# LECTURE 100 – APPLICATIONS OF FREQUENCY SYNTHESIZERS (References – Previous ECE 6440 Class Notes)

## **Objective**

The objective of this presentation is:

- 1.) Show the applications of frequency synthesizers at the system level
- 2.) Introduce concepts of phase noise and spurious responses

## **Outline**

- Review of Modulation
- Phase Noise
- Use of a PLL for Modulation and Demodulation
- Frequency Synthesizers
- Continuation of the Design of a 450-475 MHz DPLL Synthesizer
- Summary

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## **REVIEW OF MODULATION**

## **Amplitude Modulation**



$$v_{am}(t) = V_c[1 + m_a \cos \omega_m t] \cos \omega_c t$$

where

$$m_{a} = \text{modulation index} = \frac{K_{a}V_{m}}{V_{c}}$$

$$v_{am}(t) = V_{c}\cos\omega_{c}t + m_{a}V_{c}\cos\omega_{m}t\cos\omega_{c}t$$

$$= V_{c}\cos\omega_{c}t + V_{c}[\frac{m_{a}}{2}\cos(\omega_{c}t + \omega_{m}t) + \frac{m_{a}}{2}\cos(\omega_{c}t - \omega_{m}t)]$$

Spectrally,





# Spurs Caused by Unintentional AM

An example:



In a frequency synthesizer, AM modulation is unwanted and  $m_a <<1$ . The single-sideband (SSB) to carrier ratio is given as,

Power of carrier = 
$$P_c = \frac{(V_c)^2}{R}$$
 and

A Power of sideband =  $P_{side}$  =

... The SSB spur to carrier ratio in dBc is given as

$$20\log_{10}\left(\frac{P_{side}}{P_c}\right) = 20\log_{10}\left(\frac{m_a}{2}\right) \text{ dBc}$$

Thus a small amplitude modulation index can cause reasonably large spurs.

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 $\left(m_a \frac{V_c}{2}\right)^2$ 

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# **Removal of AM by Amplitude Limiting**

Amplitude limiting can be used to remove AM.



It will turn out that phase noise has two components – amplitude noise and phase noise. Because of the above example, phase noise is much more important.

Illustration of amplitude and phase noise:





Output frequency:

 $\omega_o(t) = \omega_c + k_f V_m \cos \omega_m t = \omega_c + \Delta \omega_c \cos \omega_m t$ The peak value of  $\omega_c = \Delta \omega_c = k_f V_m$  (called the frequency deviation)

$$\theta(t) = \int \omega_o(t) dt = \int [\omega_c + k_f V_m \cos \omega_m t] dt = \omega_c t + \frac{k_f V_m}{\omega_m} \sin \omega_m t$$

$$\therefore \quad v_{fm}(t) = V_c \cos\left(\omega_c t + \frac{k_f V_m}{\omega_m} \sin \omega_m t\right) = V_c \cos(\omega_c t + \beta \sin \omega_m t)$$

where

$$\beta = \text{modulation index} = \frac{\Delta \omega_c(\text{peak})}{\omega_m} = \frac{k_f V_m}{\omega_m}$$

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#### **Phase Modulation**



Peak phase deviation and modulation index =  $\theta_d = k_p V_m$ 

$$v_{pm}(t) = V_c \cos(\omega_c t + k_p V_m \sin \omega_m t) = V_c \cos(\omega_c t + \theta_d \sin \omega_m t)$$

Note that in the time domain, FM and PM are identical.

$$v_{fm}(t) = V_c \cos(\omega_c t + \beta \sin \omega_m t)$$
$$v_{pm}(t) = V_c \cos(\omega_c t + \theta_d \sin \omega_m t)$$

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#### **Spectrum of FM Modulation**

Find the frequency domain equivalence of FM modulation:

Using Bessel function of the first kind with order *n*, we get

$$\begin{aligned} v_{fm}(t) &= V_c \left\{ J_0(\beta) \sin \omega_c t + J_1(\beta) [\sin(\omega_c + \omega_m)t - \sin(\omega_c - \omega_m)t] \\ &+ J_2(\beta) [\sin(\omega_c + 2\omega_m)t - \sin(\omega_c - 2\omega_m)t] + J_3(\beta) [\sin(\omega_c + 3\omega_m)t - \sin(\omega_c - 3\omega_m)t] + \cdots \right\} \end{aligned}$$

Spectrum:



**Observations:** 

- The modulation index,  $\beta$ , controls the number of sidebands
- The spacing between the sidebands is  $f_m$
- $BW \approx 2(\Delta f_{peak} + f_m)$  (Carson's rule)

For narrowband FM,  $\beta \ll 1$ 

$$\therefore$$
  $J_0(\beta) \approx 1$ ,  $J_1(\beta) \approx 0.5\beta$ , and  $J_n(\beta) \approx 0$  if  $n \ge 2$ 

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## **FM and PM Spurs** ( $\beta \ll 1$ )

Spurs are unintentional and not wanted.

If  $\beta \ll 1$  and  $\theta_d \ll 1$ , then  $\beta \approx \theta_d$ 

The spectrum for FM or PM becomes,



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#### **SSB Spurs**

Example:

Find the SSB spur if a VCO power supply has a ripple of  $10\mu V(\text{peak})$  at 1000Hz that is superimposed on the control voltage of the VCO.



Assuming that the power supply ripple is superimposed on the controlling voltage, we get,

 $\Delta f_c = (5 \times 10^6 \text{ Hz/V})(10 \mu \text{V}) = 50 \text{ Hz}$ 

The unintentional modulation frequency is 1000Hz.

$$\therefore \quad \beta = \frac{\Delta f_c}{f_m} = \frac{50}{1000} = 0.050 \quad \Rightarrow \quad \text{SSB Spur} = 20 \, \log_{10} \left( \frac{0.05}{2} \right) = -34 \, \text{dBc}$$

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#### **Influence of Frequency Multiplication on Spurs**

Consider the case of a frequency doubler.

$$V_{c}$$

$$V_{s}$$

$$V_{s$$

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#### Effect of Frequency Multiplication on FM/PM Spurs – Continued

From the previous results, we see that as *n* increases, the spur level at the output





## **Single Sideband Noise Spectral Density**

Assume the carrier experiences a single-frequency FM or PM. Consider the power in the sideband at an offset of  $f_m$  from the carrier in a 1Hz bandwidth:

$$\mathcal{L}_{fm} = \frac{\text{Noise power per Hz bandwidth}}{\text{Total carrier power}} = \frac{f_m^{0.5}}{P_c}$$
where  $P_{\theta}(f)$  is the normalized power spectral density  
(W/Hz) and  $P_c$  is the total power under the power  
spectrum and is called the carrier power.  
If the power spectral density is a constant over the 1  
Hz bandwidth, then the phase noise can be attributed  
to an equivalent sine wave modulation of phase  
deviation,  $\theta_d$ .  
 $\mathcal{L}_{c} \mathcal{L}_{fm} = \frac{P_{\theta}(f_m)}{P_c} = \frac{\left(\frac{\theta_d}{2}\right)^2}{P_c}$   
The total noise power in both sidebands is  $S_{\theta}(f_m) = 2\mathcal{L}(f_m)$   
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The phase noise data for a 1mW, 40MHz VCO.

-200  $10^{\overline{4}}$  $10^{5}$  $10^{6}$ 100 1000 Frequency Offset from Carrier (Hz) SU03H04P6 An empirical expression for this SSB phase noise is  $\mathscr{L}(f_m) = 10 \log_{10} \left\{ \frac{2FkT}{P_c} \left[ 1 + \left( K_1 \frac{f_1}{f_m} \right) \right] \left[ 1 + \left( K_2 \frac{f_2}{f_m} \right)^2 \right] \right\}$ 

where *F*,  $K_1$  and  $K_2$  are scaling factors and  $f_1 = 200\pi$  and  $f_2 = 2\pi 10^5$  in the above graph.

