

# RHEED & Its Role in MBE Systems

**Shalabh Goyal**  
**School OF ECE**  
**Georgia Tech.**

# Outline

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- Molecular Beam Epitaxy Systems
- Importance of RHEED in MBE Systems
- Physics involved
- Conclusions

# Molecular Beam Epitaxy

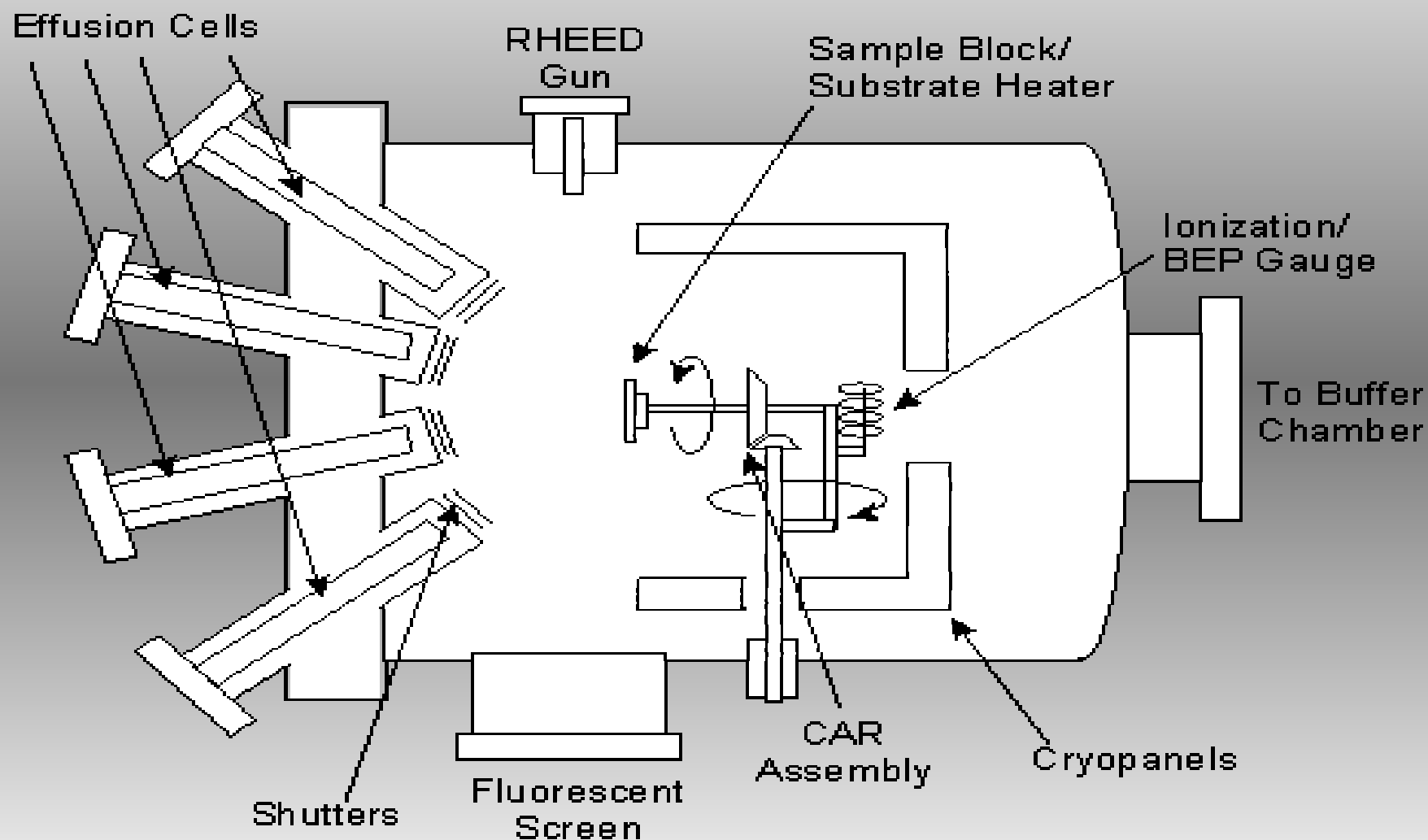
- Technique to grow high-quality layers with very abrupt interfaces
- Done in UHV environment
- Beams of atoms or molecules directed on to the heated wafer
- Now high throughput production systems possible for MBE

