

# An Adaptive Scheme of Sharing Compressed Flow Information Among Networked Underwater Gliders

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**Abstract**—Underwater glider fleets are often used cooperatively for large-scale ocean observation. A key requirement for underwater glider operation is to reduce the amount of information that needs to be shared among gliders over communication links. This paper presents a method to estimate the quality of communication link between underwater gliders sharing their information. The representation of high flow region that gliders should notice is compressed using the support vector data description (SVDD) method. The ratio of compression of SVDD is optimized to match the link quality and SVDD error estimation. The compressed data is then communicated among gliders for a distributed path planning algorithm. We show that such an adaptive compression method can provide desired accuracy.

## I. INTRODUCTION

Underwater gliders play important roles in ocean sampling [1] due to its long-endurance, low-cost and reusability. Gliders travel at relatively low speed comparing to the speed of ocean current. Gliders should also avoid to surface in areas with heavy ship traffic. These requirements post challenges for path planning algorithms.

For large scale environmental monitoring, it is often preferred to use a fleet of gliders that cooperate with each other to increase the quality of data collected [2]. Cooperative path planning, however, remains a novel research direction for marine robots. Our previous work [3] proposed a distributed approach for cooperative path planning using a reduced amount of information. The reduction, which was achieved by a method based on the support vector data description (SVDD) [4], extracts boundaries of flow regions with high speed that gliders should avoid. The reduced information is then communicated among neighboring gliders. In reality, the underwater acoustic communication link or the satellite communication link, the two major communication methods used by gliders are subject to time-varying disturbances. The reduced information may not be able to be reliably transmitted. In this work, we consider the changing link quality of the communication channel and adjust the ratio of reduction according to both the link quality and the fidelity of representation.

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This work is supported by the National Natural Science Foundation of China (Grant No. 61233013) and the State Key Laboratory of Robotics at Shenyang Institute of Automation (Grant No. 2014-Z02).

Link quality estimation plays a key role in wireless sensor networks. It has an overall impact on the network performance and also affects the design of higher level protocols [5]. Quality of service (QoS) represents the overall performance of a communication network seen by the users of the network, hence are directly related to networked robotics [6]. Underwater networking reprints a fast growing area that is developed from underwater communication. An effective protocol to transmit data packets underwater is called Stop and Wait (S&W), which is a type of Automatic Repeat reQuest (ARQ) scheme. The transmitter sends a packet and then waits for a response, called an acknowledgement, from the receiver. If this acknowledgement does not arrive within a predefined time, or a negative acknowledgement arrives, a packet will be retransmitted. The efficiency of the conventional protocol can be improved by transmitting a group of packets [7], and the optimal packet size can be determined as a function of QoS that is related to range and bit rate.

In this paper, we first propose a QoS estimation method for the communication links used by underwater gliders. Then, we improve the data compression scheme in [3] to incorporate the estimated QoS. The compression ratio is determined by solving an optimization problem that is constrained by the estimated QoS. The compressed data is then shared among the gliders for distributed path planning. Our method enables the gliders to adaptively adjust the compression ratio to match the QoS of communication links. This allows us to investigate the quality of path planning under the influence of unreliable communication.

The paper is organized as follows. In section II, we briefly review the problem of distributed path planning and the need to find a compressed representation of flow field. In section III, we set up the problem for this paper. The adaptive compression scheme is proposed in section IV. Section V demonstrates the simulation results of distributed path planning and section VI provides conclusion and discussion.

