

MODELING THE MEASURED EM INDUCTION RESPONSE OF TARGETS AS A SUM OF DIPOLE TERMS EACH WITH A DISCRETE RELAXATION FREQUENCY

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ABSTRACT

Broadband electromagnetic induction (EMI) sensors have been shown to be able to reduce false alarm rates and increase the probability of detecting landmines. To aid in the development of these sensors and associated detection algorithms, a testing facility and inversion technique have been developed to characterize the response of typical targets and clutter objects as a function of orientation and frequency.

Index Terms— *Electromagnetic induction, EMI, landmine detection, sensor*

1. INTRODUCTION

Simple electromagnetic induction (EMI) sensors are capable of detecting most landmines; however, they will also detect every buried metal object such as bottle tops, nails, shrapnel, bullets, etc. This results in an unacceptable false alarm rate. This is even more problematic for the detection of low-metal anti-personnel landmines as they are extremely difficult to distinguish from clutter using a simple EMI sensor. However, advanced EMI sensors that use a broad range of frequencies or a broad range of measurement times along with advanced signal processing have been shown to be capable of discriminating between buried landmines and many types of buried metal clutter [1-6]. The broadband responses of many targets are relatively invariant to burial depth; however, the responses of some objects vary when they are tilted at arbitrary angles, which could cause missed detections.

To aid in the development of EMI sensors and associated detection algorithms, a testing facility and inversion technique have been developed to characterize the response of typical targets and clutter objects with respect to location, orientation, and frequency. The data from these measurements are used to develop models that are valid for any orientation of the object. Similar measurements in the field would be very difficult to perform due to the difficulty of accurately placing and rotating the target. It is difficult to analytically or numerically predict the response of many of these objects with accuracy due to uncertainties in the material parameters and geometry of the metal components in the objects. The objects are modeled as simple sets of

magnetic dipoles with discrete relaxation frequencies. It is envisioned that the models derived in this work will be utilized to reduce false alarm rates and increase the probability of detection for EMI sensors through improvements in both the hardware and the processing algorithms used to detect and discriminate buried targets.

2. MEASUREMENT SYSTEM

A laboratory positioner was developed with three automated translational stages (x, y, and z), two automated rotational stages (yaw and pitch), and one manually-adjusted rotational stage (roll, not labeled) as indicated in Fig. 1 [7]. An EMI sensor array [8] is shown in Fig. 1b with the three-loop target. This system is used to measure the response of targets in a three-dimensional region as a function of angular orientation.

3. MODEL

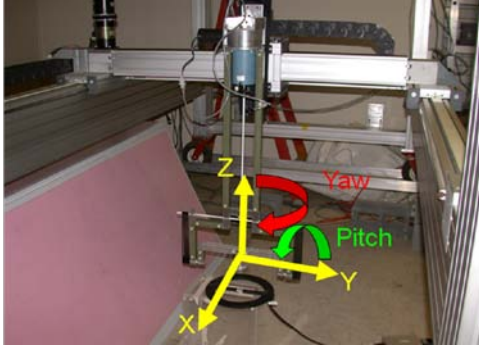
A simple dipole model is developed to predict the target response of an EMI system as a function of its position and orientation.

3.1. Magnetic Polarizability of a Target

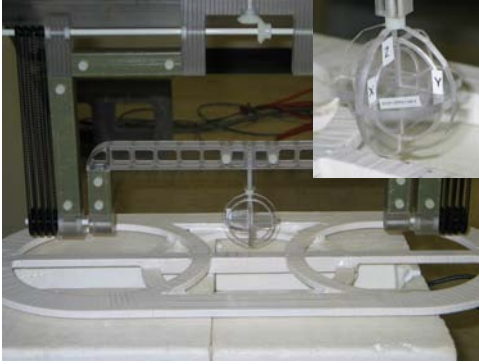
When a target is placed in a time-varying magnetic field, magnetic moments are induced due to two effects: the magnetic permeability of the target and the electrical conductivity that allows the induction of current. If the target is electrically small, the magnetic moments can be expressed in terms of the equivalent magnetic dipole moment, \mathbf{m} . The dipole moment can be calculated from the magnetic polarizability tensor, \mathbf{M} , when the exciting field \mathbf{H}_T is relatively constant over the extent of the object: $\mathbf{m} = \mathbf{M}\mathbf{H}_T$. A target will often have multiple relaxations and will have a corresponding tensor for each relaxation that contains the orientation/symmetry information for the relaxation. The magnetization for such a target can be written as the sum [2]:

$$\mathbf{M}(\omega) = T_0 \mathbf{T}_0 - \sum_k T_k \left(\frac{j\omega / \zeta_k}{1 + j\omega / \zeta_k} \right) \mathbf{T}_k \quad (1)$$

where T_k is a real constant, ζ_k is the relaxation frequency, and \mathbf{T}_k is a real, symmetric, second rank tensor. The first term is due to the bulk magnetic permeability of the target, which is assumed to be frequency independent, and the second term is due to the currents induced in the target. The tensor \mathbf{T}_k results from the path of the current for the k^{th} relaxation.



a)



b)

Fig. 1. Experimental measurement facility for EMI target characterization: a) Single EMI sensor head with automated translational (x , y , and z) and rotational (yaw about z and pitch about y) axes labeled, manual rotational axis (roll about x) unlabeled; b) EMI sensor head array with three-loop target.

3.2. EMI System

Consider the example EMI system that consists of transmit and receive coils which interact with a target. Here \mathbf{H}_T is the field at the target generated by the transmit coil when the coil is driven with the current I_T , and \mathbf{m} is the dipole moment induced on the target. It can be shown by using reciprocity that the received voltage due to the target is [9, 10]:

$$V_R = \frac{j\omega\mu}{I_R} \mathbf{H}_R^T \mathbf{m} = \frac{j\omega\mu}{I_R} \mathbf{H}_R^T \mathbf{M} \mathbf{H}_T \quad (2)$$

where \mathbf{H}_R is the magnetic field generated when the receiving loop driven with the current I_R . Note that \mathbf{H}_T , \mathbf{H}_R , and \mathbf{m} can be, and are likely to be, in different directions. The received

voltage is compared to a reference voltage to obtain the response \mathcal{R} of the system:

$$\mathcal{R} = \frac{V_R}{V_X} = \frac{\mu}{L_X I_T I_R} \mathbf{H}_R^T \mathbf{M} \mathbf{H}_T \quad (3)$$

where $V_X = j\omega L_X I_T$ is the reference voltage from a reference transformer with mutual inductance L_X which is also driven by transmit current I_T . The response of the system when the target is rotated by the Euler angles α , β , and γ can be written as

$$\mathcal{R} = \frac{\mu}{L_X I_T I_R} \mathbf{H}_R^T \mathbf{R}^T(\alpha, \beta, \gamma) \mathbf{M} \mathbf{R}(\alpha, \beta, \gamma) \mathbf{H}_T \quad (4)$$

where \mathbf{R} is a rotation matrix[11]. The angle α is the yaw angle, β is the pitch angle, and γ is the roll angle; the yaw and pitch angles are indicated in figure 1. The magnetic fields $\mathbf{H}_T(x, y, z)$ and $\mathbf{H}_R(x, y, z)$ are calculated as a function of position by direct application of the Biot-Savart law from the geometry of the wires in the coils.

4. ESTIMATION OF TARGET PARAMETERS

In a typical measurement, the response \mathcal{R} is measured as a function of position and orientation, and in this section, a method for inverting the measurement to obtain the model parameters is presented. Direct fitting of the parameters in equations 1 and 4 is difficult because of the non-linear relationship between the relaxation frequencies ζ_k and the orientation of the tensors with the response. The non-linear relation for ζ_k is dealt with using the procedure described in [12]. The non-linear relation with the orientation of the tensors is dealt with by using the symmetry of the target. The tensor \mathbf{T}_k is expanded in a set of basis tensors \mathcal{T}_k which span the allowable range of \mathbf{T}_k . This expansion allows for solution using a linear least-squares approximation procedure. For this paper, two types of expansions will be considered. First, all targets can be oriented so that \mathbf{T}_k is diagonal [11]. It can also be shown that \mathbf{T}_k is diagonal for certain targets with symmetries about the coordinate axes[13]. The three loop target shown in figure 1b is an example of a target with this symmetry. For these targets, \mathbf{T}_k is expanded as

$$\begin{aligned} T_k \mathbf{T}_k &= M_{k,xx} \mathcal{T}_{xx} + M_{k,yy} \mathcal{T}_{yy} + M_{k,zz} \mathcal{T}_{zz} \\ &= M_{k,xx} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} + M_{k,yy} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} + M_{k,zz} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}. \end{aligned} \quad (5)$$

Second, some targets have additional symmetry about the z -axis which can be used to further simplify the expansion:

$$\begin{aligned}
T_k \mathbf{T}_k &= M_{k,cy} \mathcal{T}_{cy} + M_{k,zz} \mathcal{T}_{zz} \\
&= M_{k,cy} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} + M_{k,zz} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}. \quad (6)
\end{aligned}$$

A penny, a nail, and a rifle cartridge are examples of objects with this type of symmetry. In all of these expansions, the coefficients are positive since they are aligned with the physical dipoles.