# Advantages

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- Very precise control of layer thickness
- NO complicated reactions involved at the substrate surface
- Processes like RHEED can be used for surface characterization due to UHV environment
- Toxic chemicals contained in vacuum chamber

# MBE System



# RHEED

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- Beam of energetic electrons strikes the surface at grazing angles
- For surface characterization
- Gives the crystal growth rate
- Strong interaction with the crystal surface
- In-situ Compatibility
- High Surface Sensitivity

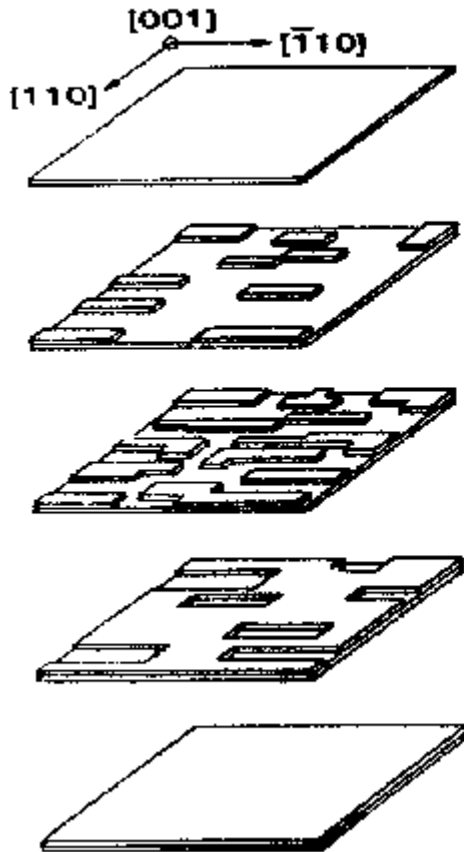
## Used in MBE for

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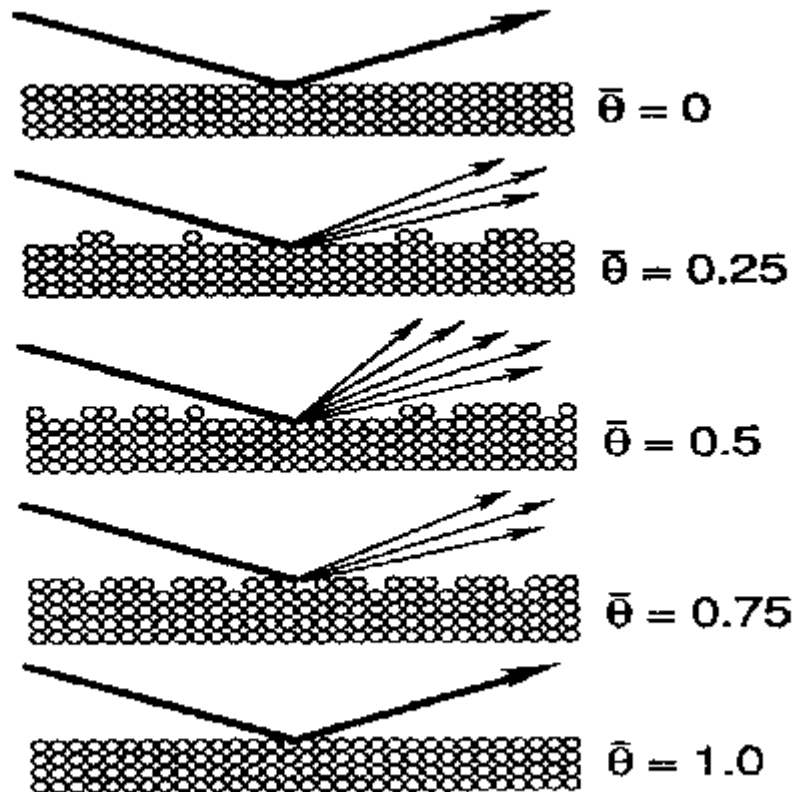
- Measuring Growth rate
- Observing removal of Oxides
- Monitoring arrangement of surface atoms