## II. BACKGROUND INFORMATION

We consider a team of  $K$  gliders  $G_1, G_2, \dots, G_K$  deployed into the ocean at different locations and need to coordinate their paths for certain task. For this paper we focus on planning

the planar trajectories for the gliders. We assume that each glider has knowledge about the depth-averaged flow within a small patch around itself. We can discretize the patch into  $m \times n$  grid points indexed by  $(i, j)$ . Consequently, the depth-averaged flow velocities in this patch can be represented by two  $m \times n$  matrices  $\mathbf{U} = \{u_{ij}\}_{m,n}$  and  $\mathbf{V} = \{v_{ij}\}_{m,n}$ , where  $u_{ij}$  denotes flow speed in the east/west direction at gridpoint  $(i, j)$  and  $v_{ij}$  denotes flow speed in north/south direction at grid point  $(i, j)$ . A local flow map can then be represented as  $\mathbf{F} = [\mathbf{U}(x, y), \mathbf{V}(x, y)]$  in this patch.

We consider glider  $G_1$  planing a path from its starting position  $\mathbf{r}_b$  to a destination  $\mathbf{r}_d$ , as illustrated by Fig. 1.  $G_1$  has its local flow map,  $\mathbf{F}_1$ , shown in Fig. 1. In this

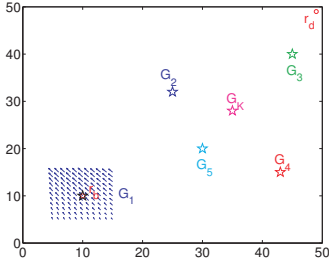


Fig. 1. Glider  $G_1$  only has local information in a small patch for planning a path from  $\mathbf{r}_b$  to  $\mathbf{r}_d$ .

local patch,  $\mathbf{F}_1$  is sufficient to plan an accurate path for  $G_1$ . However,  $G_1$  does not have information about the region out of this patch even though  $G_1$  has to avoid regions with strong currents against its desired motion outside its patch. This path planning problem can be solved by allowing gliders to share their knowledge about the flow over communication links. But transmitting all the depth averaged flow data within a glider patch over communication links is difficult and even unachievable. Therefore, the problems are to determine what information is necessary to be shared and how to reduce the amount of the information for cooperative path planning

The flow information can be reduced using support vector data description (SVDD) [4] to represent the boundaries of regions with high flow. The SVDD method produces representation of a dataset by searching for the smallest hypersphere that contains as many target points (grid points with strong flow) as possible but does not include outlier points (grid points with weak flow). Consider a set of training data  $\{\mathbf{x}_i, i = 1, 2, \dots, N\}$  that contain both target points and outlier points. SVDD finds Lagrangian multipliers  $\alpha_i^*$  that maximize

$$L = \sum_i \alpha_i (\mathbf{x}_i \cdot \mathbf{x}_i) - \sum_{i,j} \alpha_i \alpha_j (\mathbf{x}_i \cdot \mathbf{x}_j) \quad (1)$$

The optimization solutions will contain a large number of  $\alpha_i^*$  with 0 value. The target points  $\mathbf{x}_i$  with the corresponding  $\alpha_i^* > 0$  are called *support vectors*. In the 2D plane, the support vectors determine a circle that separates the target points from the outlier points, which can be viewed as a representation of the boundary of the regions of high flow.

The boundary of regions with strong flow usually has irregular shape. By replacing the inner product  $(\mathbf{x}_i \cdot \mathbf{x}_j)$  by a Gaussian kernel function  $K_G(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{\sigma^2})$  [4],

support vectors can be computed to maximize the Lagrangian

$$L = 1 - \sum_i \alpha_i^2 - \sum_{i \neq j} \alpha_i \alpha_j K_G(\mathbf{x}_i, \mathbf{x}_j) \quad (2)$$

Once a set of support vectors have been determined. They can be used to decide whether a grid point is inside or outside of the boundary. Let  $S$  be the set of support vectors. A test point  $\mathbf{z}$  is considered inside the boundary when the following inequality is satisfied

$$K_G(\mathbf{z}, \mathbf{z}) - 2 \sum_s \alpha_s^* K_G(\mathbf{z}, \mathbf{x}_s) + \sum_{s,k} \alpha_s^* \alpha_k^* K_G(\mathbf{x}_s, \mathbf{x}_k) \leq R^{*2} \quad (3)$$

where  $\mathbf{x}_s, \mathbf{x}_k \in S$ .

