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# ECE 4813

## Semiconductor Device and Material Characterization

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As with all of these lecture slides, I am indebted to Dr. Dieter Schroder from Arizona State University for his generous contributions and freely given resources. Most of (>80%) the figures/slides in this lecture came from Dieter. Some of these figures are copyrighted and can be found within the class text, *Semiconductor Device and Materials Characterization*. **Every serious microelectronics student should have a copy of this book!**



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# Diodes

PN Junction Diodes

Current - Voltage

Series Resistance

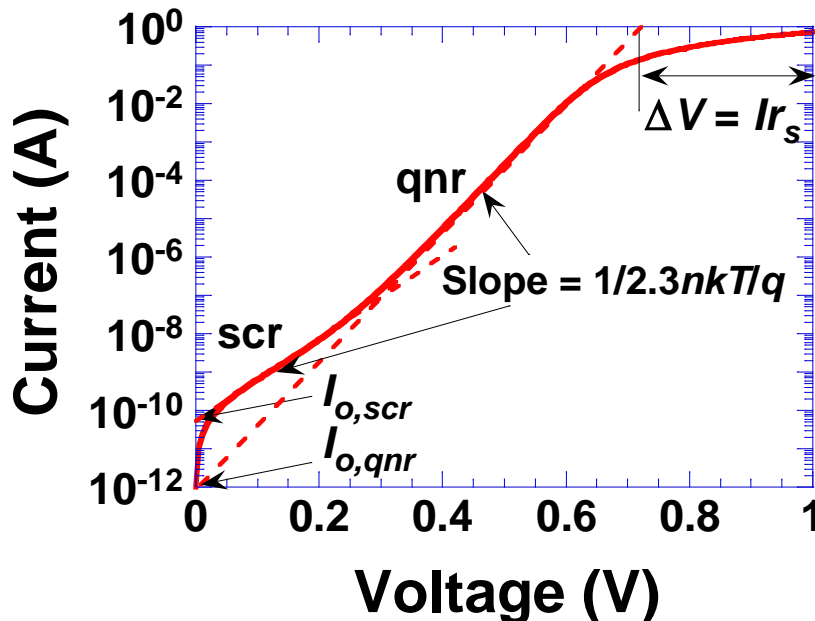
Schottky Diodes



# PN Junction Diodes

- The current in a Si pn junction diode at room temperature is due to recombination in the *space-charge region*,  $I_{scr}$  and the *quasi-neutral regions*,  $I_{qnr}$

$$I = I_{o,scr} \left( \exp\left(\frac{q(V - Ir_s)}{n_{scr}kT}\right) - 1 \right) + I_{o,qnr} \left( \exp\left(\frac{q(V - Ir_s)}{n_{qnr}kT}\right) - 1 \right)$$



For  $V > 3kT/q$  and negligible  $r_s$ :

$$I = I_o \exp\left(\frac{qV}{nkT}\right)$$

$$\log I = \log I_o + qV/nkT \ln 10$$

$$V = 0 \text{ intercept} \Rightarrow I = I_o$$

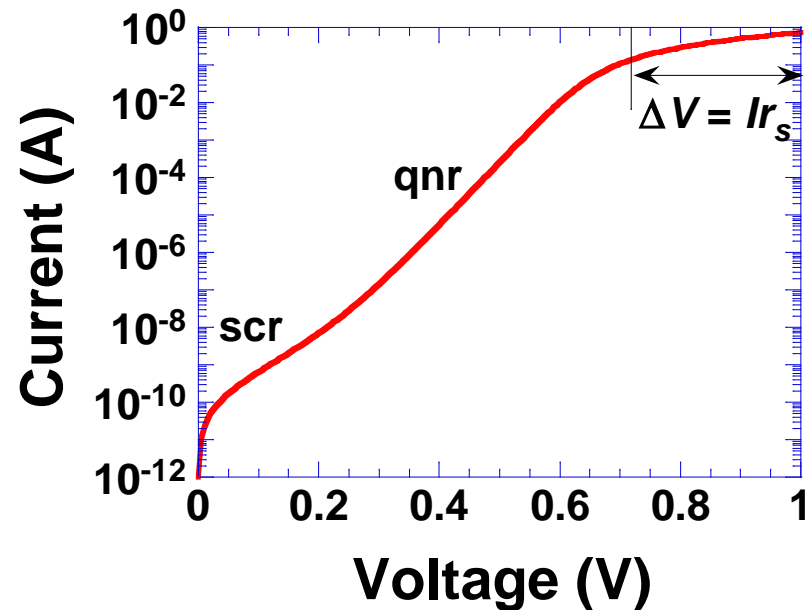
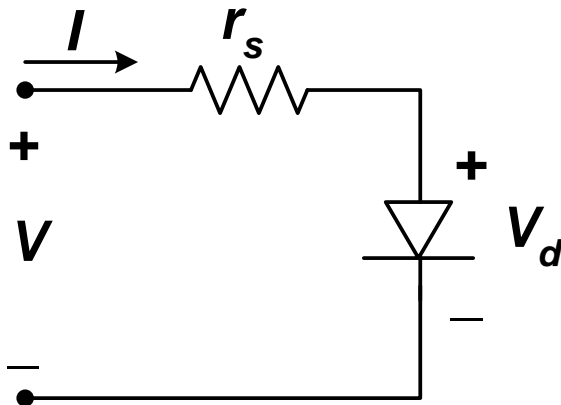
$$\text{Slope} = \frac{d \log I}{dV} = \frac{1}{\ln 10 nkT/q}$$

