

ECE 3040 Microelectronic Circuits

Exam 1

February 15, 2017

24 minutes

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Print your name clearly and largely:

Solutions

Instructions:

Read all the problems carefully and thoroughly before you begin working. You are allowed to use 1 sheet of notes (1 page front and back) as well as a calculator. There are 100 total points. Observe the point value of each problem and allocate your time accordingly. **SHOW ALL WORK AND CIRCLE YOUR FINAL ANSWER WITH THE PROPER UNITS INDICATED. Write legibly. If I cannot read it, it will be considered a wrong answer.** Do all work on the paper provided. Turn in all scratch paper, even if it did not lead to an answer. **Turn in your notes sheet.** Report any and all ethics violations to the instructor. A periodic table is supplied on the last page. Good luck!

Sign your name on ONE of the two following cases:

I DID NOT observe any ethical violations during this exam:

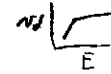
I observed an ethical violation during this exam:

First 33% Multiple Choice and True/False
(Circle the letter of the most correct answer or answers)

- 1.) (3-points) True or False: The energy bandgap is generally larger in materials with strong chemical bonds.
- 2.) (3-points) True or False: Metals are conductive because each atom prefers to not release its electrons to the electron cloud.
- 3.) (3-points) True or False: The density of states determines how likely the state is to be occupied.
- 4.) (3-points) True or False: $Al_{0.2}In_{0.50}Ga_{0.40}N_{0.4}P_{0.4}As_{0.4}$ is a valid semiconductor formula in standard semiconductor notation.
- 5.) (3-points) True or False: The fermi distribution function determines the probability of a hole existing in a state.
- 6.) (3-points) True or False: In a degenerately doped semiconductor, one must use partial ionization. *1-f(E)*
Ambiguous question; either answer accepted
- 7.) (3-points) True or False: If a material is non-degenerately doped, we know the fermi energy is located inside the bandgap and is at least $3kT$ away from either the conduction or valence band.

Select the **best** answer or answers for 8-10:

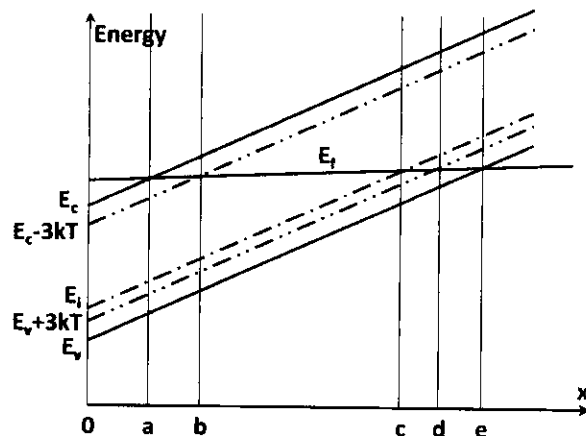
- 8.) (4-points) Which of the following are true about drift currents ...
 - a.) ... they only result from electric fields created by dopants
 - b.) ... they are driven by electric field
 - c.) ... they always result in diffusion currents that balance
 - d.) ... they are the smaller of the three types of current flow
 - e.) ... they are constant at high electric fields but vary linearly with electric field strength at low electric fields.



- 9.) (4-points) Which of the following are true about the fermi-distribution function.
 - a.) The product of the fermi-distribution function and the density of states results in a distribution of electron concentrations as a function of energy.
 - b.) The fermi-distribution function decays exponentially at higher energy
 - c.) The fermi-distribution function is always equal to $1/2$ at energy equal to the fermi-energy
 - d.) The fermi-distribution function reduces to a simple exponential for energies far away from the fermi-energy

10.) (4-points) The following energy band diagram indicates the material is:

- a.) In equilibrium E_f flat
- b.) In Steady State
- c.) Degenerate and n-type for $x < b$
- d.) Degenerate and p-type for $x > d$
- e.) Non-degenerate n-type for $b < x < c$
- f.) Non-degenerate p-type for $c < x < d$
- g.) In low level injection
- h.) In high level injection
- i.) $m_n^* > m_p^*$
- j.) $m_n^* < m_p^*$
- k.) Has zero electric field
- l.) Has a non-zero electric field everywhere



Short Answer ("Plug and Chug"):

For the following problems (11-12) use the following material parameters and assuming total ionization:

For InP:

$n_i = 1.3e7 \text{ cm}^{-3}$ $N_D = 1e17 \text{ cm}^{-3}$ donors $N_A = 1.2e17 \text{ cm}^{-3}$ acceptors $m_p^* = 0.6m_0$ $m_n^* = 0.08m_0$
 $E_G = 1.344 \text{ eV}$ Electron mobility, $\mu_n = 5000 \text{ cm}^2/\text{V-sec}$ Hole mobility, $\mu_p = 150 \text{ cm}^2/\text{V-sec}$
 Temperature = 27 degrees C