Let the boundary determined by  $G_1$  be  $\Omega_1$ . Then  $G_1$  will communicate all support vectors that represent  $\Omega_1$  to  $G_2$  for  $G_2$  to plan its path. The parameters that need to be transmitted by  $G_1$  to  $G_2$  include: the width of the Gaussian kernel  $\sigma$ , the set of support vectors  $S$ , and the corresponding value of the Lagrange multipliers. Then  $G_2$  will be able to judge whether one point  $\mathbf{z}$  is within  $\Omega_1$  or not by using the set of support vectors  $S$  and the corresponding Lagrange multipliers that represent  $\Omega_1$  as in equation (3).

The fidelity of SVDD is of great importance. There are two types of representation errors due to the reduction of information by SVDD. The first type is the **Target Rejection Error**, represented by  $e_1$ , indicates how many target points are rejected. The second type is the called **Outlier Acceptation Error**, represented by  $e_2$ , indicates how many outlier points are accepted. These errors can be adjusted by adjusting the width  $\sigma$  in the Gaussian kernel  $K_G$ . Our previous work [3] determines  $\sigma$  to minimize the following cost function

$$E = (e_1 + e_2) + \frac{N_{SV}}{N} \quad (4)$$

where  $N_{SV}$  is the total number of support vectors generated by the SVDD, and  $N$  is the total number of grid points.

### III. PROBLEM FORMULATION

We consider the situation when one glider, say  $G_2$  tries to determine a set of support vectors to be transmitted to glider  $G_1$ . If the communication link between  $G_1$  and  $G_2$  are unreliable, then the information may be corrupted during the transmission. But  $G_1$  may suppose that the information it received is correctly transmitted and reconstructs the high-flow regions in the blank zone based on these information. In the worst situation, corrupted information might lead  $G_1$  into dangerous flow.

The communication load between  $G_1$  and  $G_2$  depends on how many support vectors are needed by  $G_2$  to represents the boundary of the region with strong flow. The number of support vectors can be adjusted by the width  $\sigma$  in the Gaussian kernel  $K_G$ . To see the effect of  $\sigma$  on the number of the support vectors, let us consider a very small  $\sigma$ . In this case

$$K_G(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\frac{(\mathbf{x}_i - \mathbf{x}_j)^2}{\sigma^2}) \simeq 0$$

when  $i \neq j$ . Then Equation (2) becomes  $L = 1 - \sum_i \alpha_i^2$  which is maximized when all  $\alpha_i^* = \frac{1}{N}$ . In this situation, all

the data points in the cluster become support vectors, and no compression is achieved. For a very large  $\sigma$ ,  $K_G(\mathbf{x}_i, \mathbf{x}_j) \simeq 1$ . Then equation (2) becomes  $L = 1 - \sum_i \alpha_i^2 - \sum_{i \neq j} \alpha_i \alpha_j$  which is maximized by letting only one  $\alpha_i^* = 1$ . Hence, only one data point will be selected to represent the entire cluster. We deduce that  $\sigma$  should be determined by considering the quality of the communication link between  $G_1$  and  $G_2$ . If the link quality is high, then more support vectors can be used. If the link quality is low, then we should reduce the number of support vectors.

We consider three main components in quality estimation of the link between  $G_1$  and  $G_2$ :

- **Packet Delay Variation.** Packet delay is the time it takes to transmit a packet from source to destination. Packet delay time includes queuing time (related to packaging time of transmitter), propagating time (related to distance and medium), processing time (related to quality of receiver) and transmitting time (related to relay stations, if exist). Under standard communication condition, nominal packet delay time across certain distance can be calculated before hand. The variation represents the deviation between actual packet delay and the nominal packet delay.
- **Packet Loss Rate.** Packet loss rate equals the number of packets lost during transmission divided by the total number of transmitted packets. Packet loss occurs due to congestion and broken communication link caused by node failures or blocks.
- **Bit Error Rate (BER).** Different from packet loss rate that the entire packet has been lost, bit error rate is the number of bit errors divided by the total number of bits in a received packet. Bit errors indicate the number of received bits that have been altered due to noise, interference, distortion or bit synchronization errors.