A zero-mean down-track filter is applied to the measured response to lessen the effects of positional errors in the x direction, to increase the signal to noise ratio, to help mitigate the response to the positioning system, and to mostly remove the direct coupling between the transmit and receive coils[8]. The filtered response is obtained at the discrete observations O_p :

$$\mathcal{R}_F(O_p) = \frac{\mu}{L_x I_T I_R} \left\{ \sum_n M_{0n} \mathbf{P}_{pn} - \sum_k \left[\left(\frac{j\omega_p / \zeta_k}{1 + j\omega_p / \zeta_k} \right) \sum_n M_{kn} \mathbf{P}_{pn} \right] \right\}$$

where ω_p is the frequency at the p^{th} observation. \mathbf{P}_{pn} contains the filtering, the projections of the tensors on the fields and the rotation matrices:

$$\mathbf{P}_{pn} = \sum_g F(x_g + x_p) \mathbf{H}_R^T(x_g, y_p, z_p) \mathbf{R}^T \mathcal{T}_n \mathbf{R} \mathbf{H}_T(x_g, y_p, z_p) \quad (8)$$

where $x_p, y_p, z_p, \alpha_p, \beta_p,$ and γ_p are the locations/orientations at the p^{th} observation and where F is the down-track filter described in [8]. The values of ζ_k are determined in this paper by computing the discrete spectrum of relaxation frequencies (DSRF) as described in [12] on a response that is averaged over all the discrete observations O_p . The parameters M_{kn} are obtained by writing (7) as a matrix equation as shown in [14]. Multiple locations and/or orientations are included to get enough measurements to make it possible to solve for the parameters M_{kn} . The non-zero values of M_{kn} will be positive, and many of the parameters M_{kn} can be zero since not every relaxation will have all the tensor components..

5. RESULTS

Two targets were measured that are made with loops of wire so that their theoretical parameters are easily estimated to demonstrate the accuracy of the modeling technique. The first loop target is made with 22 AWG copper wire formed into a circular loop with a circumference of 10 cm, which has a theoretical relaxation frequency of 10.0 kHz. The theoretical and estimated model parameters are graphed as a function of the relaxation frequency, $f_r = \zeta/2\pi$, in Fig. 2a for the single-loop target. The agreement between the theory

and experiment is very good. Since the loop is z-directed, the theory predicts a single z component for the dipole expansion at 10.0 kHz; however, the expansion in equation (8) is used for this inversion which allows for three components. Ideally, the inversion would return exactly zero amplitudes for the additional components, but because of measurement errors, the additional components will not always have an amplitude of exactly zero. The additional components near 10.0 kHz are seen to be very small in figure 2a. These components could be due to a small misalignment of the target in the measurement system. Note that in the measured results, there is a weak relaxation at 250 kHz that is not predicted theoretically. We believe that this is due to the finite thickness of the wire that is not taken into account in the theoretical model.

The second loop target is a three-loop target that consists of three orthogonal loops of copper wire as shown in Fig. 1b. The theoretical and estimated model parameters are graphed as a function of the relaxation frequency in Fig. 2b. Each relaxation frequency for this target has a different component due to the arrangement of the loops. The agreement between the theory and experiment is very good, even for this more complex target.

Results are shown in Figures 2c through 2e for an anti-personnel low-metal landmine, a nail, and a 9 mm cartridge. The parameters M_{0n} are due to the frequency independent magnetic permeability of the targets and are labeled as DC on the figures. These parameters are essentially zero for three of the targets since they are non-magnetic, but are non-zero for the landmine and the steel nail since they are magnetic. The magnetic targets have relaxation terms, M_{kn} , in addition to the magnetic terms, M_{0n} . The experimental results for this broad range of targets demonstrate the capability of the model to represent the targets.

