

## **LECTURE 120 – COMPENSATION OF OP AMPS - I**

**(READING: GHLM – 425-434 and 624-638, AH – 249-260)**

### **INTRODUCTION**

The objective of this presentation is to present the principles of compensating two-stage op amps.

#### **Outline**

- Compensation of Op Amps
  - General principles
  - Miller, Nulling Miller
  - Self-compensation
  - Feedforward
- Summary

## **GENERAL PRINCIPLES OF OP AMP COMPENSATION**

### **Objective**

Objective of compensation is to achieve stable operation when negative feedback is applied around the op amp.

### **Types of Compensation**

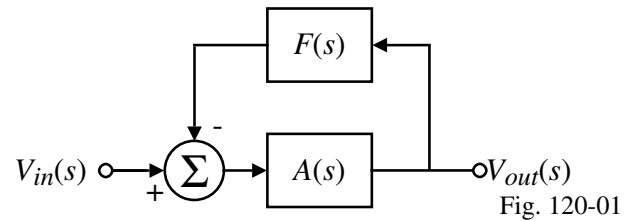
1. Miller - Use of a capacitor feeding back around a high-gain, inverting stage.
  - Miller capacitor only
  - Miller capacitor with an unity-gain buffer to block the forward path through the compensation capacitor. Can eliminate the RHP zero.
  - Miller with a nulling resistor. Similar to Miller but with an added series resistance to gain control over the RHP zero.
2. Feedforward - Bypassing a positive gain amplifier resulting in phase lead. Gain can be less than unity.
3. Self compensating - Load capacitor compensates the op amp.

## Single-Loop, Negative Feedback Systems

Block diagram:

$A(s)$  = differential-mode voltage gain of the op amp

$F(s)$  = feedback transfer function from the output of op amp back to the input.



Definitions:

- Open-loop gain =  $L(s) = -A(s)F(s)$
- Closed-loop gain =  $\frac{V_{out}(s)}{V_{in}(s)} = \frac{A(s)}{1+A(s)F(s)}$

Stability Requirements:

The requirements for stability for a single-loop, negative feedback system is,

$$|A(j\omega_0)F(j\omega_0)| = |L(j\omega_0)| < 1$$

where  $\omega_0$  is defined as

$$\text{Arg}[-A(j\omega_0)F(j\omega_0)] = \text{Arg}[L(j\omega_0)] = 0^\circ$$

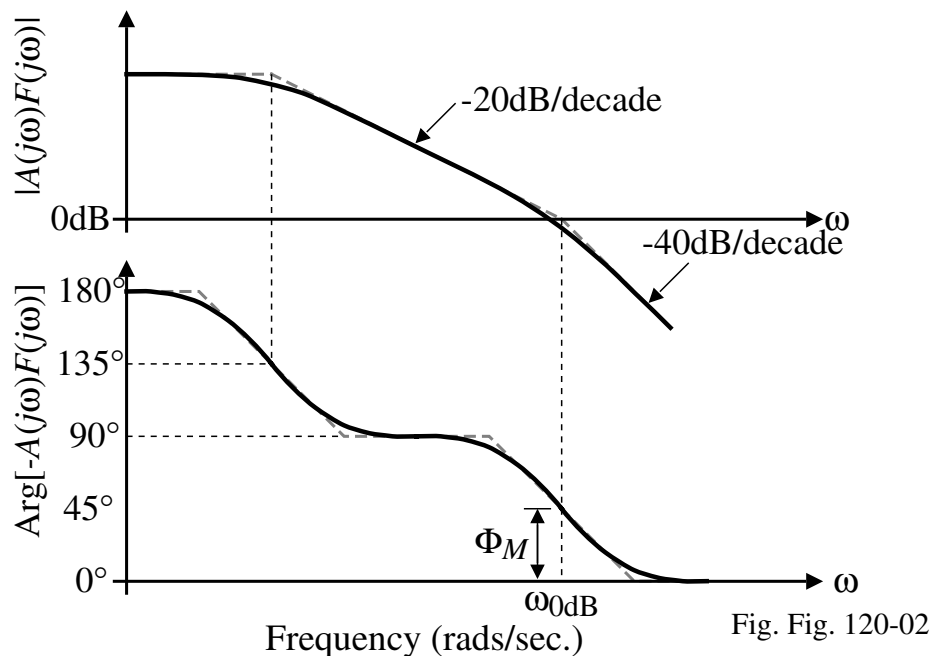
Another convenient way to express this requirement is

