu\text{m}$$

$$G_L \tau_n = (10^{20}) (100 \times 10^{-6}) = 1 \times 10^{16} \text{ cm}^{-3}$$

BC:

$$1) \Delta n(x = -50 \mu\text{m}) = 0 = A e^{50/227.6} + B e^{-50/227.6} + 1 \times 10^{16}$$

$$2) \Delta n(x = +50 \mu\text{m}) = 0 = A e^{-50/227.6} + B e^{+50/227.6} + 1 \times 10^{16}$$

Setting 1) = 2)

$$A e^{50/227.6} + B e^{-50/227.6} = A e^{-50/227.6} + B e^{50/227.6}$$

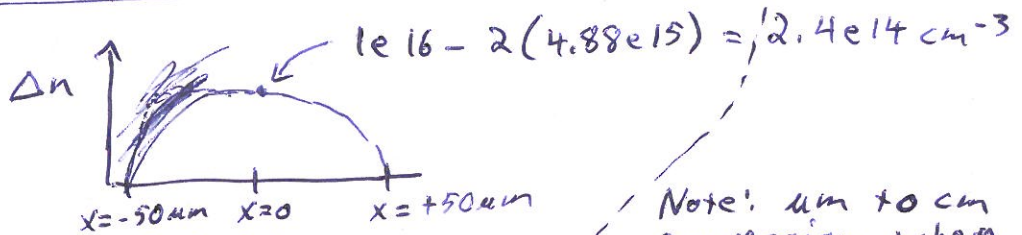
$$A (e^{50/227.6} - e^{-50/227.6}) = B (e^{50/227.6} - e^{-50/227.6})$$

Subbing into 1)  $A = B$

$$0 = A (e^{50/227.6} + e^{-50/227.6}) + 1 \times 10^{16}$$

$$A = B = -4.88 \times 10^{15} \text{ cm}^{-3}$$

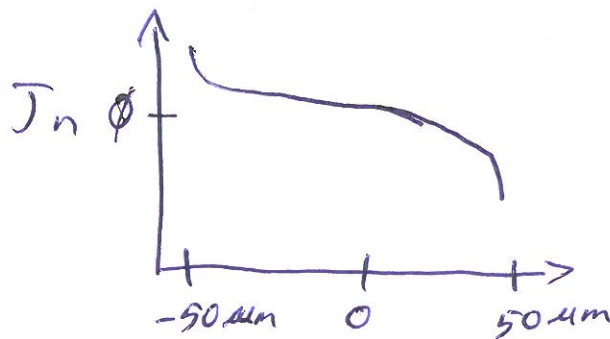
$$\Delta n(x) = -4.88 \times 10^{15} [e^{-x/227.6 \mu\text{m}} + e^{+x/227.6}] + 1 \times 10^{16} \text{ cm}^{-3}$$



$$J_n = q D_n \frac{\partial \Delta n(x)}{\partial x}$$

Note:  $\mu\text{m}$  to  $\text{cm}$  conversion when taking derivative

$$J_n = 0.177 [e^{-x/227.6} - e^{x/227.6}] \text{ A/cm}^2$$

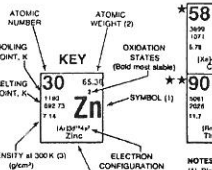


Extra work can be done here, but clearly indicate which problem you are solving.

# PERIODIC TABLE OF THE ELEMENTS

Table of Selected Radioactive Isotopes

GROUP	Table of Selected Radioactive Isotopes																VIII
IA																	2
1 H 1.00794																	2 He 4.00260
2 Li 6.941																	10 Ne 20.179
3 Be 9.01218																	18 Ar 39.948
4 B 10.811																	36 Kr 83.80
5 C 12.011																	54 Xe 131.30
6 N 14.007																	86 Rn 222
7 O 15.999																	
8 F 18.998																	
9 Ne 19.992																	
10 Na 22.990																	
11 Mg 24.305																	
12 Al 26.982																	
13 Si 28.086																	
14 P 30.974																	
15 S 32.06																	
16 Cl 35.453																	
17 Ar 39.948																	
18 K 39.098																	
19 Ca 40.078																	
20 Sc 44.956																	
21 Ti 47.88																	
22 V 50.942																	
23 Cr 51.996																	
24 Mn 54.938																	
25 Fe 55.845																	
26 Co 58.933																	
27 Ni 58.69																	
28 Cu 63.546																	
29 Zn 65.38																	
30 Ga 69.723																	
31 Ge 72.63																	
32 As 74.922																	
33 Se 78.96																	
34 Br 79.904																	
35 Kr 83.80																	
36 Rb 85.468																	
37 Sr 87.62																	
38 Y 88.906																	
39 Zr 91.224																	
40 Nb 92.906																	
41 Mo 95.94																	
42 Tc 98.906																	
43 Ru 101.07																	
44 Rh 102.905																	
45 Pd 106.42																	
46 Ag 107.868																	
47 Cd 112.411																	
48 In 114.818																	
49 Sn 118.710																	
50 Sb 121.757																	
51 Te 127.60																	
52 I 126.905																	
53 Xe 131.29																	
54 Cs 132.905																	
55 Ba 137.327																	
56 La 138.905																	
57 Ce 140.12																	
58 Pr 140.907																	
59 Nd 144.24																	
60 Pm 144.9126																	
61 Sm 150.36																	
62 Eu 151.964																	
63 Gd 157.25																	
64 Tb 158.925																	
65 Dy 162.50																	
66 Ho 164.930																	
67 Er 167.26																	
68 Tm 168.934																	
69 Yb 173.054																	
70 Lu 174.967																	
71 Hf 178.49																	
72 Ta 180.948																	
73 W 183.85																	
74 Re 186.207																	
75 Os 190.23																	
76 Ir 192.225																	
77 Pt 195.084																	
78 Au 196.967																	
79 Hg 200.59																	
80 Tl 204.387																	
81 Pb 207.2																	
82 Bi 208.980																	
83 Po 209																	
84 At 210																	
85 Rn 222																	
86 Fr 223																	
87 Ra 226																	
88 Ac 227																	
89 Th 232																	
90 Pa 231																	
91 U 238																	
92 Np 237																	
93 Pu 239																	
94 Am 243																	
95 Cm 247																	
96 Bk 247																	
97 Cf 251																	
98 Es 252																	
99 Fm 257																	
100 Md 258																	
101 No 259																	
102 Lr 260																	



ATOMIC NUMBER	58	59	60	61	62	63	64	65	66	67	68	69	70	71
58	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

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