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## Single-Stage BJT Amplifier Clipping Levels

The clipping levels of a single-stage amplifier are caused by over driving the transistor so that it either saturates or cuts off. Ideally, an amplifier should be designed so that it exhibits symmetrical clipping. That is, the amplifier should be able to put out positive and negative peak levels that are equal to each. This may not be the case for pulse amplifiers where the input signal is either positive or negative, but not both. The clipping levels of the common-emitter and common-collector amplifiers are derived in the following. The analysis assumes that the ac coupling capacitors in the circuit can be replaced with dc batteries having the same dc voltages as the capacitors.

## The Common-Emitter Amplifier

Fig. 1 shows the circuit diagram of a single stage common-emitter amplifier with the input, output, and emitter coupling capacitors replaced with dc batteries. The battery voltages are equal to the voltages across the capacitors $C_{1}, C_{2}$, and $C_{E}$ that the batteries replace. By superposition, they are given by

$$
\begin{gathered}
V_{1}=\frac{V^{+} R_{2}+V^{-} R_{1}}{R_{1}+R_{2}}-I_{B} R_{1} \| R_{2} \\
V_{2}=V^{+}-I_{C} R_{C} \\
V_{3}=V^{-}+I_{E} R_{E}
\end{gathered}
$$



Figure 1: Common-emitter Amplifier.
The positive clipping level is calculated by assuming that the input voltage $v_{S}$ goes negative until the BJT cuts off, i.e. it becomes an open circuit. The equivalent circuit is shown in Fig. 2. Under these conditions, the positive peak output voltage is given by

$$
v_{O}^{+}=\left(V^{+}-V_{2}\right) \frac{R_{L}}{R_{C}+R_{L}}=I_{C} R_{C} \frac{R_{L}}{R_{C}+R_{L}}=I_{C} R_{C} \| R_{L}
$$



Figure 2: Circuit for calculating $v_{O}^{+}$.
The negative clipping level is calculated by assuming that the input voltage $v_{S}$ goes positive until the BJT saturates. In this case, the collector-emitter voltage becomes small, ideally zero. We denote the collector-emitter saturation voltage by $V_{\text {CEsat }}$. To calculate the negative peak output voltage, it will be assumed that the base current is small enough to be neglected at the point that the BJT saturates. The equivalent circuit is shown in Fig. 3. Looking to the left of $R_{L}$, the Norton equivalent circuit consists of a current $i_{N}$ and parallel resistance $R_{N}$. By superposition, these are given by

$$
\begin{gathered}
i_{N}=\frac{V^{+}}{R_{C}}+\frac{V^{-}}{R_{E}}+\frac{V_{3}}{R_{3}}+\frac{V_{C E s a t}}{R_{E} \| R_{3}}-\frac{V_{2}}{R_{N}} \\
=\frac{V^{+}}{R_{C}}+\frac{V^{-}}{R_{E}}+\frac{V^{-}+I_{E} R_{E}}{R_{3}}+\frac{V_{C E s a t}}{R_{E} \| R_{3}}-\frac{V^{+}-I_{C} R_{C}}{R_{N}} \\
R_{N}=R_{C}\left\|R_{E}\right\| R_{3}
\end{gathered}
$$

The negative clipping level is is given by

$$
\begin{aligned}
v_{O}^{-} & =i_{N} R_{N} \| R_{L} \\
& =\left(\frac{V^{+}}{R_{C}}+\frac{V^{-}}{R_{E}}+\frac{V^{-}+I_{E} R_{E}}{R_{3}}+\frac{V_{C E s a t}}{R_{E} \| R_{3}}-\frac{V^{+}-I_{C} R_{C}}{R_{N}}\right) R_{C}\left\|R_{E}\right\| R_{3} \| R_{L} \\
& =\left(\frac{-V^{+}+V^{-}+V_{C E s a t}}{R_{E} \| R_{3}}+\frac{I_{C} R_{E}}{\alpha R_{3}}+\frac{I_{C} R_{C}}{R_{C}\left\|R_{E}\right\| R_{3}}\right) R_{C}\left\|R_{E}\right\| R_{3} \| R_{L}
\end{aligned}
$$

