Objective

The objective of this presentation is:

- 1.) Illustrate the frequency analysis of single stage amplifiers
- 2.) Introduce the Miller technique and the approximate method of solving for two poles

Outline

- Differential and Common Frequency Response of the Differential Amplifier
- Emitter/Source Follower Frequency Response
- Common Base/Gate Frequency Response
- Summary

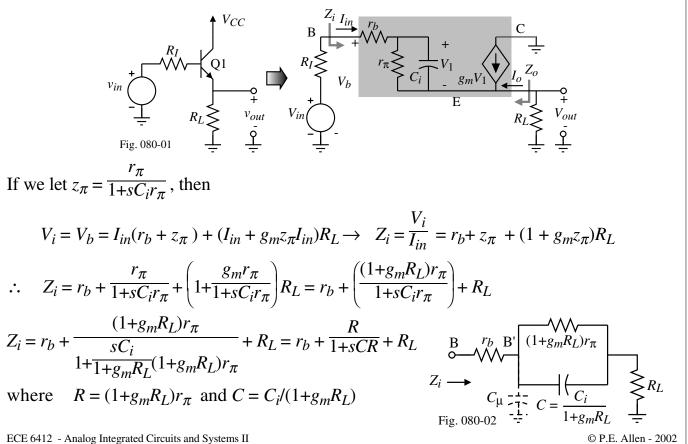
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Lecture 080 – 1 Stage Frequency Response -II (1/10/02)

Emitter Follower Input Impedance



Emitter Follower Output Impedance

From the previous model (or from the impedance transformation aspect of a BJT) we can write,

$$Z_{o} = \frac{V_{out}}{I_{o}} = \frac{z_{\pi} + R_{I} + r_{b}}{1 + g_{m}z_{\pi}} = \frac{z_{\pi} + R_{I}'}{1 + g_{m}z_{\pi}} = \frac{\frac{r_{\pi}}{1 + sC_{i}r_{\pi}} + R_{I}'}{1 + \frac{g_{m}r_{\pi}}{1 + sC_{i}r_{\pi}}} = \frac{r_{\pi} + R_{I}' + sC_{i}r_{\pi}R_{I}'}{\beta_{0} + 1 + sC_{i}r_{\pi}}$$

Multiplying top and bottom by $1/\beta_0$, gives

$$Z_o = \frac{\left(\frac{1}{g_m} + \frac{R_I'}{\beta_0} + sC_i r_\pi \frac{R_I'}{\beta_0}\right) R_I'}{R_I' + sC_i r_\pi \frac{R_I'}{\beta_0}} = \frac{(R_1 + sL)R_2}{R_2 + sL} \quad \text{assuming } \beta_0 >> 1.$$

Equivalent output circuit:

$$R_{1} = \frac{1}{g_{m}} + \frac{R_{I'}}{\beta_{0}}$$

$$R_{2} = R_{I'}$$

$$R_{2} = R_{I'}$$
Fig. 080-03

V

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Lecture 080 - 1 Stage Frequency Response -II (1/10/02)

Source Follower Frequency Response

From the previous lecture for the MOSFET $r_{\pi} = \infty$, $r_b = 0$, and $R'_L = \frac{R_L}{1 + g_{mbs}R_L}$

$$\frac{v_{out}}{v_{in}} = \frac{g_m R'_L + \frac{R'_L}{r_\pi}}{1 + g_m R'_L + \frac{R'_I + R'_L}{r_\pi}} \left[\frac{1 - \frac{s}{z_1}}{1 - \frac{s}{p_1}} \right] \longrightarrow \frac{v_{out}}{v_{in}} = \frac{g_m R'_L}{1 + g_m R'_L} \left[\frac{1 - \frac{s}{z_1}}{1 - \frac{s}{p_1}} \right]$$

ere $z_1 = -\frac{g_m}{C_{gs}}, \quad p_1 = -\frac{1}{R_1 C_{gs}} \text{ and } R_1 = \frac{R_I + R'_L}{1 + g_m R'_L} \approx \frac{1}{g_m}$

where

Calculate the transfer function for a source follower with C_{gs} =7.33pF, K'W/L=100mA/V², $R_L=2k\Omega$, $R_I=190\Omega$, and $I_D=4mA$. Let $g_{mbs} \approx 0$, $C_{gd}=0$, $C_{gb}=0$, and $C_{bs}=0$. Solution