$$\text{Arg}[-A(j\omega_{0dB})F(j\omega_{0dB})] = \text{Arg}[L(j\omega_{0dB})] > 0^\circ$$

where  $\omega_{0dB}$  is defined as

$$|A(j\omega_{0dB})F(j\omega_{0dB})| = |L(j\omega_{0dB})| = 1$$

## Illustration of the Stability Requirement using Bode Plots

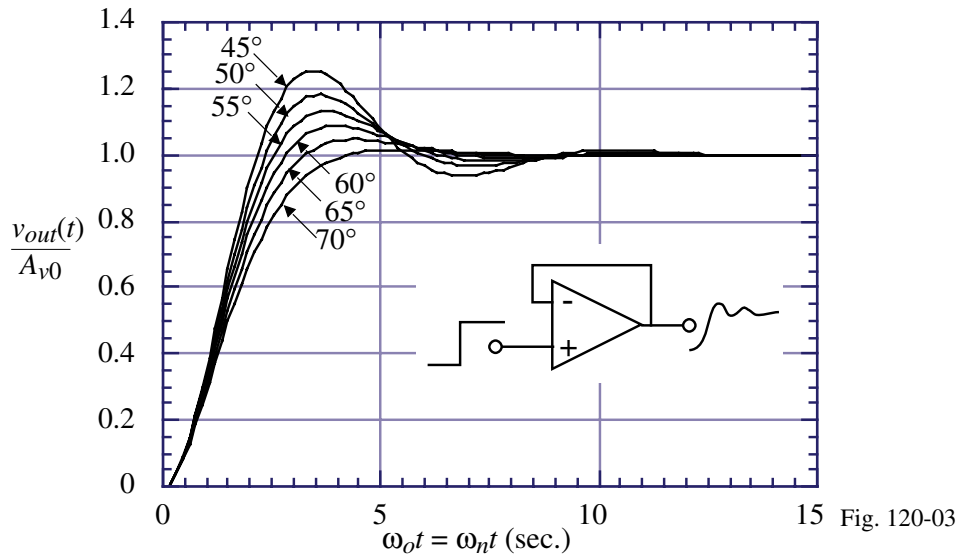


A measure of stability is given by the phase when  $|A(j\omega)F(j\omega)| = 1$ . This phase is called *phase margin*.

$$\text{Phase margin} = \Phi_M = \text{Arg}[-A(j\omega_{0dB})F(j\omega_{0dB})] = \text{Arg}[L(j\omega_{0dB})]$$

### Why Do We Want Good Stability?

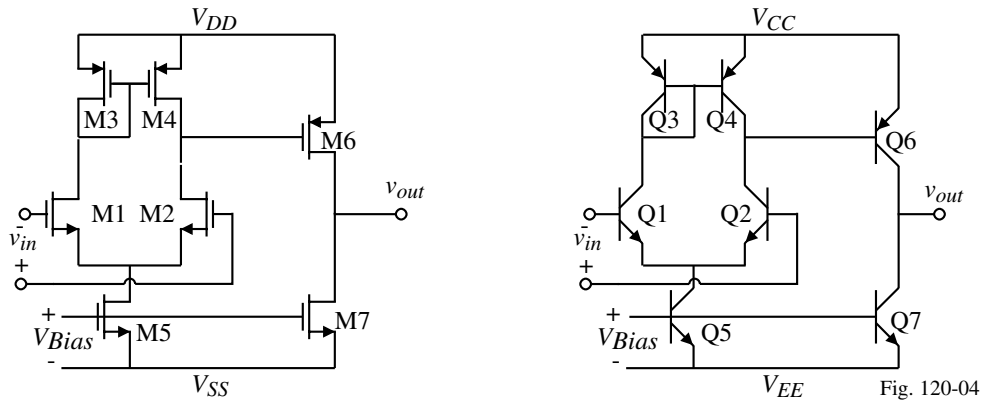
Consider the step response of second-order system which closely models the closed-loop gain of the op amp.



