

#1. Write the following numbers as binary fractions with 4 fractional bits (0.0001 precision)

- a. 29.3 11101.0100 29 (rt. to left): (1), /2 = 14 (0), /2 = 7 (1), /2 = 3 (1), /2 = 1 (1) (odd->"1")
 0.3 (left to rt.) x2 = 0.6 (0), x2 = 1.2 (1), 0.2 x2 = 0.4 (0), x2 = 0.8 (0)
 b. 0.1223 0.0001 (left to rt.) x2 = 0.2446 (0), x2 = 0.4892 (0), x2 = 0.9784 (0), x2 = 1.9568 (1)

#2. Write the missing unsigned integer numbers in binary, hex, and decimal representations.

| Decimal | Hex | Binary |
|--|---------------------------------|---|
| 299 $299/256 = 1$, $43/16 = 2$, 11 | 12B 299/256 = 1, 43/16=2, 11 | 1 0010 1011 1 2 B(11) from hex |
| $\frac{107}{6 \times 16 + 11}$ | 6B | 0110 1011 4+2 8+2+1 |
| $\frac{173}{10 \times 16 + 13}$ | AD 10,11,12,13 -> A,B,C,D | 1010 1101 8+2=10 8+4+1=13 -> AD |
| 131 $131/16 = 8$, r = 3 | 0x 83 131/16 = 8, r = 3 | 0100 0011 8 2+1=3 |
| $\frac{165}{10 \times 16 + 5}$ | A5 | 1010 0101 (from hex) |
| 99 $6 \times 16 + 3$ | 0x 63 0101 0011 = 63 hex | 01010011 |

#3. a. Express or decode the following binary floating point numbers. The fraction part (mantissa) should be normalized to five-bit accuracy (to 0.1xxxx where only the four bits xxxx are stored in memory, but show all here). The exponent should be a 5-bit number in 2's-compliment representation.

| Decimal Number | Sign Bit | Mantissa (fraction) | Exponent |
|---|-----------------|---|--|
| 2.125 $= 4 \times 0.503125$ | 0 + | 0.10001 $= 0.503125$ | 00010 $= 2, 2^2 = 4$ |
| 56 $= 11100$ | 0 "+" | 0.11100 11100. shift +5 = 0.11100 | 00101 (5) |
| -0.0003203 0.656×2^{-11} (or /2048) | 1 "-" | 0.10101 $0.5 + 0.125 + 0.031 = 0.656$ | 10101 "- (01010+1)=01011=-11 |
| -0.0398 0.000010100011 | 1 "-" | 0.10100 shift ". " right 4 -(00100) | 11100 $-4 = "-" : (~00100+1) = 11100$ |

$0.0398 \times 2 = 0.0796$ (0), $x2 = 0.1592$ (0), $x2 = 0.3184$ (0), $x2 = 0.6368$ (0), $x2 = 1.2736$ (1),
 $x2 = 0.5472$ (0), $x2 = 1.0944$ (1), $x2 = 0.1888$ (0), $x2 = 0.3776$ (0), $x2 = 0.7552$ (0), $x2 = 1.5104$ (1) ,,, (1)

b. How many bits of memory are required to store floating point numbers in this form? $1+(5-1)+5 = 10$

c. What is the precision to which a number can be stored (accuracy in %) ? 5 bits - $1/2^5 = 3$ %

Extra info: The range of absolute values is 0.5×2^{-16} to -0.98×2^{15} (how is zero stored?).

#4. Show how you would do the following calculations using 2's complement 10-bit binary numbers when A = 98 and B=205. Show the operations in binary, and the results in binary and decimal

| | Binary | Decimal |
|-------------|---|---|
| A | hex 98/16=6, 2 0x62 (leading zero is sign bit) _____ 0 0110 0010 _____ | 98 |
| B | hex 205/16 = 12(C), 13 (D) 0xCD _____ 0 1100 1101 _____ | 205 |
| -A | 1 1001 1101 (flip bits) + 0 0000 0001 (add 1) _____ 1 1001 1110 _____ | -98 |
| -B | 1 0011 0010 (flip bits) + 0 0000 0001 (add 1) _____ 1 0011 0011 _____ | -205 |
| A - B | 0 0110 0010 +A 1 0011 0011 -B _____ 1 1001 0101 _____ | 1 -> "-", find magnitude by flip, +1 0 0110 1010 + 1 0 0110 1011 = 0x6B = 6x16+11 _____ -107 _____ |
| B - A | 0 1100 1101 +B 1 1001 1110 -A _____ 0 0110 1011 _____ | "0" -> "+", 0x6B = 107 _____ 107 _____ |
| (-A) + (-B) | sign extend to increase precision (sign bit repeated to new bits on left) 1111 1001 1110 -A 1111 0011 0011 -B _____ 1110 1101 0001 _____ | 1 -> "-", find magnitude by flip, +1 0001 0010 1110 + 1 0001 0010 1111 = 0x12F = 256 + 2*16 + 15 _____ -303 _____ |