where $I_{E}=I_{C} / \alpha$ has been used.
The condition for symmetrical clipping is $v_{O}^{+}=-v_{O}^{-}$. This condition leads to

$$
I_{C} R_{C}\left\|R_{L}=\left(\frac{V^{+}-V^{-}-V_{C E s a t}}{R_{E} \| R_{3}}-\frac{I_{C} R_{E}}{\alpha R_{3}}-\frac{I_{C} R_{C}}{R_{C}\left\|R_{E}\right\| R_{3}}\right) R_{C}\right\| R_{E}\left\|R_{3}\right\| R_{L}
$$

This can be solved for $I_{C}$ to obtain

$$
\begin{aligned}
I_{C} & =\frac{\frac{V^{+}-V^{-}-V_{C E s a t}}{R_{E} \| R_{3}}}{\frac{R_{C} \| R_{L}}{R_{C}\left\|R_{E}\right\| R_{3} \| R_{L}}+\frac{R_{E}}{\alpha R_{3}}+\frac{R_{C}}{R_{C}\left\|R_{E}\right\| R_{3}}} \\
& =\frac{V^{+}-V^{-}-V_{C E s a t}}{R_{E}\left\|R_{3}\left(2+\frac{R_{E}}{\alpha R_{3}}\right)+R_{C}\right\| R_{L}\left(2+\frac{R_{C}}{R_{L}}\right)}
\end{aligned}
$$



Figure 3: Circuit for calculating $v_{O}^{-}$.

When this condition is satisfied, the common-emitter amplifier will clip symmetrically on the positive and negative peaks.

Example 1 For the CE amplifier of Fig. 1, it is given that $R_{s}=5 \mathrm{k} \Omega, R_{1}=120 \mathrm{k} \Omega, R_{2}=100 \mathrm{k} \Omega$, $R_{C}=4.3 \mathrm{k} \Omega, R_{E}=5.6 \mathrm{k} \Omega, R_{3}=100 \Omega, R_{L}=20 \mathrm{k} \Omega, V^{+}=15 \mathrm{~V}, V^{-}=-15 \mathrm{~V}, V_{B E}=0.65 \mathrm{~V}$, $\beta=99, \alpha=0.99, r_{x}=20 \Omega, V_{A}=100 \mathrm{~V}, V_{\text {CEsat }}=0.2 \mathrm{~V}$ and $V_{T}=0.025 \mathrm{~V}$. Solve for the positive and negative output clipping voltages. Calculate the value of $I_{E}$ for symmetrical clipping. What are the resultant clipping levels?

Solution. For the dc bias solution, replace all capacitors with open circuits. The Thévenin voltage and resistance seen looking out of the base are

$$
V_{B B}=\frac{V^{+} R_{2}+V^{-} R_{1}}{R_{1}+R_{2}}=-1.364 \mathrm{~V} \quad R_{B B}=R_{1} \| R_{2}=54.55 \mathrm{k} \Omega
$$

The Thévenin voltage and resistance seen looking out of the emitter are $V_{E E}=V^{-}$and $R_{E E}=R_{E}$. The bias equation for $I_{E}$ is

$$
I_{E}=\frac{V_{B B}-V_{E E}-V_{B E}}{R_{B B} /(1+\beta)+R_{E E}}=2.113 \mathrm{~mA}
$$

The clipping voltages are given by

$$
\begin{gathered}
v_{O}^{+}=I_{C} R_{C} \| R_{L}=7.61 \mathrm{~V} \\
v_{O}^{-}=\left(\frac{-V^{+}+V^{-}+V_{C E s a t}}{R_{E} \| R_{3}}+\frac{I_{E} R_{E}}{R_{3}}+\frac{\alpha I_{E} R_{C}}{R_{C}\left\|R_{E}\right\| R_{3}}\right) R_{C}\left\|R_{E}\right\| R_{3} \| R_{L} \\
=-4.45 \mathrm{~V}
\end{gathered}
$$