# Crystal growth rate by RHEED

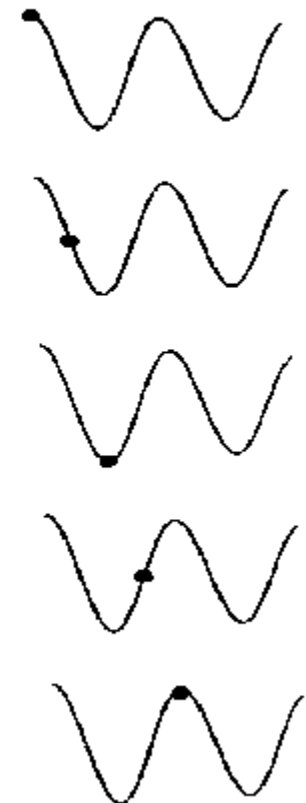
MONOLAYER GROWTH



ELECTRON BEAM



RHEED SIGNAL





# PHYSICS Aspect (Kinematic Theory)

- The interaction of electron with crystal potential is governed by Schrodinger EQ.

$$\frac{-\hbar^2}{8\pi^2 m_e} \nabla^2 \Psi(\mathbf{r}) - |e| V(\mathbf{r}) \Psi(\mathbf{r}) = \frac{\hbar^2 |\mathbf{k}_0|^2}{8\pi^2 m_e} \Psi(\mathbf{r}). \quad (1)$$

- We expand the crystal potential in Fourier components using reciprocal lattice vectors as  $(U_{\mathbf{g}} = 2m_e |e| V_{\mathbf{g}} / \hbar^2)$

$$U(\mathbf{r}) = \sum_{\mathbf{g}} U_{\mathbf{g}} \exp(i\mathbf{g} \cdot \mathbf{r}), \quad (2)$$

- Now the outgoing wave function is

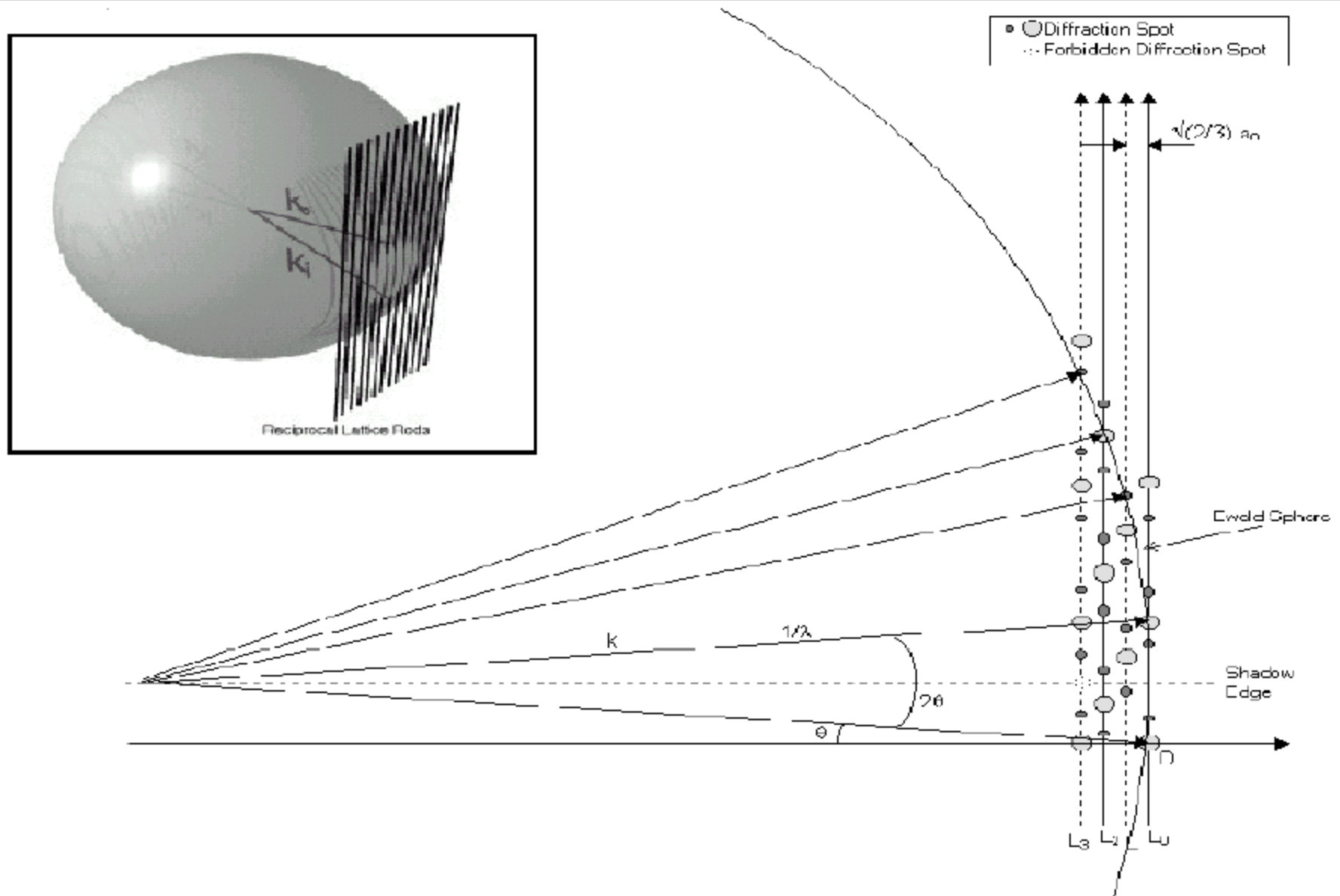
$$\Psi(\mathbf{r}) = \sum_i c_i \exp(i\mathbf{k}_i \cdot \mathbf{r}), \quad (3)$$