Our research goal is to determine a proper  $\sigma$  which will balance the representation error  $e_1$  and  $e_2$  while the resulted payload is below a safe threshold of the estimated communication link. In particular, we formulate a constrained optimization problem as follows:

$$\min_{\sigma} E = e_1 + e_2 \quad (5)$$

under the constraint

$$\text{RLQ} \leq Q_t \quad (6)$$

where RLQ represents the Required Level of Quality for sending packets with certain size under the communication link and  $Q_t$  is a predetermined threshold.

#### IV. LINK QUALITY ESTIMATION

In general, the RLQ of a communication link to transmit  $n_d$  data bits can be modeled by the following equation:

$$\text{RLQ} = \eta(\kappa_1 \cdot \text{Var}(t_d) + \kappa_2 \cdot P) \quad (7)$$

The parameters  $\kappa_1$  and  $\kappa_2$  are positive regulating factors that can be chosen by design.  $t_d$  represents the packet delay and  $\text{Var}(t_d)$  represents the variation in the packet delay.  $P$  represents the bit error rate. And  $\eta$  is a function of both the bit error rate and the packet loss rate. We will discuss how to determine these parameters.

#### A. Estimation of the Parameters

For  $G_2$  to measure Packet Delay Variation, a nominal time delay  $t_n$  for transmitting a packet of certain size over an established link is needed. Under standard communicating condition,  $t_n$  can be theoretically calculated. The transmitter should process a  $n$  bits packet before transmitting it. Let this processing time be  $t_s = n \cdot T_s$  while  $T_s$  is the time to process one bit data for transmitting. The time for receiver to process this packet is  $t_r = n \cdot T_r$  while  $T_r$  is the time to receive and check one bit. Thus a nominal delay time for transmitting a packet is

$$t_n = 2 \cdot (t_s + t_r + t_p)$$

where  $t_p = d/c$  is the propagating time from leaving the transmitter to arriving the receiver.  $d$  is the distance between the transmitter and the receiver,  $c$  is the nominal speed for a signal propagating in a medium. If the communication is over an underwater acoustic link,  $c$  equals about 1500 m/s. If  $G_2$  measures  $m$  delay time  $\{t_{d_i}\}$ , the variance of packet delay can be calculated by

$$\text{Var}(t_d) = \frac{1}{m} \sum_{i=1}^m (t_{d_i} - t_n)^2 \quad (8)$$

However, the nominal time delay  $t$  is rarely known in practice since the distance between the two gliders is unknown.

The protocol we propose to evaluate the packet delay variation, the packet loss rate and the bit error rate is adapted from Stop and Wait (S&W) scheme. This protocol requires that the transmitter, say  $G_2$ , stops and waits for a acknowledgement response after sending a handshaking message. After a link has been built,  $G_2$  sends  $G_1$  a testing packet which contains  $n$  bits. In this  $n$  bits data,  $n_h$  is allocated for the header bits,  $n_d$  is allocated for data bits and  $n_t$  is allocated for the tail bits. The  $n_d$  data bits contains a predefined sequence which is known to both the transmitter and the receiver. When  $G_1$  receives the packet, it checks the bit error and records the bit error rate as  $BER_s$ , also called *sending BER*. Immediately,  $G_1$  starts a new test packet with its  $n_t$  tail bits filled with the  $BER_s$  as a responding packet to send back to  $G_2$ . After receiving this response,  $G_2$  checks the bit error rate  $BER_r$ , also called *returning BER*, and reads  $BER_s$  together to estimate the bit error rate. Let the probability of bit error be  $p$  which can be a function of  $BER_r$  and  $BER_s$ , mathematically

$$p = f(BER_r, BER_s) \quad (9)$$

Then the total average bits error probability is

$$P = 1 - (1 - p)^{n_d} \quad (10)$$

Here we only concern the error of data bits and assume that the bit error occurs independently.