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How is noise on the reference signal processed by the frequency synthesizer?



The closed loop transfer function from the reference phase noise,  $\theta_{r,n}$  is the same as for the reference phase,  $\theta_r$  or  $\theta_1$ , to the output phase.

$$\therefore \quad \frac{\theta_2'(s)}{\theta_{r,n}(s)} = \frac{\frac{K_v F(s)}{N}}{s + \frac{K_v F(s)}{N}}$$

(Can divide this by *N* to get the phase noise at the input)

Note that the PLL loop is a lowpass filter for the reference noise.



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#### **VCO Phase Noise**

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How is noise on due to the VCO processed by the frequency synthesizer?



The transfer function from the VCO noise,  $\theta_{o,n}$  to the output,  $\theta_2$ , is given as

$$\frac{\theta_2'(s)}{\theta_{2,n}(s)} = \frac{\frac{s}{N}}{\frac{K_v F(s)}{N}}$$
The PLL loop acts like a highpass filter to the VCO noise. Note that the choice of  $F(s)$  does not alter the highpass nature of the relationship.  

$$\frac{\theta_2'(s)}{\theta_{2,n}(s)} = \frac{\frac{s}{N}}{\frac{K_v F(s)}{N}}$$
Amplitude
$$\frac{-20\log_{10}(N)}{\frac{1}{2\pi N}}$$

VC not

Fig. 100-19

 $2\pi N$ 



# **Phase Noise at the Output Frequency**

What is the phase noise at the output due to the reference noise and the VCO noise?



- Note that the PLL loop acts like a bandpass filter for the reference noise and a bandreject filter for the VCO noise.
- The total noise is the rms sum of the two noises.

$$\theta_{n,total} = 20\log_{10} \left[ \sqrt{\left(10^{\theta_{r,n}/20}\right)^2 + \left(10^{\theta_{VCO,n}/20}\right)^2} \right] = 10\log_{10} \left[10^{\theta_{r,n}/10} + 10^{\theta_{VCO,n}/10}\right]$$

- The total noise can be obtained by directly adding the noise powers.
- The loop bandwidth can be set to minimize the total phase noise.

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# USING A PLL FOR MODULATION AND DEMODULATION FM Modulation of a PLL

A PLL is frequency modulated by introducing a baseband voltage signal,  $v_{fm}$ , into the input of the VCO.



The transfer function for FM modulation of the above PLL is,

$$\frac{\omega_o(s)}{V_{fm}(s)} = \frac{sK_o}{s + \frac{K_v F(s)}{N}}$$

The fundamental behavior of the loop is determined by letting F(s) = 1 to get

$$\frac{\omega_o(s)}{V_{fm}(s)} = \frac{sK_o}{\frac{K_v}{s + \frac{K_v}{N}}} \quad \rightarrow \quad \text{Highpass filter with a gain of } K_o \text{ and } \omega_{-3\text{dB}} = \frac{K_v}{N}$$

Note that modulation frequencies less than  $\omega_{-3dB}$  are attenuated.

## **Phase Modulation of a PLL**

A PLL can be phase modulated by injecting a baseband modulating voltage at the output of the phase detector as shown below.



The transfer function from the modulation input,  $v_{pm}$ , to the output phase,  $\theta_o$ , is given as

$$\frac{\theta_o(s)}{V_{pm}(s)} = \frac{F(s)K_o}{s + \frac{K_v F(s)}{N}}$$

The fundamental behavior of the loop is determined by letting F(s) = 1 to get

$$\frac{\theta_o(s)}{V_{pm}(s)} = \frac{K_o}{\frac{K_v}{s + \frac{K_v}{N}}} \rightarrow \text{Lowpass filter with a gain of } \frac{N}{K_d} \text{ and } \omega_{-3dB} = \frac{K_v}{N}$$

Note that modulation frequencies greater than  $\omega_{-3dB}$  are attenuated.