# PN Junction Diode Resistance

- Diode series resistance reduces the current

$$I = I_0 \left( \exp\left(\frac{qV_d}{nkT}\right) - 1 \right) \quad V = V_d + Ir_s$$

$$I = I_0 \left( \exp\left(\frac{q(V - Ir_s)}{nkT}\right) - 1 \right)$$



# Diode Resistance

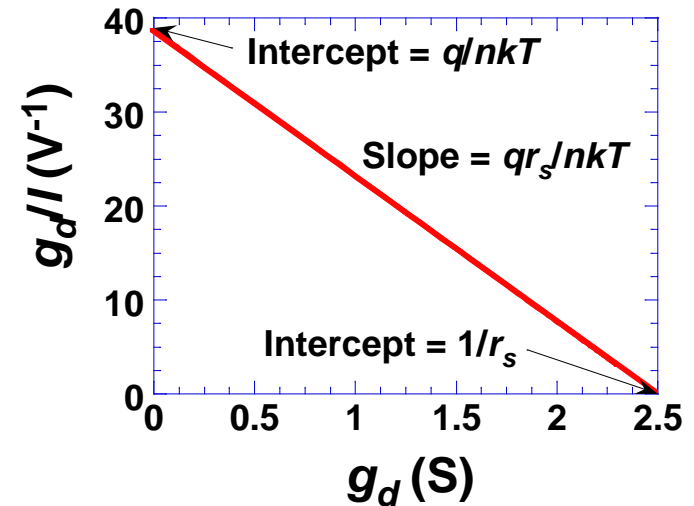
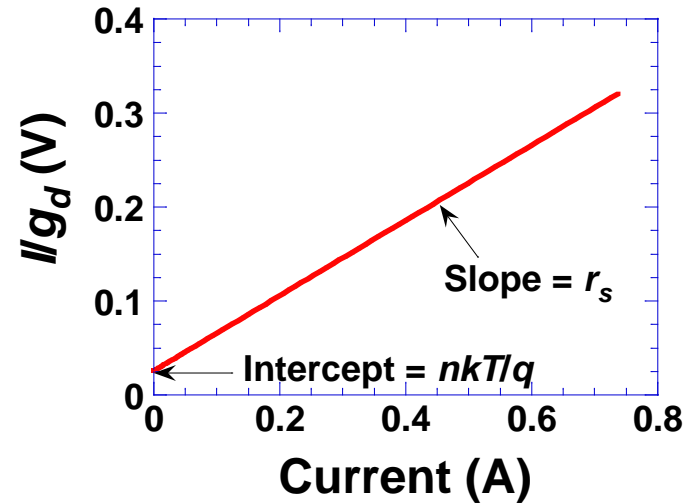
$$I = I_o \exp\left(\frac{q(V - Ir_s)}{nkT}\right)$$