6. CONCLUSIONS

An experimental facility has been established to measure the response of typical targets for EMI sensors as a function of location and orientation. A method of modeling the targets as an expansion of simple dipoles with discrete relaxations is presented along with a method to invert the measured responses to obtain the model parameters. The models are valid for any position and orientation of the target. Targets with known models were measured to establish the accuracy of the technique. Numerous other targets have been measured and their models catalogued.

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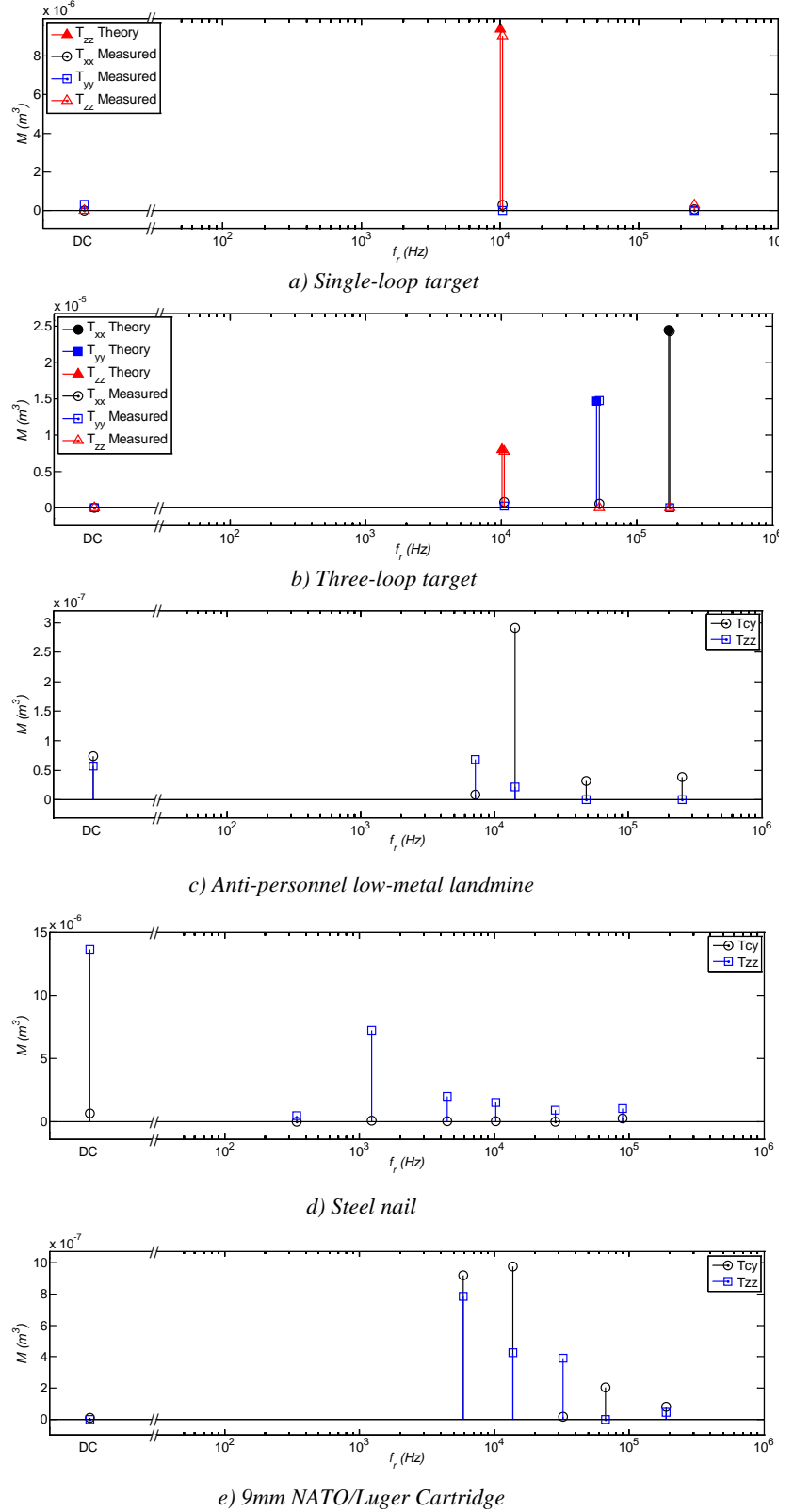


Fig. 2. Estimated model parameters as a function of relaxation frequency.