- According to perturbation theory

$$c_i = \frac{im_e}{\hbar^2 K_o} \int \sum_{\mathbf{g}} U_{\mathbf{g}} \exp(i(\mathbf{g} - \mathbf{k}_i + \mathbf{k}_0) \cdot \mathbf{r}) d\mathbf{r}, \quad (4)$$

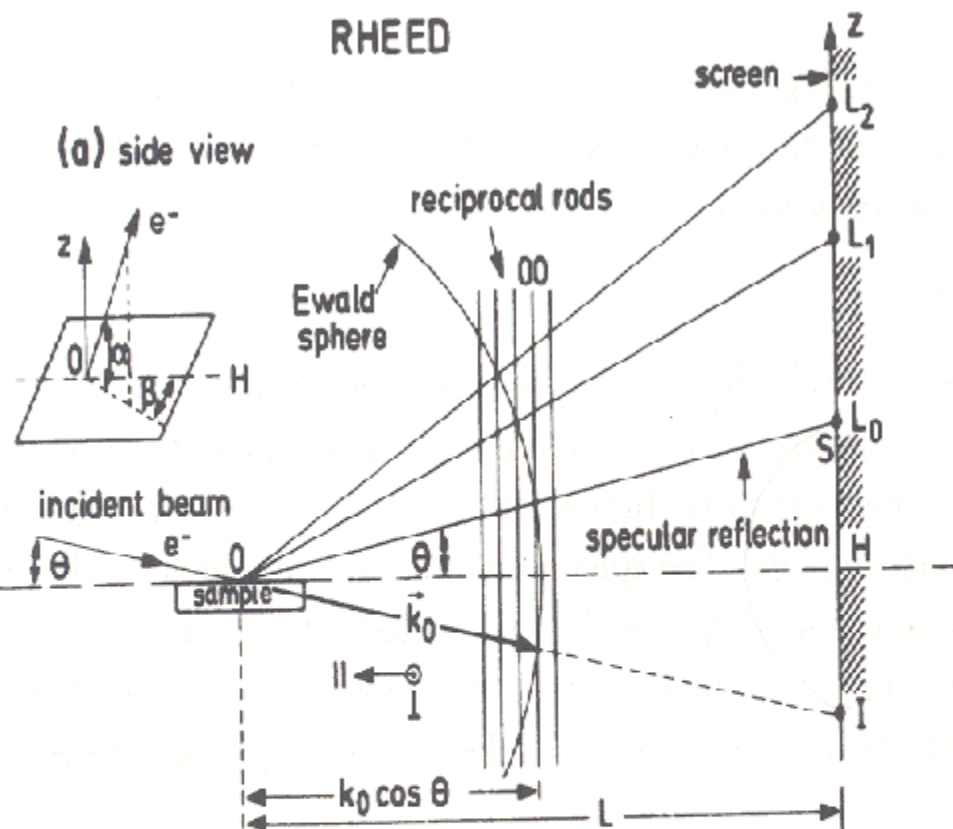
- $C_i$ s are proportional to  $U_{\mathbf{g}} \delta(\mathbf{k}_0 - \mathbf{k}_i + \mathbf{g})$  so the Laue diffraction condition is given by  $\mathbf{k}_i - \mathbf{k}_0 = \mathbf{g}$ .