If  $G_2$  fails to receive the response, then either  $G_1$ 's response is lost or  $G_1$  does not receive the packet at all. When  $G_2$  sends a packet, no matter the response is received or not, we say that  $G_2$  performs a *one-round test*. This one-round test is successful if the response of the packet is received and failing if the response is not received within a predefined time interval. If failure, a new packet is retransmitted by  $G_2$  thus starts a new one-round test. When the response is finally received even after several retries or the maximum limit of retries has reached, we

say a *full round test* has been performed. A full-round test may contain many one-round tests. If a one-round test fails and the packet has been retransmitted  $n_w$  times with  $t_w$  being the time interval between the retransmissions, then a delay of  $n_w t_w$  occurs. Let  $T_d$  be the time of successfully transmitting one packet at the last one-round test. Then the full-round test takes a total time given below

$$t_d = T_d + n_w \cdot t_w, \quad 0 \leq n_w \leq n_m \quad (11)$$

where  $n_w$  denotes how many times  $G_2$  does not receive a response in a full-round test and indicates the Packet Loss Rate.  $n_m$  is the maximum limit of retries.

Suppose the handshaking protocol performs  $k$  full-round tests, then  $G_2$  will measure a set of  $\{T_{di}\}$  and a set of  $\{t_{di}\}$ ,  $i = 1 \dots k$ . We evaluate  $t_n$  by

$$t_n = \frac{1}{k} \sum_{i=1}^k T_{di} \quad (12)$$

The variance of packet delay  $\text{Var}(t_d)$  is then evaluated using equation (8).

For each one-round test, we just want to correctly transmit the  $n_d$  data bits. Time for processing  $n_d$  bits is  $n_d \cdot T_s$  while the nominal time spent is  $t_n$ . Considering the bits error, the effective time for transmission of the data bits would be  $n_d \cdot T_s \cdot (1 - P)$  where  $P$  is the total average bits error rate in (10). The efficiency of the transmission then can be described by

$$\eta = \frac{n_d \cdot T_s \cdot (1 - P)}{t_n} = \frac{n_d \cdot T_s}{t_n} \cdot (1 - p)^{n_d} \quad (13)$$

This efficiency  $\eta$  takes the bit error probability  $p$  into consideration as well as the communication load  $n_d$ . The efficiency would be improved if  $n_d$  increases and  $p$  decreases.

Until now, all parameters in the RLQ equation (7) have been estimated. If a link has constant  $\text{Var}(t_d)$  and  $P$ , then larger  $n_d$  leads higher efficiency  $\eta$ , but requires higher RLQ. If either the  $\text{Var}(t_d)$  or  $P$  becomes larger, then the RLQ for sending a packet with the same size becomes higher.

Fig. 2 illustrates that the RLQ related to the number of data bits  $n_d$ . We assume that the CPU works at 10MHz e.g.  $T_s = 1/10^7 s$ . The average nominal time delay  $t = 0.5s$ , the packet delay variance  $\text{Var}(t_d) = 0.01$  and the bit error rate  $p = 10^{-4}$ . The regulating parameters are selected by  $\kappa_1 = 1/8T_s$  and  $\kappa_2 = 1/10T_s$ . When the link is under poorer condition, the

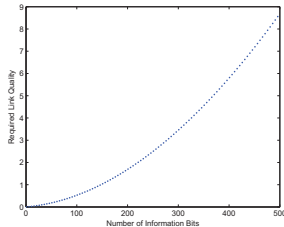


Fig. 2. The Required Level of Quality for transmitting varying  $n_d$  bits under certain communication condition.