11.) (5-points) Where is the fermi energy (relative to the valence band which is referenced to zero energy)?

$$p_0 = \frac{N_A - N_D}{2} + \sqrt{\frac{(N_A - N_D)^2}{4} + n_i^2} = 2e16 \text{ cm}^{-3} \quad n_0 = \frac{n_i^2}{p_0} = \frac{(1.3e7)^2}{2e16} = 0.00845 \text{ cm}^{-3}$$

$$E_i = \frac{E_g}{2} + \frac{3}{4} kT \ln\left(\frac{m_p^*}{m_n^*}\right) = 0.711 \text{ eV}$$

Several Approaches:

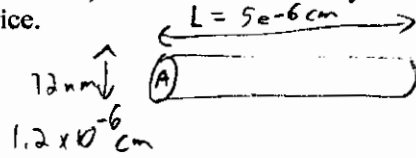
$$1) \quad p = 2e16 = n_i e^{(E_i - E_f)/kT} \\ \Rightarrow E_f = 0.163 \text{ eV}$$

$$2) \quad n = 0.00845 \text{ cm}^{-3} = n_i e^{(E_f - E_i)/kT} \\ E_f = 0.163 \text{ eV}$$

$$3) \quad N_C = 2.51 \times 10^{19} \left(\frac{m_n^*}{m_0}\right)^{3/2} \\ = 5.679e17 \text{ cm}^{-3} \quad 1.344 \\ n = 0.00845 \text{ cm}^{-3} = N_C e^{(E_f - E_C)/kT} \\ E_f = 0.161 \text{ eV}$$

$$4) \quad N_V = 2.51 \times 10^{19} \left(\frac{m_p^*}{m_0}\right)^{3/2} \\ p = N_V e^{(E_V - E_f)/kT} \\ E_f = 0.165 \text{ eV}$$

12.) (8-points) A 12 nm (1 nm = 1e-9 m) diameter x 50 nm long cylindrical semiconductor resistor is made from the semiconductor from problem 11 for use in a microprocessor. It is biased on two opposing sides (longest dimension) with a 0.7 volt battery. Determine both the electron and hole currents flowing in the device.

$$\text{Area } A = \pi (0.6 \times 10^{-6})^2 = 1.13e-12 \text{ cm}^2$$


$L = 5e-6 \text{ cm}$

$$\rho = \frac{1}{q(\mu_n n + \mu_p p)} \quad R = \frac{\rho L}{A}$$

$$\rho_n = \frac{1}{q\mu_n n} \quad \rho_p = \frac{1}{q\mu_p p}$$

$$\rho_n = 1.47e17 \text{ } \Omega\text{-cm} \quad \rho_p = 2.08 \text{ } \Omega\text{-cm}$$

$$R_n = 6.54e23 \text{ } \Omega \quad R_p = 9.21e6$$

$$I_n = 1e-24 \text{ Amps} \quad I_p = 76 \text{ nA}$$

Section 3 (more short answer)

13.) (14-points total) The material in problems 11 and 12 is exposed to the sun's light (like in a solar cell) that generates $1e19 \text{ cm}^{-3}$ extra electron - hole pairs.

a) (2 points) Is this low level or high level injection?

$$p = \Delta p + p_0 = 1e19 + 2e16 \approx 1e19 \text{ cm}^{-3}$$

High level injection

b) (8 points) Draw the 1 dimensional energy band diagram showing the placement of both the quasi-fermi levels (E_{fn} and E_{fp} - should be a numeric answer) relative to E_i , E_c , and E_v .

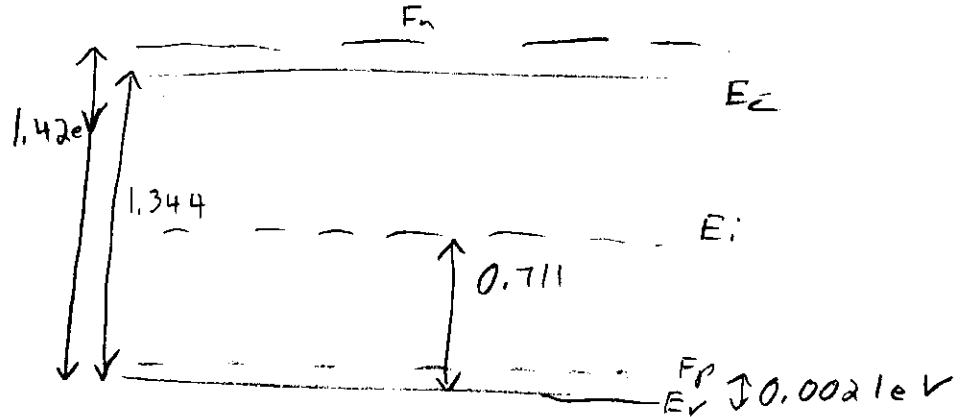
$$F_n: n = n_i e^{(F_n - E_i)/kT}$$

$$F_n = 1.42 \text{ eV}$$

$$F_p: p = n_i e^{(E_i - F_p)/kT}$$

$$p_0 + \Delta p \approx 1.002e19 \text{ cm}^{-3}$$

$$F_p = 0.0021 \text{ eV}$$



c) (4 - points) What is the total current flowing when light is present?