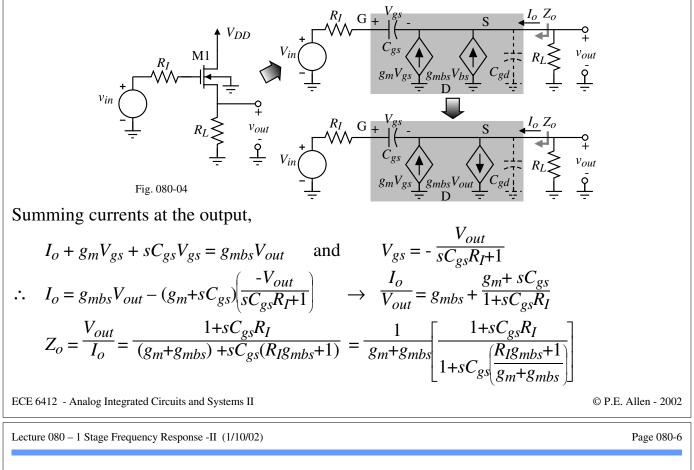
$$g_m = \sqrt{2(100)4} \text{ mA/V} = 28.2 \text{mA/V}. \qquad \frac{v_{out}}{v_{in}} = \frac{28.2 \cdot 2}{1 + 28.2 \cdot 2} = 0.983 \text{V/V}$$
$$|z_1| = \omega_T = \frac{g_m}{C_{gs}} = 3.85 \text{x} 10^9 \text{ rads/s}, \qquad R_1 = \frac{R_I + R'_L}{1 + g_m R'_L} = \frac{190 + 2000}{1 + 128.2 \cdot 2} = 38.2 \Omega,$$
$$p_1 = -\frac{10^{12}}{38.2 \cdot 7.33} = -3.57 \text{x} 10^9 \text{ rads/s} \qquad (C_{gd}, C_{gb}, \text{ and } C_{bs} \text{ cause two poles, 1 zero)}$$

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Source Follower Output Impedance

The output impedance of the source follower can be found from the previous general analysis or from the following model:



Identification of the Output Impedance

Find the value of R_1 , R_2 , and L in the equivalent output impedance model shown for the source follower.

Note that,

...

$$Z_o = \frac{R_2(R_1 + sL)}{R_1 + R_2 + sL} \approx \frac{R_2(R_1 + sL)}{R_2 + sL} \quad \text{if} \quad R_1 << R_2$$

The best way to solve this problem is to use the limits of Z_o .

$$\lim Z_o (s \to 0) = \frac{R_1 R_2}{R_1 + R_2} \approx R_1 = \frac{1}{g_m + g_{mbs}} \text{ where } R_1 << R_2$$
$$\lim Z_o (s \to \infty) = R_2 = \frac{R_I}{R_I g_{mbs} + 1}$$
$$L = \frac{C_{gs}(1 + R_I g_{mbs})}{g_m + g_{mbs}} = \frac{C_{gs} R_I R_1}{R_2}$$

If one includes C_{gd} in parallet with the equivalent circuit, the potential for resonance of the output impedance will occur roughly at $\sqrt{\frac{1}{LC_{gd}}}$ if R_1 is small. Using the values of the previous example with $g_{mbs} = 0.1g_m$ and $C_{gd} = 0.5$ pf gives $R_1 = 32.2\Omega$, $R_2 = 123.7\Omega$ and $L = (7.33 \text{pF} \cdot 190\Omega \cdot 32.2\Omega/123.7\Omega) = 0.362 \text{nH} \Rightarrow f_{osc} = 11.8 \text{GHz}$

