

ECE3065
HW1
Due by Thursday, 24. January 2013

1. The amplitude of an FM Radio Wave is described by the function
$$Y(x,t) = 1.5\cos(2 \times 10^8 \pi t - 2/3 \pi x + \pi/3) e^{-0.0005x} \text{ (Volts)}$$
 - (a) What is the amplitude A , the period T , the frequency f , the wavelength λ , the reference phase ϕ_0 and the attenuation factor α ? The velocity of light in the air is $c=3 \times 10^8$ m/sec.
 - (b) What are the values of the propagation constant β and of the radial frequency ω ? Do not forget the units!
 - (c) What is the propagation direction and why?
 - (d) What will be the amplitude of the FM wave for $t=10^{-5}$ sec and $x=3$ km? Supposing that a Radio receiver can pick up FM waves with amplitude larger than 0.1V without deterioration of the quality of reception, could a radio placed at the above distance receive efficiently this FM wave at $t=10^{-5}$ sec?
2. A transmission line of length L connects a wireless communication antenna to a voltage source with frequency f . Assuming that the velocity of wave propagation is $c=3 \times 10^8$ m/sec, for which of the following situations it is reasonable to ignore the presence of the transmission line in the analysis of the circuit:
 - (a) $L=0.1$ m, $f=1$ GHz
 - (b) $L=1$ m, $f=1.8$ GHz
 - (c) $L=0.01$ m, $f=0.9$ GHz
 - (d) $L=5$ cm, $f=60$ GHz
3. A 50Ω lossless coaxial transmission line is terminated in an antenna with impedance $Z_L=(30-j60)\Omega$. The wavelength is 5 cm. Calculate:
 - (a) The reflection coefficient Γ at the load
 - (b) The Standing Wave ratio S on the line
 - (c) If the electrical length of the coaxial line is $L=0.35\lambda$, what is the input impedance?
 - (d) If under matched conditions, the transmitter can deliver 10 Watts to the load, how much power does it deliver to this antenna?
4. A 50W lossless line used in a Radar filter:
 - (a) has electrical length $L=\lambda/4$ and is terminated with a 60Ω resistive load. What is the reflection coefficient and the input impedance?
 - (b) has electrical length $L=\lambda/8$ and is terminated with an Open Circuit. What is the reflection coefficient and the input impedance? Does the Open Circuit behave as an inductor or as a capacitor and why?
 - (c) Has electrical length $L=\lambda/6$ and is terminated with a Short Circuit? What is the reflection coefficient and the input impedance? Does the Short Circuit behave as and inductor or as a capacitor and why?
5. A lossless 50Ω microstrip transmission line, that is used in a nanosensor is terminated in a short circuit. Find:
 - (a) The reflection coefficient Γ

- (b) The input impedance at a distance 2.3λ from the load
 - (c) The input admittance at a distance 2.3λ from the load
6. A lossless 50Ω coaxial transmission line is to be matched to a satellite parabolic antenna with $Z_L = (75 - j20)\Omega$ using an L,C matching network around the center frequency of 6GHz.
- (a) Calculate the TWO solutions and their respective bandwidth for $\Gamma_M = 0.05$.
 - (b) How would the matching circuit get modified if we used a different antenna with $Z_L = (25 - j20)\Omega$. Calculate the new TWO solutions and their respective bandwidth for $\Gamma_M = 0.05$.
7. A 100 MHz FM broadcast station uses a 300Ω transmission line between the transmitter and a tower-mounted half-wave dipole antenna with impedance equal to 73Ω . You are asked to match the antenna to the line.
- (a) Using a quarter-wave section, determine the electrical length and the characteristic impedance of the quarter-wave section.
 - (b) Determine the physical length of the quarter-wave section if it is made of polystyrene with $\epsilon_r = 2.56$.
 - (c) What is the bandwidth of the transformer for $\Gamma_M = 5\%$?
 - (d) Using a 3-stage binomial transformer, determine the characteristic impedance and the electrical length of each section
 - (e) What is the bandwidth of the binomial transformer for $\Gamma_M = 5\%$?