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# FM Demodulation using a PLL

The PLL can also serve as an FM demodulator. The following block diagram is a PLL FM receiver.



The transfer function from  $\omega_r$  to the output of the demodulator,  $v_f$ , is given as

$$\frac{V_f(s)}{\omega_r(s)} = \frac{K_d F(s)}{s + \frac{K_v F(s)}{N}}$$

The fundamental behavior of the loop is determined by letting F(s) = 1 to get

$$\frac{V_f(s)}{\omega_r(s)} = \frac{K_d}{\frac{K_v}{s + \frac{K_v}{N}}} \longrightarrow \text{Lowpass filter with a gain of } \frac{N}{K_o} \text{ and } \omega_{-3\text{dB}} = \frac{K_v}{N}$$

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Comments:

• Note that the loop demodulates signals *within* the loop bandwidth. This configuration is called a "modulation tracking loop". Within the loop the transfer function is,

$$\frac{V_f(s)}{\omega_r(s)} = \frac{N}{K_o}$$

• The VCO linearity controls the linearity of the FM demodulator. Many applications use N = 1.



interestione, the phase detector determines the intearity of the 1 w demod

In many cases, the phase modulation is transmitted without a carrier. An example of BPSK is shown.



Ordinary PLLs phase lock to the carrier and hence cannot be used to demodulate this type of modulation.

The most common methods for recovering the carrier and demodulating the signal are the *squaring loop, remodulator,* and the *Costas loop*.

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## **Phase Demodulation with No Carrier – Squaring Loop**

Block diagram of the demodulator:





## **Phase Demodulation with No Carrier – Remodulator Loop**

One of the problems with the squaring loop is that the carrier frequency is doubled. The remodulator multiplies the input by  $m(t)\cos(\theta_e)$  rather than  $m(t)\sin(\omega_c t)$  avoiding the double-frequency carrier.



## **Phase Demodulation with No Carrier – Costas Loop**

The Costas loop reverses the order of multiplication putting the phase detector before the multiplier.



Putting the phase detector before the multiplier replaces the noise-limiting bandpass filter with a simpler lowpass filter.

The phase demodulation schemes presented above (squaring loop, remodulator, and Costas) are only good for binary modulation. Similar but more complex circuits are required for quaternary PSK.

### FREQUENCY SYNTHSIZERS

## **Multi-Loop DPLL Frequency Synthesizer**

A multi-loop frequency synthesizer is a way of implementing very small channel requirements without having a small reference frequency.

The two-loop or multi-loop frequency synthesizer can provide the required frequency resolution while meeting the capture time and VCO phase noise specifications.



# **Fractional-N PLL Frequency Synthesizer**

The fractional-N PLL has the ability to resolve the channel spacing to less than  $f_{ref}/N$ .



How do you increase the frequency resolution by a factor of 10?

- 1.) Replace the 0.1MHz reference with a 0.01MHz reference. However, this will slow the loop by a factor of 10.
- 2.) Use a multi-loop synthesizer.
- 3.) Use the fractional-N method.

Principle of the fractional-N technique:

Divide by  $N_1$  for P periods and by  $N_2$  for Q periods.

Effective 
$$N = \left(\frac{P}{P+Q}\right)N_1 + \left(\frac{Q}{P+Q}\right)N_2 = \frac{PN_1 + QN_2}{P+Q}$$

#### **Fractional-N PLL Frequency Synthesizer - Continued**

Comments on the Fractional-N Technique:

• Usually we take  $N_2 = N_1 + 1$  to determine the average output frequency. Therefore,

$$N_{aver} = \frac{PN_1 + Q(N_1 + 1)}{P + Q} = N_1 + \frac{Q}{P + Q} = N_1 + f$$

where *f* is the frequency step and is  $0 \le f \le 1$ 

• Consider the example from the previous slide.