A “good” step response is one that quickly reaches its final value. Therefore, we see that phase margin should be at least 45° and preferably 60° or larger. (A rule of thumb for satisfactory stability is that there should be less than three rings.)

### Uncompensated Frequency Response of Two-Stage Op Amps

Two-Stage Op Amps:



Small-Signal Model:

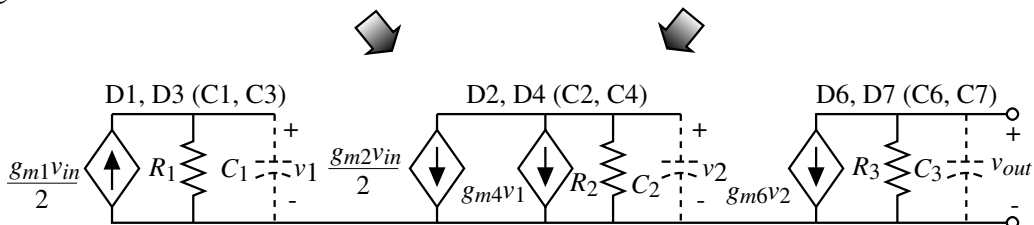


Fig. 120-05

Note that this model neglects the base-collector and gate-drain capacitances for purposes of simplification.

## Uncompensated Frequency Response of Two-Stage Op Amps - Continued

For the MOS two-stage op amp:

$$R_1 \approx \frac{1}{g_{m3}} \parallel r_{ds3} \parallel r_{ds1} \approx \frac{1}{g_{m3}}$$

$$R_2 = r_{ds2} \parallel r_{ds4}$$

$$\text{and } R_3 = r_{ds6} \parallel r_{ds7}$$

$$C_1 = C_{gs3} + C_{gs4} + C_{bd1} + C_{bd3}$$

$$C_2 = C_{gs6} + C_{bd2} + C_{bd4}$$

$$\text{and } C_3 = C_L + C_{bd6} + C_{bd7}$$

For the BJT two-stage op amp:

$$R_1 = \frac{1}{g_{m3}} \parallel r_{\pi3} \parallel r_{\pi4} \parallel r_{o3} \approx \frac{1}{g_{m3}}$$

$$R_2 = r_{\pi6} \parallel r_{o2} \parallel r_{o4} \approx r_{\pi6}$$

$$\text{and } R_3 = r_{o6} \parallel r_{o7}$$

$$C_1 = C_{\pi3} + C_{\pi4} + C_{cs1} + C_{cs3}$$

$$C_2 = C_{\pi6} + C_{cs2} + C_{cs4}$$

$$\text{and } C_3 = C_L + C_{cs6} + C_{cs7}$$

Assuming the pole due to  $C_1$  is much greater than the poles due to  $C_2$  and  $C_3$  gives,

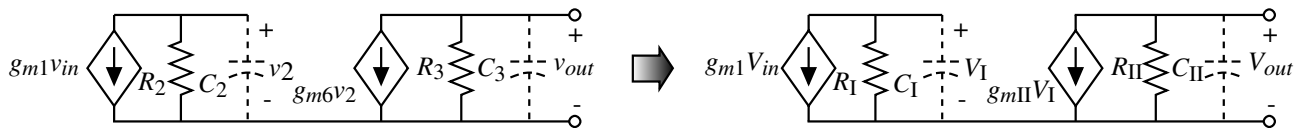


Fig. 120-06

The locations for the two poles are given by the following equations

$$p'_1 = \frac{-1}{R_I C_I} \quad \text{and} \quad p'_2 = \frac{-1}{R_{II} C_{II}}$$

where  $R_I$  ( $R_{II}$ ) is the resistance to ground seen from the output of the first (second) stage and  $C_I$  ( $C_{II}$ ) is the capacitance to ground seen from the output of the first (second) stage.

