

1. a) poles: $-3, 2$ unstable

b) poles: $-3, -2$ stable

c) poles: $-3, 2 \pm 3j$ unstable

d)

s^4	1	1	4
s^3	3	2	0
s^2	$\frac{1}{3}$	4	
s^1	-34		
s^0	4		

\rightarrow unstable

e)
$$H(s) = \frac{8s^2 + 2s - 7}{s(s^4 + 2s^3 - 2s^2 + 3s + 2)}$$

pole at $s=0 \Rightarrow$ not stable

use Routh test on $s^4 + 2s^3 - 2s^2 + 3s + 2$

to see if any poles are unstable

s^4	1	-2	2
s^3	2	3	
s^2	$-\frac{7}{2}$	2	
s^1	$\frac{29}{4}$		
s^0	2		

\rightarrow unstable

$$2. a) H(s) = \frac{10s+2}{s^3+3s^2+4s+k}$$

$$\begin{array}{l|ll} s^3 & 1 & 4 \\ s^2 & 3 & k \\ s^1 & \frac{12-k}{3} & 0 \\ s^0 & k & \end{array}$$

$$0 < k < 12$$

$$b) H(s) = \frac{10}{s^2 + (2+k)s + 4}$$

$$\begin{array}{l|ll} s^2 & 1 & 4 \\ s^1 & 2+k & 0 \\ s^0 & 4 & \end{array}$$

$$-2 < k$$

$$c) H(s) = \frac{k(s-1)}{s^2 + (2+k)s + 2-k}$$

$$\begin{array}{l|ll} s^2 & 1 & 2-k \\ s^1 & 2+k & \\ s^0 & 2-k & \end{array}$$

$$-2 < k < 2$$