Assume we want a resolution of  $f_{ref}/10$ . Therefore,  $N_1 = 999$ , P = 1,  $N_2 = 1000$ , and Q = 9. This gives,

$$f_{out} = 0.1 \text{MHz} \left( \frac{PN_1 + Q(N_1 + 1)}{P + Q} \right) = 0.1 \left( \frac{1.999 + 9.1000}{10} \right) \text{MHz}$$
$$= 0.1 \left( \frac{9999}{10} \right) \text{MHz} = 99.99 \text{MHz}$$

• Another example follows. Let P = 5 and Q = 5. The output frequency is

$$f_{out} = 0.1 \text{MHz}\left(\frac{PN_1 + Q(N_1 + 1)}{P + Q}\right) = 0.1\left(\frac{5.999 + 5.1000}{10}\right) \text{MHz} = 99.95 \text{MHz}$$

By adjusting P and Q we can fill in all 10kHz increments between the 100kHz reference steps.

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#### **Fractional-N PLL Frequency Synthesizer - Continued**

Implementation of the fractional-N synthesizer:

• The change of one unit in the frequency divider is most often accomplished with the *swallow counter* or *cycle swallower* shown below.



- Upon command, the cycle swallower removes a pulse and thus increases the overall frequency division by one.
- The fractional-*N* synthesizer method sets the average frequency to the required value. However, the reference frequency is not equal to the feedback frequency.
- Since the reference frequency is not equal to the fedback frequency, there will be a phase jitter that is introduced in the form of spurs

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The problem of spurs in a fractional-N PLL:



How do the spurs occur?

- 1.) Assume that the VCO output frequency is the desired 99.99MHz.
- 2.) 99.99MHz divided by 1000 puts 99.99kHz to the phase detector.
- 3.) The phase detector generates a phase error in the direction to increase the VCO frequency.
- 4.) The phase error accumulates until the divider changes to 999.
- 5.) Then the phase error is reversed and causes the VCO frequency to decrease.
- 6.) The result of this behavior is a sawtooth ripple on the phase detector output voltage.
- 7.) If not removed, this ripple would cause severe spurs in the output of the synthesizer.

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# **Fractional-N PLL Frequency Synthesizer - Continued**

A method to remove the spurs from the Fractional-*N* synthesizer:



The above circuit uses a DAC to create an inverse phase-voltage to keep the control voltage to the VCO flat.

Comments:

- By increasing P and Q it is possible to greatly increase the frequency resolution.
- The phase noise performance depends upon how well the DAC removes the reference noise sidebands.

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## CONTINUATION OF THE 450MHZ FREQUENCY SYNTHESIZER EXAMPLE Specifications

Design a DPLL frequency synthesizer that meets the following specifications:

| Frequency Range:      | 450 – 475 MHz                              |
|-----------------------|--|
| Channel Spacing:      | 25 kHz                                     |
| Modulation:           | FM from 300 to 3000 Hz                     |
| Modulation Deviation: | ±5kHz                                      |
| Loop Type:            | Type 2                                     |
| Loop Order:           | Second order                               |
| VCO Gain:             | $K_o = 1.25$ MHz/V = 7.854 Mradians/sec./V |
| Phase Detector Type:  | PFD ( $\beta = 2\pi$ )                     |
| Phase Detector Gain:  | $K_d = 0.796$ V/radian                     |
| Reference Frequency   |  |
| FM Spurs:             | < -70 dBc                                  |
| Prescaler:            | 20/21 Dual Modulus                         |

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#### **Reference Frequency Ripple Voltage Modulation of the VCO**

Since the ripple on the VCO control voltage is the same as PM, we can use the previous results developed for PM.