## Uncompensated Frequency Response of an Op Amp

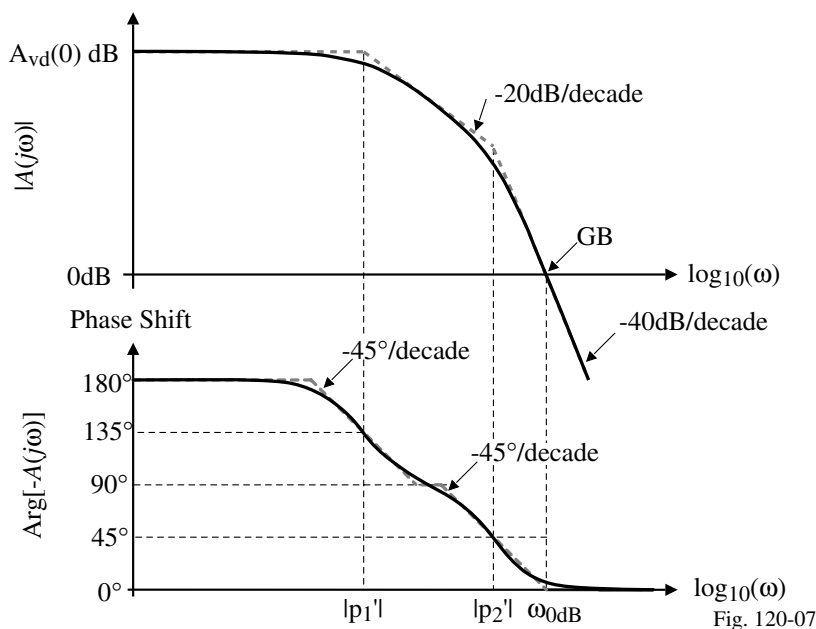


Fig. 120-07

If we assume that  $F(s) = 1$  (this is the worst case for stability considerations), then the above plot is the same as the loop gain.

Note that the phase margin is much less than  $45^\circ$ .

Therefore, the op amp must be compensated before using it in a closed-loop configuration.

## MILLER COMPENSATION

### Two-Stage Op Amp

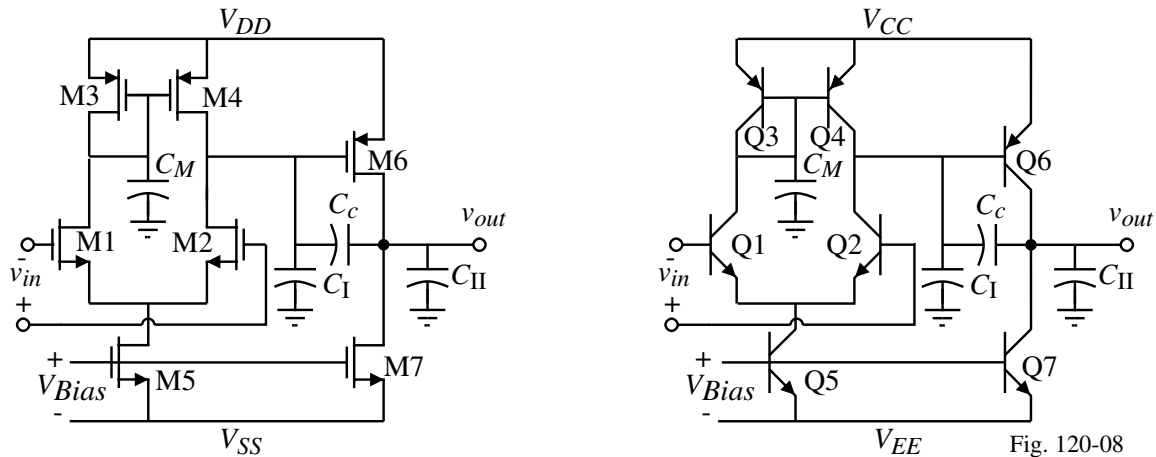


Fig. 120-08

The various capacitors are:

$C_c$  = accomplishes the Miller compensation

$C_M$  = capacitance associated with the first-stage mirror (mirror pole)

$C_I$  = output capacitance to ground of the first-stage

$C_{II}$  = output capacitance to ground of the second-stage

### Compensated Two-Stage, Small-Signal Frequency Response Model Simplified

Use the CMOS op amp to illustrate:

1.) Assume that  $g_{m3} \gg g_{ds3} + g_{ds1}$

2.) Assume that  $\frac{g_{m3}}{C_M} \gg GB$

Therefore,

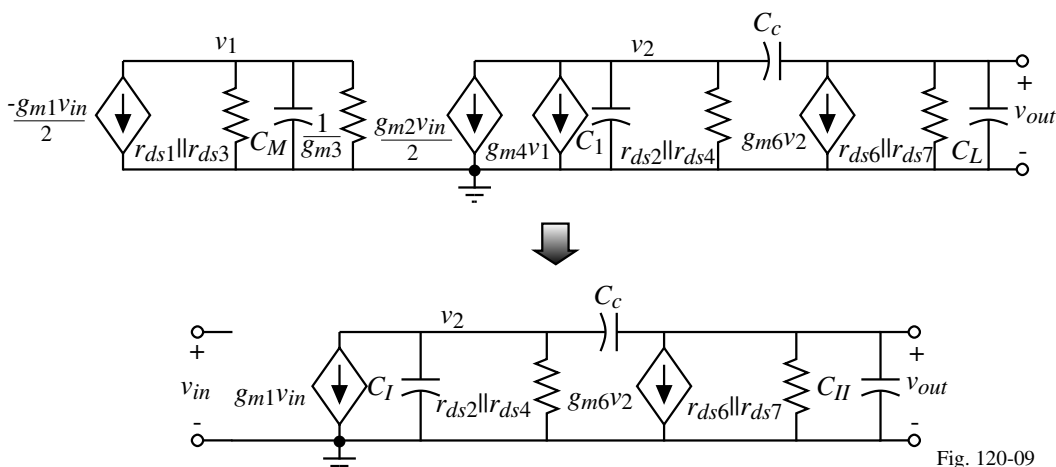
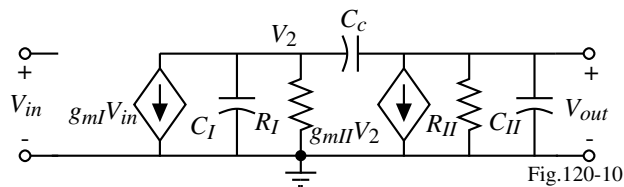


Fig. 120-09

Same circuit holds for the BJT op amp with different component relationships.

### General Two-Stage Frequency Response Analysis



where

$$g_{mI} = g_{m1} = g_{m2}, R_I = r_{ds2} || r_{ds4}, C_I = C_1$$

and

$$g_{mII} = g_{m6}, R_{II} = r_{ds6} || r_{ds7}, C_{II} = C_2 = C_L$$

Nodal Equations:

$$-g_{mI}V_{in} = [G_I + s(C_I + C_c)]V_2 - [sC_c]V_{out} \quad \text{and} \quad 0 = [g_{mII} - sC_c]V_2 + [G_{II} + sC_{II} + sC_c]V_{out}$$