- For a finite sized crystal reciprocal lattice points elongates to form the rod like structures

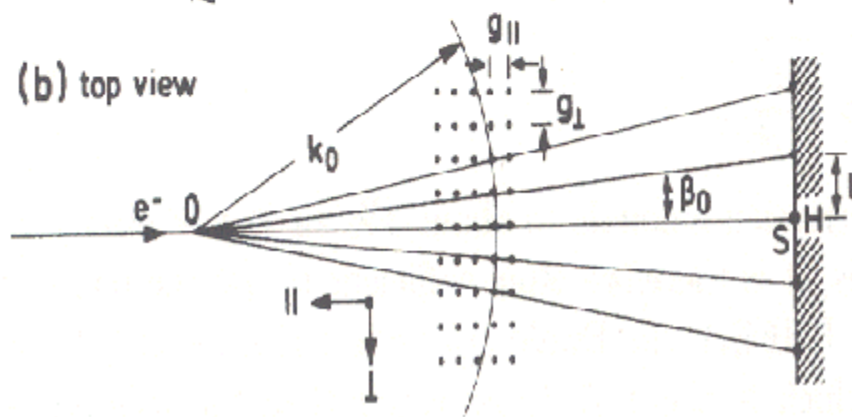


# RHEED

(a) side view

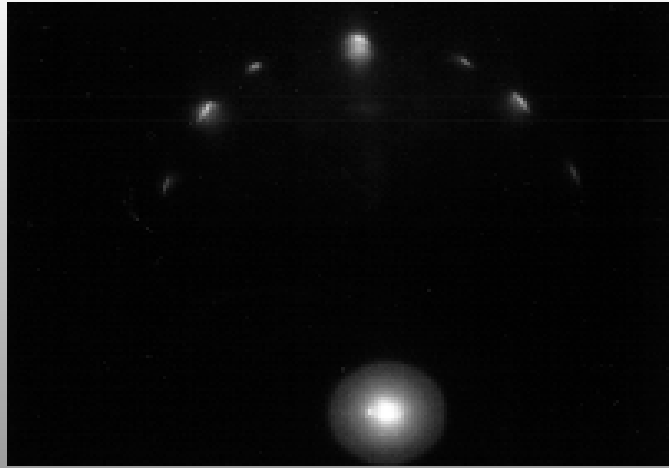


(b) top view

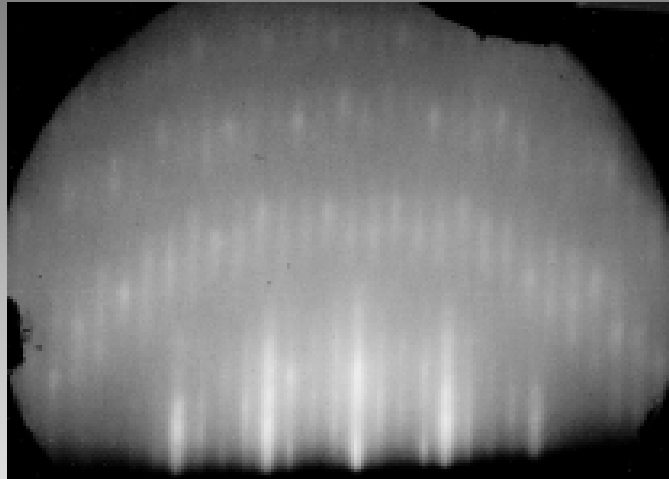


$$ng_{\parallel} = k_0 \left[ \cos \theta - \frac{1}{\sqrt{(L_n/L)^2 + 1}} \right],$$