$$\frac{\theta_o(s)}{V_{pm}(s)} = \frac{F(s)K_o}{s + \frac{K_v F(s)}{N}}$$

The filter was given as,

$$F(s) = \frac{sR_2C + 1}{sR_1C} = \frac{s\tau_2 + 1}{s\tau_1}$$
 where  $\tau_1 = 0.419$  ms and  $\tau_2 = 1.575$  ms

The closed-loop transfer function is given as,

$$\frac{\theta_o(s)}{V_{pm}(s)} = \frac{\left(\frac{s\tau_2 + 1}{s\tau_1}\right)K_o}{\frac{K_v\left(\frac{s\tau_2 + 1}{s\tau_1}\right)}{s + \frac{K_v\left(\frac{s\tau_2 + 1}{s\tau_1}\right)}{N}}} = \frac{K_o\left(\frac{\tau_2}{\tau_1}\right)\left(s + \frac{1}{\tau_2}\right)}{s^2 + \left(\frac{K_v}{N}\right)\left(\frac{\tau_2}{\tau_1}\right)s + \frac{K_v}{N\tau_1}} = \frac{K_o\left(\frac{\tau_2}{\tau_1}\right)\left(s + \frac{1}{\tau_2}\right)}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

At high frequencies (greater than the closed-loop bandwidth), the transfer function becomes,

$$\frac{\theta_o(s)}{V_{pm}(s)} = \frac{K_o}{s} \left( \frac{\tau_2}{\tau_1} \right) \qquad \rightarrow \qquad \theta_o = \frac{K_o}{s} \left( \frac{\tau_2}{\tau_1} \right) V_{pm}$$

Therefore, the reference frequency ripple voltage present at the input of the loop filter causes PM spurs to appear at the output.

One of the more significant sources of reference frequency modulation comes from the input offset voltage of the filter if op amps are used.



# Source of Reference Frequency Modulation – Continued

Applying  $v_{pm}/2 = 18\mu V$  to the reference modulation transfer function gives the following result. The spurs created by the reference and its harmonics can be read from the graph.

#### **PSPICE** Input File:



## **Redesign with a Third-Order Loop**

Because the spur specification is not met, we will design a third-order filter to get the additional attenuation needed.

Third-Order Filter:



The passive pre-filter will provide the additional attenuation. It also has the effect of increasing the rise and fall times of the pulsed input to the op amp which reduces the slew-rate requirements of the op amp.

To achieve the -70dBc spur level we need 20.6dB of additional attenuation. Since we want 20.6dB of additional attenuation at 25kHz, find the pole frequency of the filter.

No. of decades = 
$$10^{\frac{\text{Attenuation}}{20}} = 10^{\frac{20.6}{20}} = 1.03$$
 decades  
 $f_c = \frac{f_r}{10^{\text{ndec}}} = \frac{f_r}{10^{1.03}} = \frac{25 \text{kHz}}{10.715} = 2.333 \text{kHz}$   
It can be shown that  $C_1 = \frac{4}{R_1 2 \pi f_c} = 0.114 \mu \text{F}$ 

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#### **Third-Order Reference Modulation Transfer Function**

The new filter function can be expressed as,

$$F(s) = \frac{s\tau_2 + 1}{s\tau_1} \left(\frac{1}{s\tau_3 + 1}\right)$$

The transfer function from the reference modulation to the output phase is

$$\frac{\theta_o(s)}{V_{pm}(s)} = \frac{\left(\frac{s\tau_2 + 1}{s\tau_1(s\tau_3 + 1)}\right)K_o}{\frac{K_v(s\tau_2 + 1)}{s + \frac{K_v(s\tau_1(s\tau_3 + 1))}{N}}} = \frac{K_o(\frac{\tau_2}{\tau_1})(s + \frac{1}{\tau_2})}{s^3\tau_3 + s^2 + \left(\frac{K_v}{N}\right)(\frac{\tau_2}{\tau_1})s + \frac{K_v}{N\tau_1}}$$

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## Spur Performance for the Third-Order Filter



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**Results:** 







The loop gain of the third-order PLL is given by,

 $LG(s) = \frac{s\tau_2 + 1}{s^2\tau_1} \left( \frac{K_d K_o}{N(s\tau_3 + 1)} \right)$ 

Using the previously designed parameters we get the open-loop gain below.