Solving using Cramer's rule gives,

$$\frac{V_{out}(s)}{V_{in}(s)} = \frac{g_{mI}(g_{mII} - sC_c)}{G_I G_{II} + s[G_{II}(C_I + C_{II}) + G_I(C_{II} + C_c) + g_{mII}C_c] + s^2[C_I C_{II} + C_c C_I + C_c C_{II}]}$$

$$= \frac{A_o [1 - s(C_c / g_{mII})]}{1 + s[R_I(C_I + C_{II}) + R_{II}(C_2 + C_c) + g_{mII}R_I R_{II}C_c] + s^2[R_I R_{II}(C_I C_{II} + C_c C_I + C_c C_{II})]}$$

where,  $A_o = g_{mI}g_{mII}R_I R_{II}$

In general,  $D(s) = \left(1 - \frac{s}{p_1}\right)\left(1 - \frac{s}{p_2}\right) = 1 - s\left(\frac{1}{p_1} + \frac{1}{p_2}\right) + \frac{s^2}{p_1 p_2} \rightarrow D(s) \approx 1 - \frac{s}{p_1} + \frac{s^2}{p_1 p_2}$ , if  $|p_2| \gg |p_1|$

$$\therefore \boxed{p_1 = \frac{-1}{R_I(C_I + C_{II}) + R_{II}(C_{II} + C_c) + g_{mII}R_I R_{II}C_c} \approx \frac{-1}{g_{mII}R_I R_{II}C_c}, \quad z = \frac{g_{mII}}{C_c}}$$

$$\boxed{p_2 = \frac{-[R_I(C_I + C_{II}) + R_{II}(C_{II} + C_c) + g_{mII}R_I R_{II}C_c]}{R_I R_{II}(C_I C_{II} + C_c C_I + C_c C_{II})} \approx \frac{-g_{mII}C_c}{C_I C_{II} + C_c C_I + C_c C_{II}} \approx \frac{-g_{mII}}{C_{II}}, \quad C_{II} > C_c > C_I}$$

### Summary of Results for Miller Compensation of the Two-Stage Op Amp

There are three roots of importance:

1.) Right-half plane zero:

$$z_1 = \frac{g_{mII}}{C_c} = \frac{g_{m6}}{C_c}$$

This root is very undesirable- it boosts the magnitude while decreasing the phase.

2.) Dominant left-half plane pole (the Miller pole):

$$p_1 \approx \frac{-1}{g_{mII}R_I R_{II}C_c} = \frac{-(g_{ds2} + g_{ds4})(g_{ds6} + g_{ds7})}{g_{m6}C_c}$$

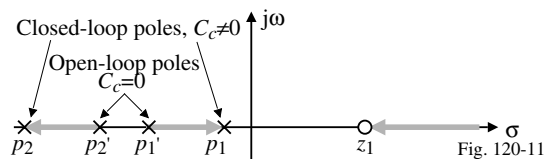
This root accomplishes the desired compensation.

3.) Left-half plane output pole:

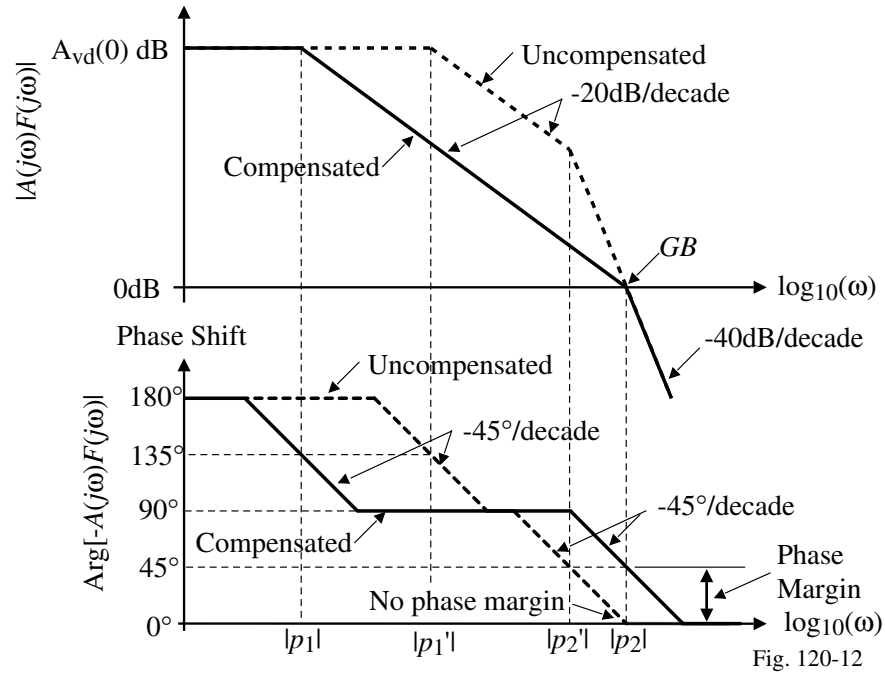
$$p_2 \approx \frac{-g_{mII}}{C_{II}} \approx \frac{-g_{m6}}{C_L}$$

This pole must be  $\geq$  unity-gainbandwidth or the phase margin will not be satisfied.

Root locus plot of the Miller compensation:



### Compensated Open-Loop Frequency Response of the Two-Stage Op Amp



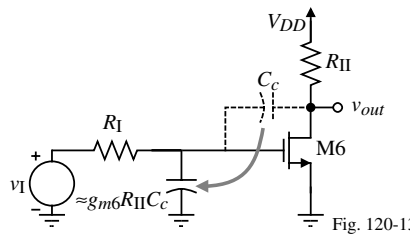
Note that the unity-gainbandwidth,  $GB$ , is

$$GB = A_{vd}(0) \cdot |p_1| = (g_{mI}g_{mII}R_I R_{II}) \frac{1}{g_{mII}R_I R_{II}C_c} = \frac{g_{mI}}{C_c} = \frac{g_{m1}}{C_c} = \frac{g_{m2}}{C_c}$$

### Conceptually, where do these roots come from?

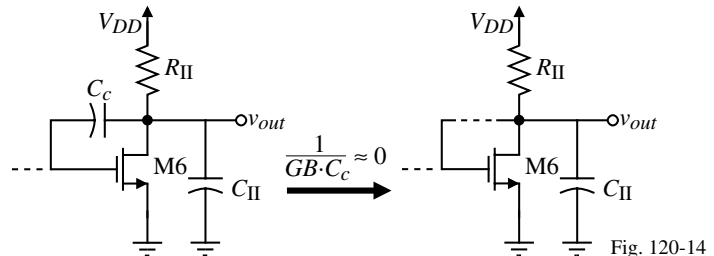
1.) The Miller pole:

$$|p_1| \approx \frac{1}{R_I(g_{m6}R_{II}C_c)}$$



2.) The left-half plane output pole:

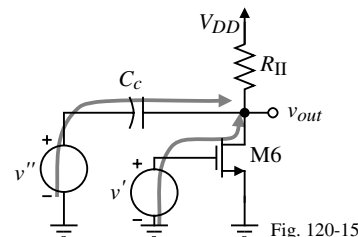
$$|p_2| \approx \frac{g_{m6}}{C_{II}}$$



3.) Right-half plane zero (Zeros always arise from multiple paths from the input to output):

$$v_{out} = \left( \frac{-g_{m6}R_{II}(1/sC_c)}{R_{II} + 1/sC_c} \right) v' + \left( \frac{R_{II}}{R_{II} + 1/sC_c} \right) v'' = \frac{-R_{II} \left( \frac{g_{m6}}{sC_c} - 1 \right)}{R_{II} + 1/sC_c} v$$

where  $v = v' = v''$ .