The value of $I_{E}$ for symmetrical clipping is

$$
I_{E}=\frac{I_{C}}{\alpha}=\frac{1}{\alpha} \frac{V^{+}-V^{-}-V_{\text {CEsat }}}{R_{E}\left\|R_{3}\left(2+\frac{R_{E}}{\alpha R_{3}}\right)+R_{C}\right\| R_{L}\left(2+\frac{R_{C}}{R_{L}}\right)}=2.30 \mathrm{~mA}
$$

To achieve this, either $R_{1}, R_{2}$, or both could be adjusted. The change in bias current would also change the small-signal gain. The new clipping levels are

$$
v_{O}^{+}=-v_{O}^{-}=I_{C} R_{C} \| R_{L}=6.86 \mathrm{~V}
$$

## The Common-Collector Amplifier

Fig. 4 shows the circuit diagram of a single stage common-emitter amplifier with the input, output, and emitter coupling capacitors replaced with dc batteries. The battery voltages are equal to the voltages across the capacitors $C_{1}, C_{2}$, and $C_{E}$ that the batteries replace. By superposition, they are given by

$$
\begin{gathered}
V_{1}=\frac{V^{+} R_{2}+V^{-} R_{1}}{R_{1}+R_{2}}-I_{B} R_{1} \| R_{2} \\
V_{2}=V^{-}+I_{E} R_{E}
\end{gathered}
$$



Figure 4: Common-collector amplifier.
The positive clipping level is calculated by assuming that the input voltage $v_{S}$ goes positive until the BJT saturates. In this case, the collector-emitter voltage becomes small, ideally zero. We denote the collector-emitter saturation voltage by $V_{\text {CEsat }}$. To calculate the positive peak output voltage, it will be assumed that the base current is small enough to be neglected at the point that the BJT saturates. The equivalent circuit is shown in Fig. 5. The output voltage is given by

$$
v_{O}^{+}=V^{+}-V_{C E s a t}-V_{2}=V^{+}-V_{C E s a t}-\left(V^{-}+I_{E} R_{E}\right)
$$

The negative clipping level is calculated by assuming that the input voltage $v_{S}$ goes negative until the BJT cuts off, i.e. it becomes an open circuit. The equivalent circuit is shown in Fig. 6. Under these conditions, the negative peak output voltage is given by

$$
v_{O}^{-}=\left(V^{-}-V_{2}\right) \frac{R_{L}}{R_{E}+R_{L}}=\left[V^{-}-\left(V^{-}+I_{E} R_{E}\right)\right] \frac{R_{L}}{R_{E}+R_{L}}=-I_{E} R_{E} \| R_{L}
$$

The condition for symmetrical clipping is $v_{O}^{+}=-v_{O}^{-}$. This condition leads to the condition

$$
\left[V^{+}-V_{C E s a t}-\left(V^{-}+I_{E} R_{E}\right)\right] \frac{R_{L}}{R_{E}+R_{L}}=I_{E} R_{E} \| R_{L}
$$



Figure 5: Circuit for calculating $v_{O}^{+}$.


Figure 6: Circuit for calculating $v_{O}^{-}$.