#### **PSPICE** File:



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#### **VCO Phase Noise**

The third-order transfer function from the VCO phase noise to the output is,



The transfer function from the VCO noise,  $\theta_{o,n}$  to the output,  $\theta_2$ , is given as

$$\frac{\theta_{2}'(s)}{\theta_{o,n}(s)} = \frac{\frac{s}{N}}{s + \frac{K_{v}F(s)}{N}} = \frac{\frac{s}{N}}{\frac{K_{v}\left(\frac{s\tau_{2}+1}{s\tau_{1}}\right)\left(\frac{1}{s\tau_{3}+1}\right)}{s + \frac{K_{v}\left(\frac{s\tau_{2}+1}{s\tau_{1}}\right)\left(\frac{1}{s\tau_{3}+1}\right)}{N}} = \frac{s^{3}\tau_{3} + s^{2}}{s^{3}\tau_{3} + s^{2} + s\frac{K_{v}}{N}\frac{\tau_{2}}{\tau_{1}} + \frac{K_{v}}{N\tau_{1}}}$$



## VCO Phase Noise - Continued



# Lock Range, Lock Time and Pull-In Range for the 450MHz Frequency Synthesizer Example

Lock Range:

 $\Delta \omega_L = 2N\beta \zeta \omega_n = (2)(18,000)(2\pi)(0.726)(905) = 148.62$  Mradians/sec.

 $\Delta f_L = 23.65 \text{ MHz}$ 

Lock Time:

$$T_L \approx \frac{1}{\omega_n} = \frac{1}{905} = 1.1$$
 msec.

Pull-In Range:

The pull-in range is theoretically infinite. It will be limited by the dynamic range of the loop components.

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#### **Prescaler Design**

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The equations needed to fine the *M*- and *A*-counter values are:

$$f_o = [(M-A)P + (P+1)A]f_r$$

$$N = \frac{f_o}{f_r} = (M-A)P + (P+1)A = MP + A$$

$$\frac{N}{P} = M + \frac{A}{P} \quad \text{where} \quad M = \text{integer of}\left(\frac{N}{P}\right) \quad \text{and} \; A = N-MP$$

For this example, we find the values of *M* and *A* to produce an output frequency of 451.075MHz.

$$N = \frac{f_o}{f_r} = \frac{451.075 \text{ MHz}}{0.025 \text{ MHz}} = 18043$$
  

$$M = \text{integer of} \left(\frac{N}{P}\right) = \frac{18043}{20} = 902.15 = 902 \text{ and } A = N-MP = 18043-902 \cdot 20 = 3$$

Other values are calculated in a similar manner:

| M   | MP     | A     |         |         |             |         |  |  |
|-----|--------|-------|---------|---------|-------------|---------|--|--|
|     | P = 20 | 0     | 1       | 2       |             | 19      |  |  |
| 900 | 18000  | 450.0 | 450.025 | 450.050 | $(MP+A)f_r$ | 450.475 |  |  |
| 901 | 18020  | 450.5 | 450.525 | 450.550 | •••         | 450.975 |  |  |
| ••• | •••    | •••   | •••     | •••     |             | •••     |  |  |
| 949 | 18980  | 474.5 | 474.525 | 474.550 | •••         | 474.975 |  |  |

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#### **SUMMARY**

• Review of Modulation AM, FM, and PM Spurs Influence of frequency multiplication and division on spurs

• Phase Noise

Single sideband noise Reference phase noise

VCO phase noise

- Use of a PLL for Modulation and Demodulation
- Frequency Synthesizers

Achieving small channel resolution without using small reference frequencies

- Multi-loop
- Fractional N

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