## Influence of the Mirror Pole

Up to this point, we have neglected the influence of the pole,  $p_3$ , associated with the current mirror of the input stage. A small-signal model for the input stage that includes  $C_3$  is shown below:

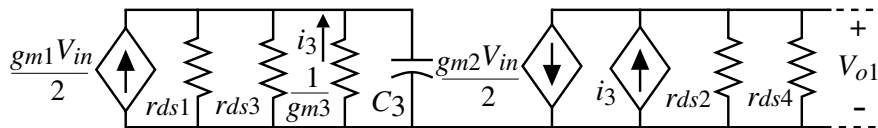


Fig. 120-16

The transfer function from the input to the output voltage of the first stage,  $V_{o1}(s)$ , can be written as

$$\frac{V_{o1}(s)}{V_{in}(s)} = \frac{-g_{m1}}{2(g_{ds2} + g_{ds4})} \left[ \frac{g_{m3} + g_{ds1} + g_{ds3}}{g_{m3} + g_{ds1} + g_{ds3} + sC_3} + 1 \right] \approx \frac{-g_{m1}}{2(g_{ds2} + g_{ds4})} \left[ \frac{sC_3 + 2g_{m3}}{sC_3 + g_{m3}} \right]$$

We see that there is a pole and a zero given as

$$p_3 = -\frac{g_{m3}}{C_3} \quad \text{and} \quad z_3 = -\frac{2g_{m3}}{C_3}$$

## Influence of the Mirror Pole – Continued

Fortunately, the presence of the zero tends to negate the effect of the pole. Generally, the pole and zero due to  $C_3$  is greater than  $GB$  and will have very little influence on the stability of the two-stage op amp.

The plot shown illustrates the case where these roots are less than  $GB$  and even then they have little effect on stability.

In fact, they actually increase the phase margin slightly because  $GB$  is decreased.

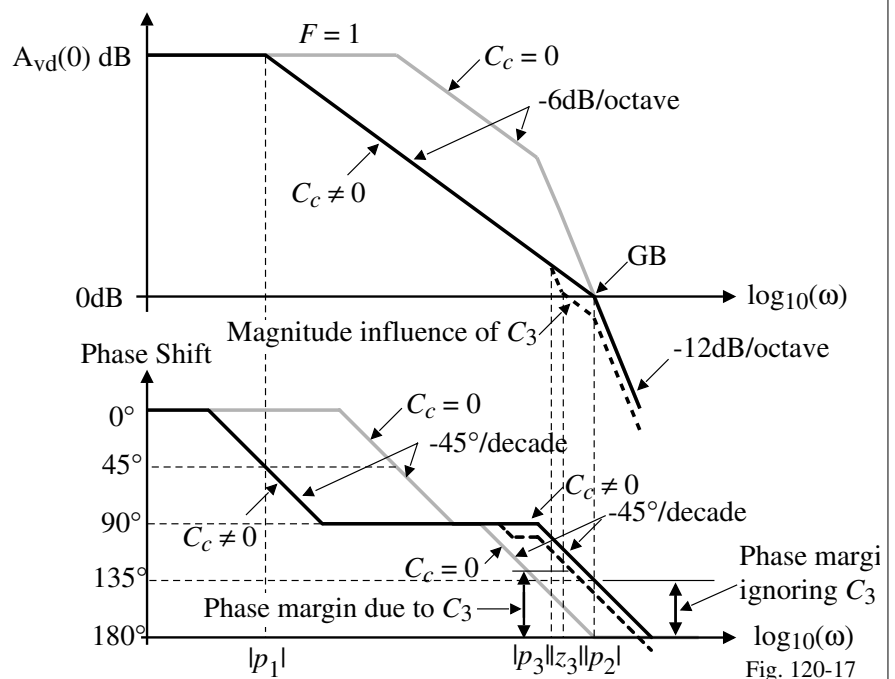


Fig. 120-17



## **SUMMARY**

### Compensation

- Designed so that the op amp with unity gain feedback (buffer) is stable
- Types
  - Miller
  - Miller with nulling resistors
  - Self Compensating
  - Feedforward