$$R = \frac{1}{q(u_n n + u_p p)}$$

$$= \frac{1}{1.6e-19 (5000 \times 1e19 + 150 \times 1e19)}$$

$$R = \frac{\rho L}{A}$$

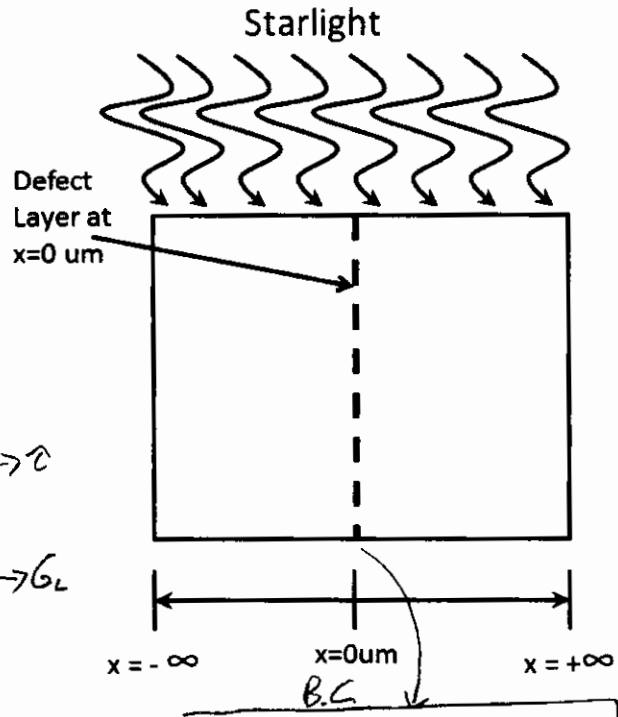
$$R = 537 \Omega$$

$I = 1.3 \text{ mA}$

Pulling all the concepts together for a useful purpose:

14.) (40-points)

An infinite slab of semiconductor extends from positive to negative infinity. For a very long time, starlight has constantly illuminated the semiconductor and is absorbed uniformly with a very small absorption coefficient. The semiconductor is doped p-type with an acceptor concentration of $5 \times 10^{15} \text{ cm}^{-3}$ and has a minority carrier lifetime of 2×10^{-6} microseconds. The sunlight is absorbed uniformly in the semiconductor generating an excess minority carrier concentration rate of $10^{14} \text{ cm}^{-3}/\text{sec}$. At the center of the semiconductor at $x=0$, a defect layer exists which results in a lower excess minority carrier concentration than anywhere else in the semiconductor.



Thus, at $x=0$, $\Delta n(x=0) = 1 \times 10^8 \text{ cm}^{-3}$. If

the semiconductor is held at room temperature (27 degrees C), determine the minority carrier diffusion current density at all positions in the semiconductor ($-\infty \geq x \geq \infty$). Assume a minority carrier mobility of $2 \text{ cm}^2/\text{Vsec}$ and the intrinsic concentration is $1 \times 10^{-14} \text{ cm}^{-3}$.

Hint: It may be helpful to break this problem up into two symmetric problems.

$L_n = \sqrt{D_n \tau_n} = \sqrt{0.0518 (2 \times 10^{-6})} = 3.219 \mu\text{m}$ $D_n = \frac{kT}{q} \mu_n = 0.0518 \text{ cm}^2/\text{sec}$

Given: $0 = D_n \frac{d^2 \Delta n_p}{dx^2} - \frac{\Delta n_p}{\tau_n}$ General Solution is: $\Delta n_p(x) = A e^{-x/L_n} + B e^{+x/L_n}$

$-\infty < x < \infty$ Given: $0 = D_n \frac{d^2 \Delta n_p}{dx^2} - \frac{\Delta n_p}{\tau_n} + G_L$ General Solution is: $\Delta n_p(x) = A e^{-x/L_n} + B e^{+x/L_n} + G_L \tau_n$

Given: $0 = D_n \frac{d^2 \Delta n_p}{dx^2}$ General Solution is: $\Delta n_p(x) = A + Bx$