■ Diode conductance

$$g_d = \frac{I(1 - r_s g_d)}{nkT/q}$$

$$\frac{g_d}{I} = \frac{1 - r_s g_d}{nkT/q}$$

$$\frac{I}{g_d} = \frac{nkT}{q} + Ir_s$$



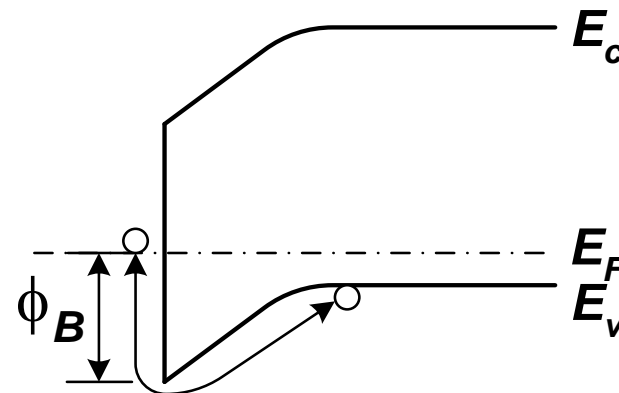
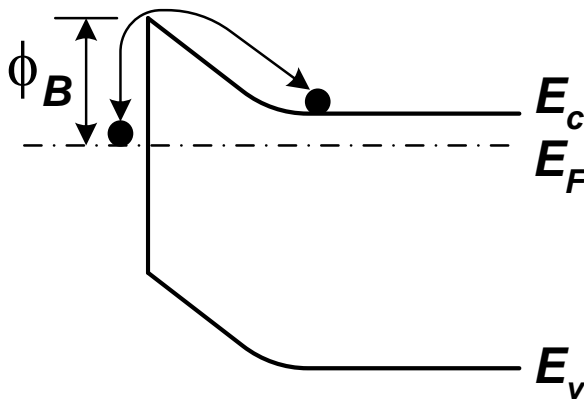
# Schottky Barrier Diodes

- Schottky barrier diodes have  $I$ - $V$  curves very similar to  $pn$  junction diodes
- The turn-on voltage can be controlled more than that of  $pn$  diodes because the barrier height can be controlled somewhat