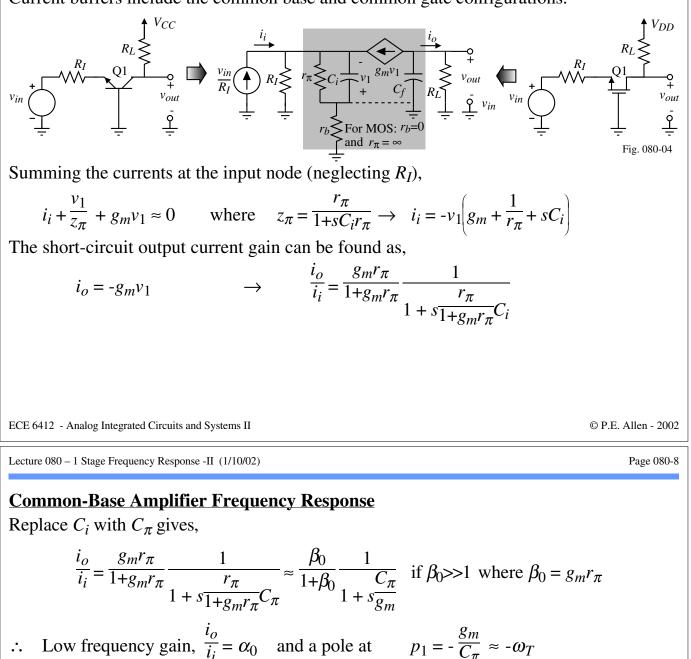
Vout

Fig. 080-05

 R_2

 $-Z_o$

Current buffers include the common base and common gate configurations.



If the output current flows through R_L , then the current gain has another pole due to C_u :

$$\frac{i_o}{i_i} = \frac{g_m r_\pi}{1 + g_m r_\pi} \frac{1}{1 + s \frac{r_\pi}{1 + g_m r_\pi} C_\pi} \frac{1}{1 + s R_L C_\mu} \approx \frac{\beta_0}{1 + \beta_0} \left(\frac{1}{1 + s \frac{C_\pi}{g_m}}\right) \left(\frac{1}{1 + s R_L C_\mu}\right) = A_i \left(\frac{1}{1 + \frac{s}{p_1}}\right) \left(\frac{1}{1 + \frac{s}{p_2}}\right) \left($$

Example:

If $I_C = 1$ mA, $\beta_0 = 100$, $C_{\pi} = 10$ pF, $C_{\mu} = 0.5$ pF, $C_{cs} = 1$ pf, and $R_L = 2$ k Ω , evaluate the CB amplifier. $g_m = 1/26$ mS

$$A_i = 0.99, p_1 = -2.6 \times 10^{12} \text{ rad/s}, \text{ and } p_2 = -\frac{1}{R_L(C_\mu + C_{cs})} = -0.333 \times 10^9 \text{ rad/s}$$

Common Gate Amplifier Frequency Response

Short-circuit current gain:

$$\frac{i_o}{i_i} = \frac{g_m r_\pi}{1 + g_m r_\pi} \frac{1}{1 + s \frac{r_\pi}{1 + g_m r_\pi} C_i} \longrightarrow \frac{i_o}{i_i} = \frac{1}{1 + s \frac{C_{gs} + C_{bs}}{g_m + g_{mbs}}}$$

Current gain ($R_L \neq 0$):

$$\frac{\dot{i}_{o}}{\dot{i}_{i}} = \frac{1}{1 + s\frac{C_{gs} + C_{bs}}{g_{m} + g_{mbs}}} \left(\frac{1}{1 + sR_{L}C_{gd}}\right) = A_{i} \left(\frac{1}{1 + \frac{s}{p_{1}}}\right) \left(\frac{1}{1 + \frac{s}{p_{2}}}\right)$$

where

$$A_i = 1$$
, $p_1 = -\frac{g_m + g_{mbs}}{C_{gs} + C_{bs}}$ and $p_2 = -\frac{1}{R_L C_{gd}}$

Example

Calculate the transfer function for a common-gate amplifier with C_{gs} =7.33pF, *K'W/L*=100mA/V², R_L =2k Ω , and I_D =4mA. Let $g_{mbs} \approx 0$, C_{gd} = 1pF, and C_{bs} = 2pF.

$$g_m = \sqrt{2.4 \cdot 100} \text{ mS} = 28.2 \text{mS}$$
 \therefore $p_1 = -\frac{28.2 \times 10^{-3}}{9.33 \times 10^{-12}} = -3.03 \times 10^9 \text{ rad/s}$
and $p_2 = -\frac{1}{2000 \cdot 10^{-12}} = 0.5 \times 10^9 \text{ rad/s}$

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Lecture 080 – 1 Stage Frequency Response -II (1/10/02)

SUMMARY

- The emitter follower and source follower have very high frequency responses
- The –3dB frequency will most likely be caused by the pole at the output of the follower
- The equivalent output of the emitter follower is inductive
- The common base and common gate amplifiers have a current gain of 1
- The CB and CG amplifiers have a high frequency response because of the low input resistance at the input
- If $R_L \neq 0$, the pole at the output of the CB and CG amplifiers causes the -3dB frequency
- The common base amplifier has an input impedance that is inductive
- More detailed analysis of these amplifiers leads to complex poles which will influence the high frequency behavior

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