Given: $0 = D_n \frac{d^2 \Delta n_p}{dx^2} + G_L$ General Solution is: $\Delta n_p(x) = Ax^2 + Bx + C$

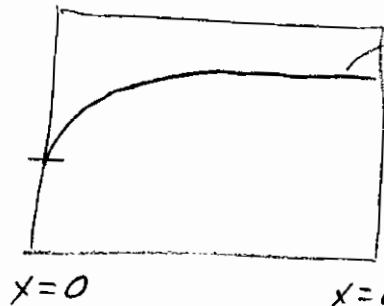
Given: $0 = D_n \frac{d^2 \Delta n_p}{dx^2} + G_L f(x)$ General Solution is: $\Delta n_p(x) = \left[-\frac{G_L}{D_n} \iint f(x) dx^2 \right] + Bx + C$

Given: $\frac{d \Delta n_p}{dt} = -\frac{\Delta n_p}{\tau_n}$ General Solution is: $\Delta n_p(t) = \Delta n_p(t=0) e^{-t/\tau_n}$

$x = \pm \infty$ Given: $0 = -\frac{\Delta n_p}{\tau_n} + G_L$ General Solution is: $\Delta n_p = G_L \tau_n$

Extra work can be done here, but clearly indicate which problem you are solving.

Use $\infty > x \geq 0$: (Negative $1/2$ is same due to symmetry or you could solve it twice)



@ $x = +\infty$

$$\Delta n(x=\infty) = G_L \tau_n =$$

Note: If you don't see this then see * below

$$\Delta n_p(x) = A e^{-x/L_n} + B e^{+x/L_n} + G_L \tau_n$$

B.C. 1: * $\Delta n_p(x=\infty) = A(0) + B(\infty) + G_L \tau_n$

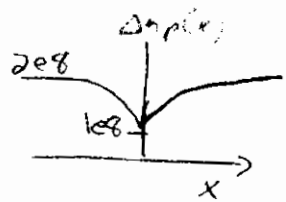
$B \Rightarrow 0$ in order to have a physical meaning

$$(\Delta n_p(x=\infty) = G_L \tau_n = 2e8 \text{ cm}^{-3})$$

B.C. 2: $\Delta n(x=0) = 1e8 \text{ cm}^{-3} = A e^0 + 0 e^0 + G_L \tau_n$
 $= A + 2e8 \text{ cm}^{-3}$

$$A = -1e8 \text{ cm}^{-3}$$

$x \geq 0$	$\Delta n(x) = 2e8 - 1e8 e^{-x/3.219 \mu\text{m}} \text{ [cm}^{-3}\text{]}$
$x \leq 0$	$\Delta n(x) = 2e8 - 1e8 e^{+x/3.219 \mu\text{m}} \text{ [cm}^{-3}\text{]}$



by symmetry,
 $A=0 + B = -1e8 \text{ cm}^{-3}$

$$J_n = q D_n \frac{d\Delta n_p(x)}{dx}$$

$$= (1.6e-19) (0.0518) \frac{[1e8 \text{ cm}^{-3}]}{(3.219 \times 10^{-4} \text{ cm})} e^{-x/3.219 \mu\text{m}}$$

note units $\equiv \text{cm}$

$x \geq 0$	$J_n = + 2.57 \text{ nA} e^{-x/3.219 \mu\text{m}} \text{ A/cm}^2$
$x \leq 0$	$J_n = - 2.57 \text{ nA} e^{+x/3.219 \mu\text{m}} \text{ A/cm}^2$



Extra work can be done here, but clearly indicate which problem you are solving.

PERIODIC TABLE OF THE ELEMENTS

Table of Selected Radioactive Isotopes

GROUP	Table of Selected Radioactive Isotopes																VIII
IA																	He
1																	2
3																	10
11																	18
19																	36
37																	54
55																	86
87																	118

(Note: The above table is a simplified representation of the periodic table showing element symbols and atomic numbers. The actual image contains detailed data for each element, including names, symbols, and atomic numbers.)

KEY

- ATOMIC NUMBER
- ATOMIC WEIGHT (2)
- OXIDATION STATES (Most may have)
- SYMBOL (Z)
- ELECTRON CONFIGURATION
- NAME
- SOLID POINT (K)
- MELTING POINT (K)
- DENSITY at 20°C (g/cm³)

(Note: This key is used to interpret the data provided for each element in the periodic table.)

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	91	92	93	94	95	96	97	98	99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

NOTES:

- (1) Solid - red; Gas - blue; Liquid - green.
- (2) Based upon atomic weight (A) indicates most stable of isotopes.
- (3) Radioactive isotopes are indicated by the atomic number (Z) and the mass number (M) in the upper right corner.
- (4) Elements with no stable isotopes are indicated by the atomic number (Z) and the mass number (M) in the upper right corner.

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