$$I = I_s (e^{qV/nkT} - 1); \quad I_s = AA^* T^2 e^{-q\phi_B/kT}$$

$$A^* = 4\pi q k^2 m_n^* / h^3 = 120 (m_0 / m_n^*) \text{ A/cm}^2 \text{K}^2$$

Richardson Constant





# Schottky Barrier Diodes: $I - V$

$$I = I_s (e^{qV/nkT} - 1); \quad I_s = AA^* T^2 e^{-q\phi_B/kT}$$

Want  $n$ ,  $A^*$  and  $\phi_B$

## ■ Current - Voltage

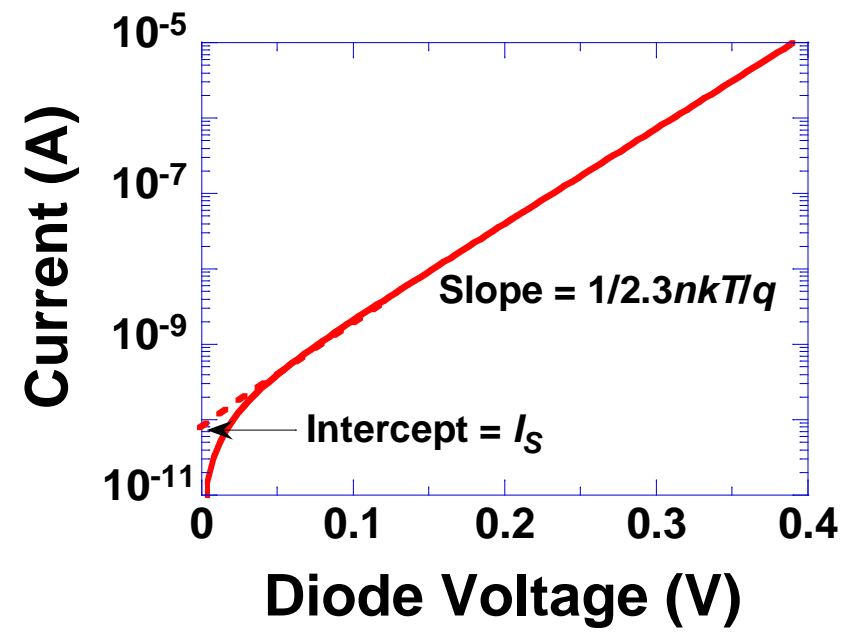
$$\log I = \log I_s + qV/nkT \ln 10$$

$V = 0$  intercept  $\Rightarrow I = I_s$

$$\text{Slope} = \frac{d \log I}{dV} = \frac{1}{\ln 10 nkT/q}$$

$$\phi_B = \frac{kT}{q} \ln \left( \frac{AA^* T^2}{I_s} \right)$$

Need to know  $A^*$



$$\text{For } V \geq 4 kT/q \Rightarrow I = I_s e^{qV/nkT}$$



# Schottky Barrier Diodes: $I - T$

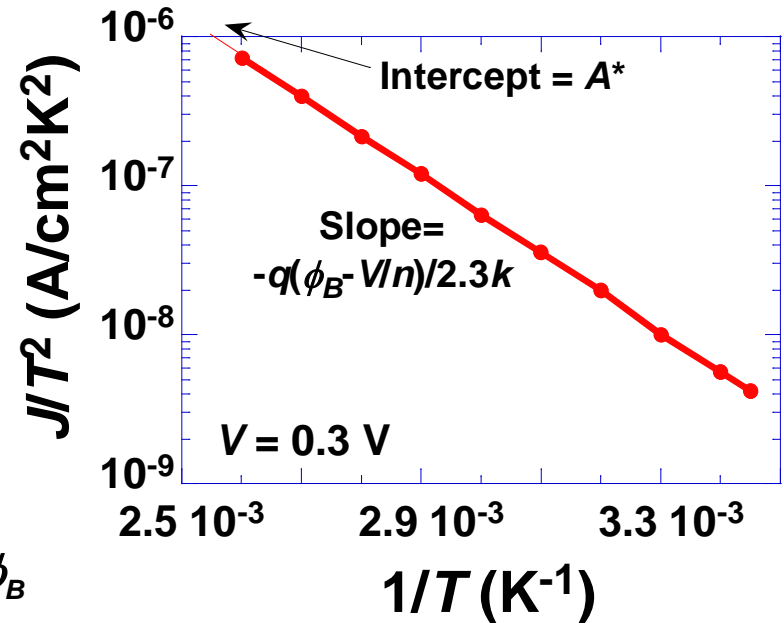
- $\log(J/T^2)$  versus  $1/T$ 
  - ◆ To determine  $\phi_B$  and  $A^*$

$$J = A^* T^2 \exp(-q(\phi_B - V/n)/kT)$$

$$\ln(J/T^2) = \ln A^* - \frac{q(\phi_B - V/n)}{kT}$$

$1/T = 0$  intercept =  $A^*$

$$\text{Slope} = \frac{d \log(J/T^2)}{d(1/T)} = -\frac{q(\phi_B - V/n)}{k \ln(10)} \Rightarrow \phi_B$$

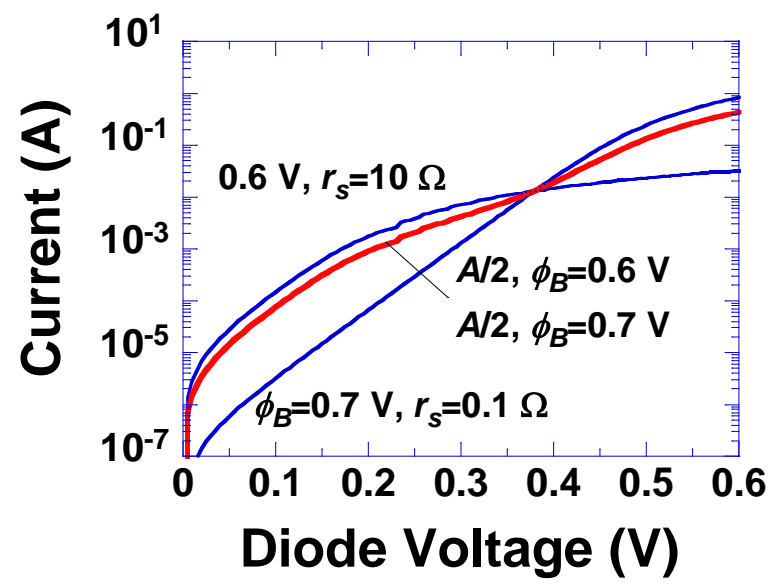
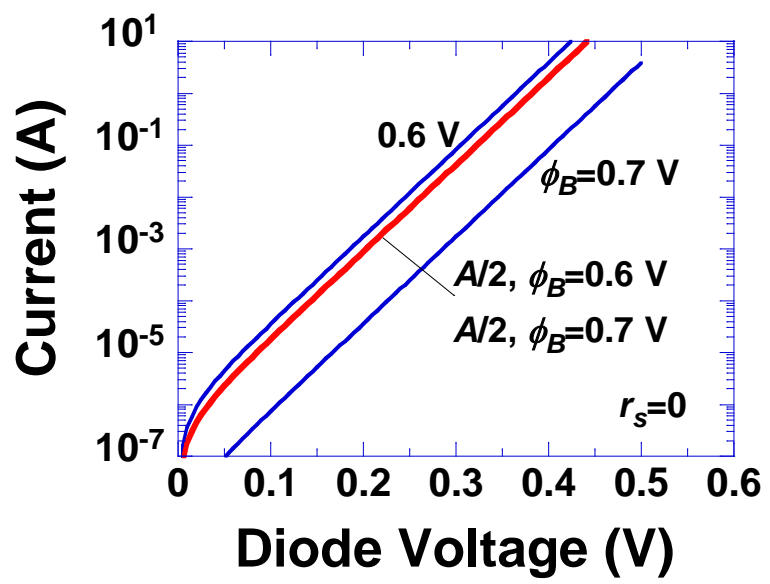