RLQ for transmitting packet with same size becomes higher. Fig. 3(a) shows that the RLQ along with the range of the bit

error rate  $p$  evaluated by equation (9). The information bits in this case is selected as  $n_d = 300$ . The others are identical to those in Fig. 2. We can see that with increasing of  $p$ , the quality is deteriorating. RLQ changing with the time delay variance  $\text{Var}(t_d)$  is shown in Fig. 3(b). The bit error rate  $p$  is set to be  $10^{-4}$ .

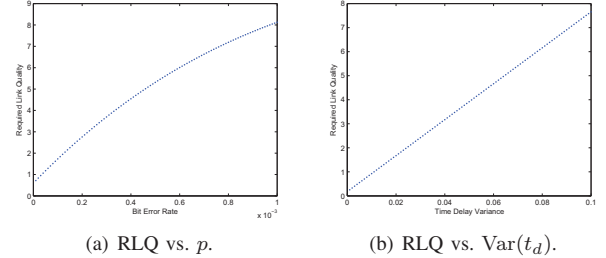


Fig. 3. The Required Level of Quality for transmitting certain  $n_d$  data bits under different communication condition.

### B. Determine the Compression Level

We now come back to the optimization problem in (5). The constraint

$$\text{RLQ} \leq Q_t$$

needs to be satisfied. RLQ is related to the number of data bits  $n_d$ . Let  $c$  be the number of bits for coding one number. There are  $N_{SV}$  two dimensional support vectors plus one parameter for  $\sigma$ , the width of Gaussian kernel, to be coded. Therefore,

$$n_d = c(1 + 2N_{SV}). \quad (14)$$

Hence RLQ is now a function of  $N_{SV}$  determined by  $\sigma$ . The representing errors  $e_1$  and  $e_2$  in the optimization problem (5) are also determined by  $\sigma$  if the testing points are preselected.

It is difficult to solve this problem directly. Instead, we pursue approximation solution using numerical method. In our model, the RLQ is increasing with varying  $n_d$  under certain communication condition. So that the preset  $Q_t$  would claim that the transmitting data bits  $n_d$  should be less than a certain  $n_d^*$ . The number of support vectors related to  $n_d^*$  is denoted by  $N_{SV}^*$ . If the link quality is not considered, or no constraints existed in the optimization problem, there is a  $\sigma$  which leads minimal error  $E$ , denoted by  $\sigma_{op}$ . The number of support vectors resulted by  $\sigma_{op}$  is  $N_{SV}^{op}$ . We compare  $N_{SV}^{op}$  with  $N_{SV}^*$  to see whether the global optimal  $\sigma_{op}$  can be selected. If  $N_{SV}^{op}$  satisfies that  $N_{SV}^{op} < N_{SV}^*$ , which means the resulting communication load is within safe threshold, then  $\sigma_{op}$  is chosen. Otherwise,  $N_{SV}^{op} > N_{SV}^*$ , indicates that packet of such size would be corrupted during the upcoming communication. For sake of safety, we should minimize the number of  $N_{SV}$  to contain less communication load. The  $\sigma$  should be increased to minimize  $N_{SV}$ . While the increased  $\sigma$  leads larger error than minimal  $E$ . The optimal  $\sigma$  in this situation should be the one its resulting  $N_{SV} < N_{SV}^*$  and the same time the error  $E$  is minimal.

## V. PATH PLANNING SIMULATION USING REDUCED INFORMATION

After receiving the support vectors and weights from all other gliders,  $G_1$  now has sufficient knowledge to plan



paths using the fast marching algorithm [3].  $G_1$  interprets the information into knowledge about the outside blank zone. It checks whether a grid point is within an area with strong flow or not using the support vectors  $S$  and corresponding  $\alpha^*$  using Equation (3).

