

3.1(c)

$$Q(s)Q(-s) = s^4 + 1.75s^2 + 4$$

$$s^2 = \frac{-1.75 \pm j3.5969}{2} = -0.875 \pm j1.7984$$

$$= 2 \angle 115.94$$

$$s = 1.414 \angle 57.97^\circ = 0.75 + j1.19896$$

$$Q = (s + 0.75 + j1.19896)(s + 0.75 - j1.19896)$$

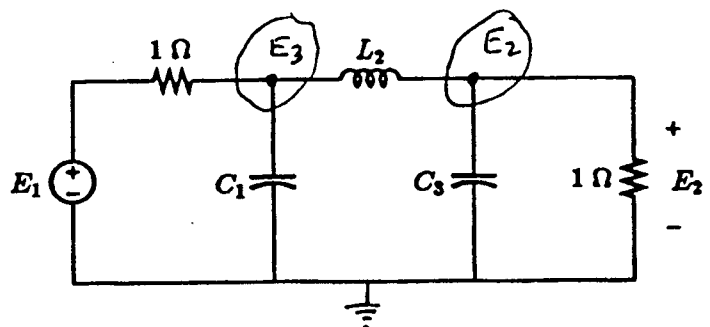
$$= s^2 + 1.5s + 2$$

$$H(s) = \frac{s+2}{s^2+1.5s+2}$$

3.5 Node equations are

$$\frac{E_3 - E_1}{1} + sC_1 E_3 + \frac{E_3 - E_2}{sL_2} = 0$$

$$\frac{E_2 - E_3}{sL_2} + sC_3 E_2 + E_2 = 0$$



Solving we get

$$\frac{E_2}{E_1} = \frac{\frac{1}{2}}{\frac{C_1 L_2 C_3}{2} s^3 + \frac{C_1 L_2 + L_2 C_3}{2} s^2 + \frac{C_1 + L_2 + C_3}{2} s + 1}$$

Hence  $K = \frac{1}{2}$ . Set  $\frac{C_1 L_2 C_3}{2} = 1$ ,  $\frac{C_1 L_2 + L_2 C_3}{2} = 2$ ,  $\frac{C_1 + L_2 + C_3}{2} = 2$

Solving gives  $C_1 = 1$ ,  $C_3 = 1$ ,  $L_2 = 2$ .

$$3.6 \quad 10 \log(1 + \epsilon^2) = 0.4 \quad \epsilon = 0.310609$$

$$v = \frac{1}{3} \sinh^{-1}\left(\frac{1}{\epsilon}\right) = 0.628552$$

$$\sinh v = 0.670766 \quad \cosh v = 1.204129$$

$$s_{1,2} = \sin \frac{2\pi}{6} \sinh v \pm j \cos \frac{2\pi}{6} \cosh v$$

$$= -0.335383 \pm j 1.042806$$

$$s_3 = -\sinh v = -0.670766$$

$$H(s) = \frac{K}{(s + 0.335383 \pm j 0.1042806)(s + 0.670766)}$$

$$= \frac{K}{(s^2 + 0.670766s + 1.19993)(s + 0.670766)}$$

$$= \frac{K}{s^3 + 1.341531s^2 + 1.649853s + 0.804869}$$

$$K = 0.804869$$

3.11

$$H(s) = \frac{K (s^2 + \frac{1}{\omega_1^2})(s^2 + \frac{1}{\omega_2^2}) \cdots (s^2 + \frac{1}{\omega_N^2})}{s^{2N} + b_{2N-1}s^{2N-1} + \cdots + b_1s + b_0}$$

$$H^2(\omega) = K^2 = \frac{1}{1 + \frac{\epsilon^2}{\omega_1^4 \omega_2^4 \cdots \omega_N^4}}, \quad K = \frac{\omega_1^2 \omega_2^2 \cdots \omega_N^2}{\sqrt{\epsilon^2 + \omega_1^4 \omega_2^4 \cdots \omega_N^4}}$$

$$H^2(0) = \left( \frac{K}{b_0 \omega_1^2 \omega_2^2 \cdots \omega_N^2} \right)^2 = \frac{1}{1 + \epsilon^2 \omega_1^4 \omega_2^4 \cdots \omega_N^4}$$

$$b_0 = \frac{K \sqrt{1 + \epsilon^2 \omega_1^4 \omega_2^4 \cdots \omega_N^4}}{\omega_1^2 \omega_2^2 \cdots \omega_N^2}$$