This can be solved for the required dc bias voltage $V_{X}$ across the emitter resistor $R_{E}$ to obtain

$$
V_{X}=I_{E} R_{E}=\frac{1}{2}\left(V^{+}-V_{C E s a t}-V^{-}\right)
$$

Note that this is not a function of $R_{L}$.
Let the symmetrical clipping voltage be denoted by $v_{C L}$. From the equation for $v_{O}^{-}$, it is given by

$$
v_{C L}=-v_{O}^{-}=I_{E} R_{E} \| R_{L}=I_{E} \frac{R_{E} R_{L}}{R_{E}+R_{L}}=V_{X} \frac{R_{L}}{R_{E}+R_{L}}
$$

This equation can be solved for $R_{E}$ to obtain

$$
R_{E}=\left(\frac{V_{X}}{v_{C L}}-1\right) R_{L}=\left(\frac{V^{+}-V_{C E s a t}-V^{-}}{2 v_{C L}}-1\right) R_{L}
$$

It follows that $I_{E}$ is given by

$$
I_{E}=\frac{V_{X}}{R_{E}}=\frac{V^{+}-V_{C E s a t}-V^{-}}{2 R_{E}}
$$

Example 2 For the CC amplifier in Fig. 1, it is given that $R_{S}=5 \mathrm{k} \Omega, R_{1}=120 \mathrm{k} \Omega, R_{2}=100 \mathrm{k} \Omega$, $R_{E}=5.6 \mathrm{k} \Omega, R_{L}=20 \mathrm{k} \Omega, V^{+}=15 \mathrm{~V}, V^{-}=-15 \mathrm{~V}, V_{B E}=0.65 \mathrm{~V}, \beta=99, \alpha=0.99, r_{x}=20 \Omega$, $V_{A}=100 \mathrm{~V}$ and $V_{T}=0.025 \mathrm{~V}$. Solve for $v_{O}^{+}$and $v_{O}^{-}$.

Solution. Because the dc bias circuits are the same as for the common-emitter amplifier example, the bias values are the same. It follows that the clipping levels are given by

$$
\begin{gathered}
v_{O}^{+}=V^{+}-V_{C E s a t}-\left(V^{-}+I_{E} R_{E}\right)=14.04 \mathrm{~V} \\
v_{O}^{-}=-I_{E} R_{E} \| R_{L}=-9.25 \mathrm{~V}
\end{gathered}
$$

The value of $I_{E}$ for symmetrical clipping is

$$
I_{E}=\frac{V^{+}-V_{C E s a t}-V^{-}}{2 R_{E}}=2.66 \mathrm{~mA}
$$

To achieve this, either $R_{1}, R_{2}$, or both could be adjusted. The change in bias current would also change the small-signal gain. The new clipping levels are

$$
v_{O}^{+}=-v_{O}^{-}=I_{E} R_{E} \| R_{L}=11.6 \mathrm{~V}
$$

Example 3 The CC amplifier of Example 2 is required to clip symmetrically at the level $v_{C L}=8 \mathrm{~V}$ with the new load resistance $R_{L}=3 \mathrm{k} \Omega$. Calculate the required values of $R_{E}$ and $I_{E}$. If $R_{2}$ is held constant at the value $R_{2}=100 \mathrm{k} \Omega$, calculate the new value of $R_{1}$ to bias the transistor at the new current.

Solution. The required voltage across $R_{E}$ is $V_{X}=\left(V^{+}-V_{\text {CEsat }}-V^{-}\right) / 2=14.9 \mathrm{~V}$. It follows that the new values for $R_{E}$ and $I_{E}$ are

$$
\begin{gathered}
R_{E}=\left(\frac{V_{X}}{v_{C L}}-1\right) R_{L}=\left(\frac{14.9}{5}-1\right) 3000=2.59 \mathrm{k} \Omega \\
I_{E}=\frac{V_{X}}{R_{E}}=5.76 \mathrm{~mA}
\end{gathered}
$$

The new value of $R_{1}$ must satisfy

$$
\left(\frac{V^{+}}{R_{1}}+\frac{V^{-}}{R_{2}}-\frac{I_{E}}{1+\beta}\right) R_{1} \| R_{2}=V^{-}+V_{X}+V_{B E}
$$

This can be solved for $R_{1}$ to obtain $R_{1}=67.8 \mathrm{k} \Omega$.