We assume that five gliders  $G_1, G_2, G_3, G_4$  and  $G_5$  work in a rectangular region in the ocean that is discretized into 50 by 50 grid points. The initial positions are  $G_1(14, 15)$ ,  $G_2(18, 34)$ ,  $G_3(25, 20)$ ,  $G_4(39, 15)$  and  $G_5(39, 39)$  respectively. The (simulated) spatially distributed currents in this region are generated by the ocean current model used in [8]. Within

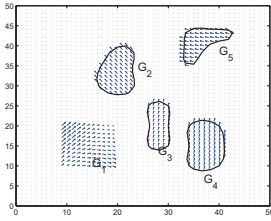


Fig. 4. SVDD results on the high-flow regions in each glider's local patch.

their own patch, gliders  $G_2, G_3, G_4$  and  $G_5$  pick out the grid points with velocity greater than  $v = 0.22$  while  $G_1$  is moving at speed  $v_g = 0.25$ . The selected high-flow regions are denoted by  $\Omega_2, \Omega_3, \Omega_4$  and  $\Omega_5$  respectively, shown in Fig. 4.

Each glider uses SVDD to compress the region with higher flow. The Gaussian kernel width  $\sigma$  is determined to satisfy equation (5) and constraint (6). We set parameters in link quality estimation  $T_s = 1/10^7 s$ ,  $t = 0.5 s$ ,  $\text{Var}(t_d) = 0.001$  and  $p = 10^{-4}$ . The regulating parameters are selected as  $\kappa_1 = 1/8T_s$  and  $\kappa_2 = 1/10T_s$ . Let  $c$  in equation (14) be 30. Take  $\Omega_5$  for instance, we set  $Q_t = 6.3$ , the consequence is that the  $N_{SV}$  should be smaller than a threshold. We directly plot out the relationship between  $\sigma$  and RLQ, as shown in Fig. 5(a). The error estimation  $E$  change with  $\sigma$  is plotted in Fig. 5(b). Constrained by  $Q_t$ , the  $\sigma$  should larger than 4.2.

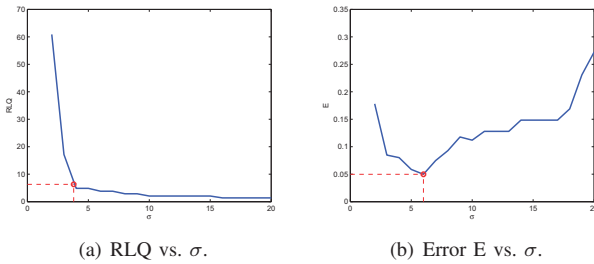


Fig. 5. For  $\Omega_2$ , the optimal  $\sigma$  could meet the requirement of safety link quality  $Q_t$ .

From Fig. 5(b), we can see that the least  $E = 0.0499$  occurs when  $\sigma = 6$ . Thus in this situation, the optimal  $\sigma$  equals 6. For  $\Omega_3$ , see Fig. 6(a), the  $\sigma$  should be larger than 3.6. Comparing with Fig. 6(b), the optimal  $\sigma$  should be 4 although the global minimum is located at  $\sigma = 3$ .

The distributed path planning result is shown in Fig. 7(b), we label this situation as “distributed”. For comparison, we assume that  $G_1$  knows the flow information of the entire

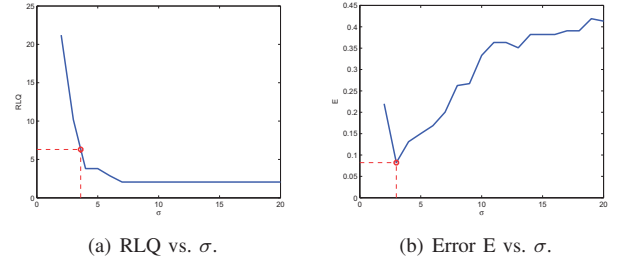


Fig. 6. For  $\Omega_3$ , the optimal  $\sigma$  could not meet the requirement of safety link quality  $Q_t$ . A sub-optimal  $\sigma$  is chosen.

region, this situation is labeled as “global”. The global path planning results is shown in Fig. 7(a). We can see that in this situation the glider  $G_1$  would leverage the high-flow region.