# Schottky Barrier Diodes: $I - V$

- Barrier height can be determined from  $I - V$  or  $I - T$  plots
- Forward-biased current is very sensitive to barrier height
- If barrier height non-uniform, the lowest barrier height regions dominate
- Series resistance is important



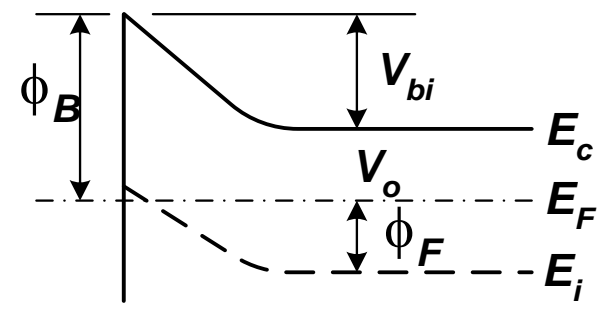


# Schottky Barrier Diodes: C - V

- C-V measurements are less sensitive to  $\phi_B$  variations

$$\frac{C}{A} = \sqrt{\frac{qK_s\epsilon_0 N_D}{2(V_{bi} - V)}}$$

$$\left(\frac{A}{C}\right)^2 = \frac{2(V_{bi} - V)}{qK_s\epsilon_0 N_D}$$



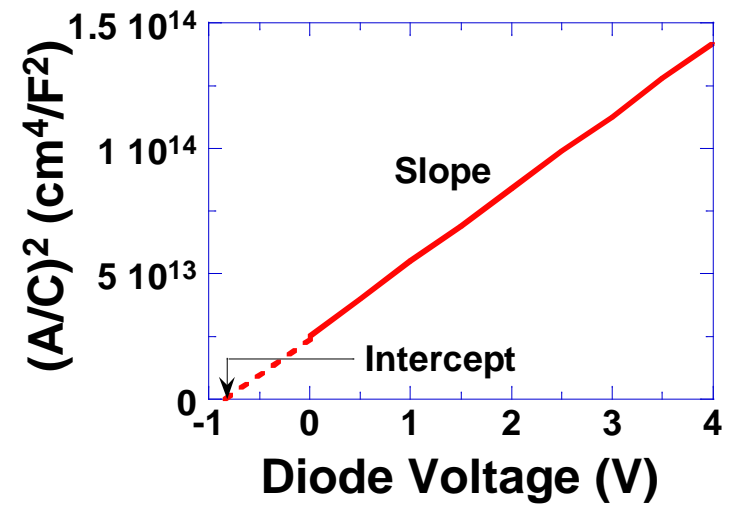
- Slope  $\Rightarrow N_D$

$$Slope = \frac{-2}{qK_s\epsilon_0 N_D}$$

- Intercept  $\Rightarrow \phi_B$

$$\phi_B = V_{bi} + V_o$$

$$V_o = E_G/q - E_i/q - \phi_F$$





# Review Questions

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- Why is the  $I$ - $V$  curve a straight line on a semilog plot?
- Why does a Si diode  $\log I - V$  curve have two slopes?
- How does series resistance affect the diode current?
- How is the barrier height of Schottky diodes determined?
- Why can the Schottky diode barrier heights be different when determined from  $I$ - $V$  or  $C$ - $V$  data?