$$ng_{\perp} = \frac{k_0}{\sqrt{(L/nl)^2 + 1}},$$

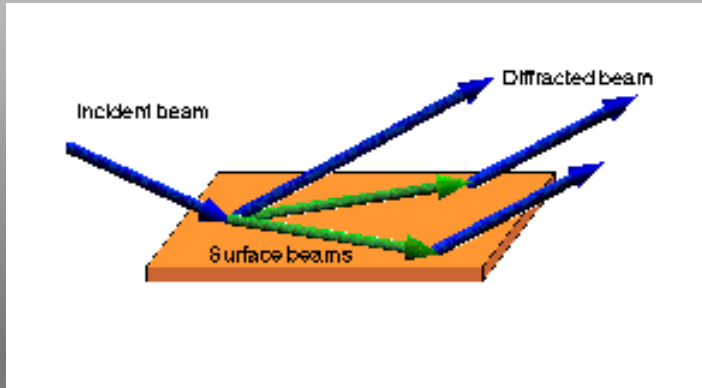


Well Annealed  
Sapphire Surface

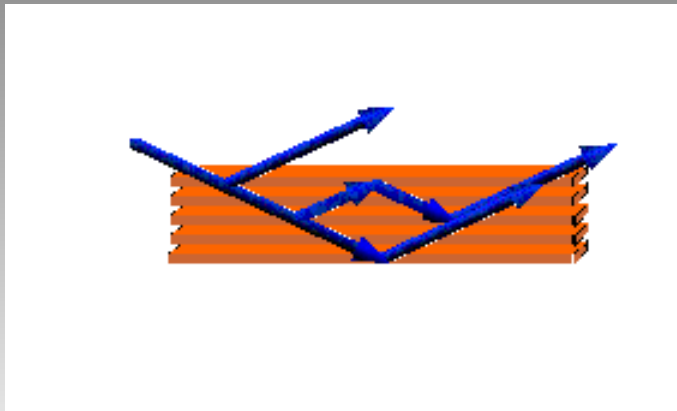


Two Laue circles  
with Streaks

# Surface Resonance & Kikuchi Lines



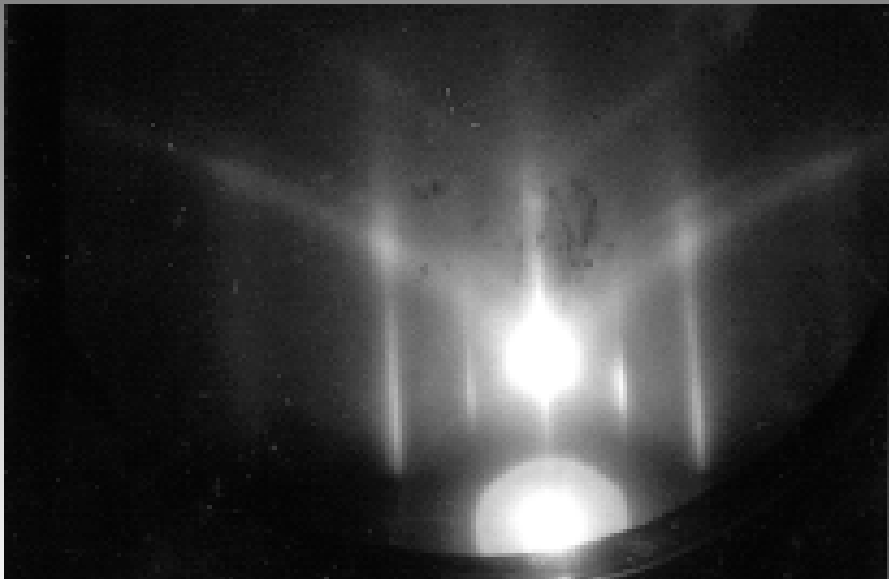
Surface Resonance



Bragg's Diffraction Planes

# Surface resonance and kikuchi lines

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# Conclusions

- RHEED in principle can give substantial information about crystal surface
- Kinematic theory gives little error in predicting the position of diffraction spots
- Kinematic theory does not take into account surface resonance and inelastic collisions
- The exact measure of intensities cannot be done by kinematic theory
- In MBE systems it is used to have qualitative measure of surface perfection