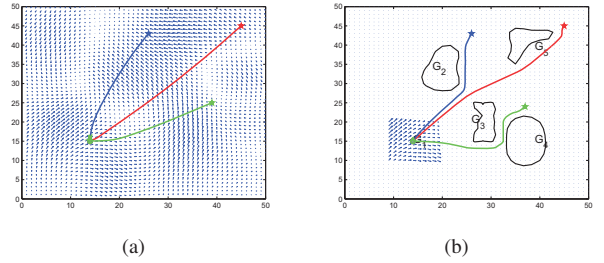


Fig. 7. (a) Global path planning; (b) Distributed path planning.

If the quality of a link is under lower level, in simulation, we change the time delay variance  $p$  from  $10^{-4}$  to  $10^{-2}$ , then sending same size packet would need higher required link quality. The RLQ with varying  $\sigma$  is shown in Fig. 8(a). If the safety threshold is required to be 6.3, the  $\sigma$  should be larger than 9.2. Then the optimal  $\sigma$  moves to 10. Fig. 9 shows

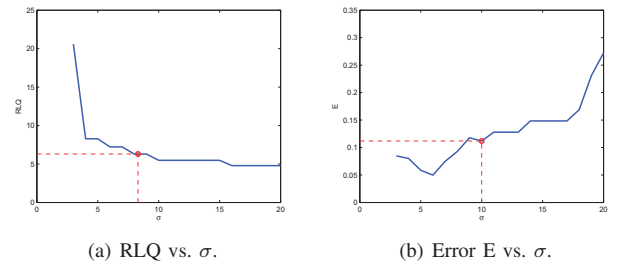


Fig. 8. For  $\Omega_3$ , the global optimal  $\sigma$  could not meet the requirement of safety link quality  $Q_t$ . The chosen  $\sigma$  is a local one.

the paths planed with lower-level link quality comparing with the higher quality results. The planner of  $G_1$  recognizes and rebuilds the high-flow region by checking whether a gridpoint is accepted by the SVDD mapping. If accepted, the flow on this point is signed to be the average flow together with this SVDD. When the  $\sigma$  becomes large, the description would accept lot of points that are not originally belong to the high-flow region  $\Omega$ . Therefore the rebuilt regions in Fig. 9(b) are larger than the Fig. 9(a). Under poorer communication condition, more grid points are viewed as obstacles. The paths deviate from the optimal path.

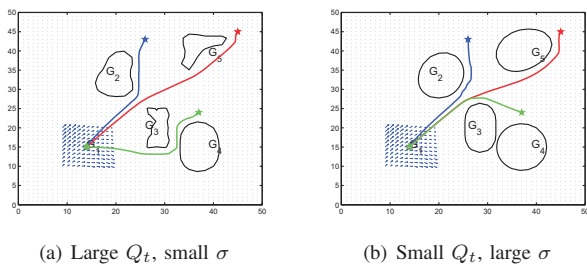


Fig. 9. Paths planned with different  $\sigma$ .

## VI. CONCLUSIONS AND FUTURE WORK

This paper presents a novel approach to adjust the parameter of SVDD which is used to reduce information shared among underwater gliders for path planning based on link quality estimation. It is shown that the SVDD method with properly determined parameter  $\sigma$  can effectively represent the boundary of the regions with strong current. Simulation results show that the link quality estimation works well to determine the ratio of reduction to balance the accuracy of shared information with the quality of the communication link. Our future work will explore possibilities of representing the direction of the strong flow so that some high flow regions can be leveraged by path planning.

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