

Bring this homework to class on Tuesday Sept. 11, but do not turn it in until the end of class.

#1. Using DeMorgan's Theorem, express the function as indicated.

$$F(A,B,C) = AC' + A'C' + BC'$$

a. With only OR and Complement operations:  $F(A,B,C) = (A'+C)' + (A+C)' + (B'+C)'$

$$F(A,B,C) = ((AC')' (A'C')')' + BC'$$

b. With only AND and Complement operations:  $F(A,B,C) = ((AC')' (A'C')' (BC')')$

#2. In order to design a single stage logic circuit, we need to express the logic function so that only single literals are complemented [ no complemented parentheses like  $(A+B)'$  ]. Express the following logic functions that way (use DeMorgan's theorem):

$$(A' + B)'C + ((D + E')F)' = AB'C + (D+E')' + F' = \underline{AB'C + D'E + F'}$$

$$(AB(C + D))' = (AB)' + C + D = \underline{A' + B' + C + D}$$

$$(((A'B)'C)'D)' = (A'B)'C + D' = \underline{A + B' + C' + D'}$$

#3. For the truth tables below, express the minterm sum of products, and the maxterm product of sums:

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

sum of products  $F(A,B,C) = A'B'C + A'BC + AB'C' + ABC' = m1 + m3 + m4 + m6$

product of sums  $F(A,B,C) = (A+B+C) (A+B'+C) (A'+B+C') (A'+B'+C') = M0 M2 M5 M7$

#3. For the truth tables below, fill in the Karnaugh map

A	B	C	F
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

A \ BC	00	01	11	10
0	0	1	1	0
1	1	0	0	1

minterm indices 1, 3, 4, 6 [ for all 1's, index = 4A + 2B + C ]

maxterm indices 0, 2, 5, 7 [ for all 0's, index = 4A + 2B + C ]

#4. For the Karnaugh map below, circle the Prime Implicants and label the Essential Prime Implicants with "EPI".

		EPI = B'D'				
AB \ CD	00	01	11	10		
00	1	0	1	1	EPI = A'C'	
01	0	1	1	1		
11	0	1	0	0		
10	1	1	0	1		

EPI = BC'D

Write the reduced logic expression: B'D' + A'C' + BC'D + AB'C' [ AC'D could replace AB'C' ]

maxterm indices (decimal) 1, 4, 11, 12, 14, 15

#5. Express the following as a sum of products (minterms) and as a product of sums(maxterms).

$$F(A,B,C) = (AB' + BC) (AC + AB'C)$$

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$$= AB'AC + AB'AB'C + BCAC + BCAB'C$$

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$$= AB'C + AB'C + ABC + 0$$

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SOP:  $= AB'C + ABC$

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$$= m_5 + m_7 \quad [ 101, 111 ]$$

$$F(A,B,C) = (AB' + BC) (AC + AB'C)$$

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$$= (AB' + B) (AB' + C) (AC + AB') (AC + C) \qquad (AB' + B) = (A + B)$$

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$$= (A + B) (A + C) (B' + C) A (C + B') C \qquad (AC + C) = C$$

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$$= (A + B) (A + C) (B' + C) (C + B') A C \qquad (A + B) = (A+B+C)(A+B+C')$$

$$A = (A+B+C) (A+B+C') (A+B'+C) (A+B'+C')$$

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$$= (A+B+C)(A+B+C') (A+B+C) (A+B'+C) (A+B'+C) (A'+B'+C)$$

$$(A+B+C) (A+B+C') (A+B'+C) (A+B'+C') (A+B+C) (A+B'+C) (A'+B+C) (A'+B'+C)$$

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POS  $= (A+B+C) (A+B+C') (A+B'+C) (A+B'+C') (A'+B+C) (A'+B'+C)$

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$$= M_0 M_1 M_2 M_3 M_4 M_6$$